



Basic Math Skills

Student Workbook



Place Value

EXAMPLE

Look at the place of the underlined digit.

Write the name of the place of the underlined digit.

198 _____ tens _____

Directions Write the name of the place for each underlined digit.

- | | | | | | |
|------------------------|-------|-------------------------|-------|--------------------------|-------|
| 1. 2,4 <u>0</u> 6 | _____ | 21. 29 <u>4</u> | _____ | 41. 88,2 <u>1</u> 0 | _____ |
| 2. 1 <u>2</u> 8 | _____ | 22. 5, <u>0</u> 20,007 | _____ | 42. 9 <u>0</u> ,909 | _____ |
| 3. 70, <u>8</u> 35 | _____ | 23. 9 <u>1</u> 9,078 | _____ | 43. <u>2</u> 03,872,221 | _____ |
| 4. 17, <u>5</u> 01 | _____ | 24. 4, <u>0</u> 09 | _____ | 44. <u>9</u> 10,573 | _____ |
| 5. 301,3 <u>3</u> 9 | _____ | 25. 5, <u>6</u> 83 | _____ | 45. 10,7 <u>1</u> 0 | _____ |
| 6. 10, <u>0</u> 02 | _____ | 26. 687, <u>6</u> 33 | _____ | 46. <u>7</u> 37,098 | _____ |
| 7. 49 <u>1</u> ,918 | _____ | 27. 48, <u>0</u> 40 | _____ | 47. <u>4</u> 0,910 | _____ |
| 8. <u>4</u> 6,023 | _____ | 28. 384,9 <u>9</u> 5 | _____ | 48. 10, <u>0</u> 2 | _____ |
| 9. <u>6</u> ,005 | _____ | 29. 8, <u>8</u> 37 | _____ | 49. <u>9</u> ,033,921 | _____ |
| 10. 59, <u>7</u> 00 | _____ | 30. 23, <u>0</u> 00,821 | _____ | 50. 8 <u>1</u> 0,022,033 | _____ |
| 11. <u>3</u> 4,000 | _____ | 31. <u>1</u> ,010,001 | _____ | 51. 3 <u>0</u> 0,941 | _____ |
| 12. 500, <u>0</u> 69 | _____ | 32. <u>5</u> 3 | _____ | 52. 2, <u>6</u> 71 | _____ |
| 13. <u>3</u> 41 | _____ | 33. 5, <u>0</u> 78 | _____ | 53. 94, <u>7</u> 24 | _____ |
| 14. 10, <u>0</u> 00 | _____ | 34. <u>7</u> 08,583 | _____ | 54. <u>8</u> 03,921 | _____ |
| 15. 1, <u>0</u> 00,000 | _____ | 35. 61, <u>2</u> 22 | _____ | 55. <u>5</u> 06 | _____ |
| 16. 3, <u>9</u> 02,885 | _____ | 36. <u>7</u> 01,865 | _____ | 56. 1, <u>0</u> 34 | _____ |
| 17. <u>5</u> 03 | _____ | 37. 70, <u>7</u> 38 | _____ | 57. 9 <u>2</u> 0 | _____ |
| 18. 16, <u>0</u> 30 | _____ | 38. <u>5</u> 01,775 | _____ | 58. 1, <u>0</u> 23 | _____ |
| 19. <u>2</u> ,000,003 | _____ | 39. 102, <u>8</u> 95 | _____ | 59. 462, <u>9</u> 87 | _____ |
| 20. 73, <u>9</u> 99 | _____ | 40. 71, <u>9</u> 90 | _____ | 60. 10, <u>9</u> 35 | _____ |

Writing Numbers

EXAMPLE

Read the numeral. Write the numeral in words.

1,241 one thousand, two hundred forty-one**Directions** Write the following numerals in words.

1. 1,208 _____

2. 204 _____

3. 4,801 _____

4. 80,026 _____

5. 92,224 _____

6. 44,659 _____

7. 602,875 _____

8. 6,096,089 _____

9. 673,218,003 _____

10. 830,002 _____

Number Translations

EXAMPLE

Read the amount written in words. Write the numeral for the amount.

Four thousand, one hundred ninety-two 4,192**Directions** Write the following amounts in numerals.

1. Three thousand, five hundred thirty-six _____
2. Five hundred six _____
3. Seven hundred forty-nine _____
4. Five thousand, nine _____
5. Seven thousand, three hundred twenty-one _____
6. Nine thousand, two _____
7. Nine thousand, five hundred _____
8. Thirty-one thousand, four _____
9. Fifty-seven thousand, nine hundred _____
10. Eighty thousand, six hundred thirty-two _____
11. Forty-two thousand, three _____
12. Ninety-one thousand, four hundred eleven _____
13. Seven hundred thousand _____
14. Nine hundred thousand, sixty-four _____
15. Seven hundred seventy-one thousand, five hundred forty-nine _____
16. Four hundred fifty-five million _____
17. Three hundred five million, twenty-eight thousand, two _____
18. Eight thousand, eleven _____
19. Three hundred sixty-three thousand, five hundred four _____
20. Seventy thousand, nine hundred forty-two _____

Rounding Whole Numbers

EXAMPLE

Read the number. Round the number to the nearest tens place.
Round numbers 5–9 up. Round numbers 1–4 down.

$$26 = \underline{\quad 30 \quad}$$

Directions Round these numbers to the nearest tens place.

- | | | |
|-------------------|--------------------|---------------------|
| 1. 48 = _____ | 7. 5 = _____ | 13. 4 = _____ |
| 2. 305 = _____ | 8. 803 = _____ | 14. 18 = _____ |
| 3. 4,056 = _____ | 9. 617 = _____ | 15. 102,005 = _____ |
| 4. 408 = _____ | 10. 61,092 = _____ | 16. 4,506 = _____ |
| 5. 9,911 = _____ | 11. 777 = _____ | 17. 9 = _____ |
| 6. 72,099 = _____ | 12. 290 = _____ | 18. 61 = _____ |

Directions Round these numbers to the nearest hundreds place.

- | | | |
|---------------------|-----------------------|---------------------|
| 19. 693 = _____ | 25. 29 = _____ | 31. 34,988 = _____ |
| 20. 349 = _____ | 26. 3,002,091 = _____ | 32. 89 = _____ |
| 21. 9,012 = _____ | 27. 71 = _____ | 33. 129,999 = _____ |
| 22. 7,521 = _____ | 28. 91,029 = _____ | 34. 10,891 = _____ |
| 23. 43,071 = _____ | 29. 6,018 = _____ | 35. 509 = _____ |
| 24. 102,009 = _____ | 30. 33,951 = _____ | 36. 780 = _____ |

Directions Round these numbers to the nearest thousands place.

- | | | |
|--------------------|--------------------|---------------------|
| 37. 199 = _____ | 42. 90,098 = _____ | 47. 298 = _____ |
| 38. 499 = _____ | 43. 1,058 = _____ | 48. 78,475 = _____ |
| 39. 1,500 = _____ | 44. 501 = _____ | 49. 470,512 = _____ |
| 40. 25,509 = _____ | 45. 99 = _____ | 50. 19,000 = _____ |
| 41. 999 = _____ | 46. 301 = _____ | |

Addition of Whole Numbers

EXAMPLE

Write the problem in vertical form. Add.

$$18 + 162 + 171 + 8 = \underline{\quad 359 \quad}$$

$$\begin{array}{r} 11 \\ 18 \\ 162 \\ 171 \\ + 8 \\ \hline 359 \end{array}$$

Directions Rewrite the following addends in the vertical form and add.

- | | |
|--|--|
| 1. $32 + 141 + 68 + 122 =$ _____ | 18. $905 + 624 + 861 + 968 =$ _____ |
| 2. $4 + 37 + 812 + 774 + 1 =$ _____ | 19. $6,241 + 8,548 + 9,092 =$ _____ |
| 3. $8 + 35 + 77 + 273 + 65 =$ _____ | 20. $558 + 523 + 128 + 8,241 =$ _____ |
| 4. $54 + 76 + 90 + 725 =$ _____ | 21. $264 + 63 + 7,253 + 2 =$ _____ |
| 5. $701 + 33 + 83 + 61 + 374 =$ _____ | 22. $73 + 8,263 + 78 + 521 =$ _____ |
| 6. $7 + 837 + 504 + 91 + 522 =$ _____ | 23. $42 + 3,547 + 8,142 + 467 =$ _____ |
| 7. $93 + 705 + 866 + 73 =$ _____ | 24. $8,263 + 990 + 352 + 37 =$ _____ |
| 8. $45 + 38 + 401 + 5,000 =$ _____ | 25. $7,364 + 364 + 902 + 36 =$ _____ |
| 9. $86 + 59 + 63 + 27 + 105 =$ _____ | 26. $889 + 902 + 836 + 2,431 =$ _____ |
| 10. $395 + 57 + 82 + 273 + 88 =$ _____ | 27. $390 + 263 + 7,746 + 477 =$ _____ |
| 11. $304 + 771 + 826 + 776 =$ _____ | 28. $3,746 + 7,500 + 9,928 + 388 =$ _____ |
| 12. $366 + 8,261 + 8,837 + 912 =$ _____ | 29. $6,635 + 809 + 300 + 646 =$ _____ |
| 13. $6,372 + 75 + 908 + 76 =$ _____ | 30. $9,745 + 4,869 + 7,089 + 3,745 =$ _____ |
| 14. $874 + 7,601 + 406 + 837 =$ _____ | 31. $36 + 2,006 + 215 + 116 =$ _____ |
| 15. $7,091 + 5,308 + 354 + 34 =$ _____ | 32. $2,117 + 3,591 + 6,711 + 2,883 =$ _____ |
| 16. $645 + 823 + 806 + 7,735 =$ _____ | 33. $7,001 + 375 + 6 + 39 =$ _____ |
| 17. $6,657 + 4,321 + 7,341 =$ _____ | |

Directions Solve the following word problems with addition.

- 34.** Mark collects 178 pounds of scrap iron and 85 pounds of copper. Find the total weight of the metal. _____
- 35.** Tara purchases 280 square feet of carpet for her living room and 250 square feet for her bedroom. Find the total number of square feet she purchases. _____

Subtraction of Whole Numbers

EXAMPLE

Write the problem in vertical form. Subtract.

From 821 subtract 71. $\underline{\quad 750 \quad}$

$$\begin{array}{r} 712 \\ \cancel{8}21 \\ - 71 \\ \hline 750 \end{array}$$

Directions Rewrite these subtraction problems in the vertical form. Then subtract.

- | | |
|---|--|
| 1. $694 - 22 =$ _____ | 15. $3,049 - 1,906 =$ _____ |
| 2. From 384 subtract 75. _____ | 16. Subtract 786 from 25,004. _____ |
| 3. $602 - 113 =$ _____ | 17. $46,974 - 18,860 =$ _____ |
| 4. From 102 subtract 89. _____ | 18. From 65,208 subtract 56,987. _____ |
| 5. $856 - 773 =$ _____ | 19. $7,890 - 5,699 =$ _____ |
| 6. Subtract 871 from 1,029. _____ | 20. Subtract 61,098 from 87,987. _____ |
| 7. $552 - 498 =$ _____ | 21. $67,951 - 56,508 =$ _____ |
| 8. Subtract 528 from 717. _____ | 22. From 10,001 subtract 9,802. _____ |
| 9. $4,852 - 665 =$ _____ | 23. $78,000 - 6,784 =$ _____ |
| 10. From 3,810 subtract 1,922. _____ | 24. Subtract 675 from 1,000. _____ |
| 11. $3,952 - 3,877 =$ _____ | 25. $362,900 - 87,098 =$ _____ |
| 12. Subtract 9,099 from 10,099. _____ | 26. Subtract 81,321 from 601,030. _____ |
| 13. $12,923 - 8,973 =$ _____ | 27. $70,981 - 69,673 =$ _____ |
| 14. From 16,242 subtract 10,987. _____ | 28. From 508,821 subtract 91,055. _____ |

Directions Solve the following word problems with subtraction.

- 29.** Van sells 185 tickets to the school's Staff Talent Show.
If he was given 350 tickets to sell, how many does he have left to sell? _____
- 30.** Cassie plans a 475-mile trip. She drives 296 miles the first day.
How many miles must she drive the second day to complete her trip? _____

Multiplication Practice

EXAMPLE

Multiply the number in the left column by the number in the top row.

$$\begin{array}{r|l} & 4 \\ 3 & 12 \end{array}$$

Directions Fill in the multiplication facts. Multiply each number in the left column by each number on the top row. Write the product of each pair of numbers in the box where the column and the row meet.

1.

×	0	1	2	3	4	5	6	7	8	9	10
0	0	0	0								
1	0	1	2								
2											
3											
4											
5											
6											
7											
8											
9											
10											

2.

×	6	2	3	0	9	10	8	7	5	4	1
2											
9											
5											
4											
8											
0											
7											
6											
3											
1											
10											

Multiplication by Powers of Ten

EXAMPLES

When you multiply a number by 10, write the number.
Then write a zero at the end. $235 \times 10 = 2,350$

When you multiply a number by 100, write the number.
Then write two zeros at the end.

$$235 \times 100 = 23,500$$

When you multiply a number by 1,000, write the number.
Then write three zeros at the end.

$$235 \times 1,000 = 235,000$$

Directions Multiply by these powers of ten.

- | | |
|-----------------------------------|---------------------------------|
| 1. $325 \times 10 =$ _____ | 21. $412 \times 1,000 =$ _____ |
| 2. $421 \times 100 =$ _____ | 22. $906 \times 1,000 =$ _____ |
| 3. $4,631 \times 10 =$ _____ | 23. $10,802 \times 100 =$ _____ |
| 4. $6,023 \times 100 =$ _____ | 24. $104 \times 100 =$ _____ |
| 5. $702 \times 100 =$ _____ | 25. $56 \times 10 =$ _____ |
| 6. $3,011 \times 1,000 =$ _____ | 26. $13 \times 100 =$ _____ |
| 7. $3,203 \times 100 =$ _____ | 27. $9 \times 1,000 =$ _____ |
| 8. $26,190 \times 10 =$ _____ | 28. $83 \times 1,000 =$ _____ |
| 9. $1,043 \times 100 =$ _____ | 29. $183 \times 1,000 =$ _____ |
| 10. $50,783 \times 1,000 =$ _____ | 30. $7 \times 1,000 =$ _____ |
| 11. $72 \times 1,000 =$ _____ | 31. $801 \times 100 =$ _____ |
| 12. $38 \times 1,000 =$ _____ | 32. $334 \times 10 =$ _____ |
| 13. $106 \times 100 =$ _____ | 33. $632 \times 10 =$ _____ |
| 14. $81 \times 100 =$ _____ | 34. $4,567 \times 100 =$ _____ |
| 15. $4,123 \times 10 =$ _____ | 35. $5 \times 100 =$ _____ |
| 16. $3,007 \times 1,000 =$ _____ | 36. $20,304 \times 100 =$ _____ |
| 17. $962 \times 1,000 =$ _____ | 37. $100 \times 1,000 =$ _____ |
| 18. $300 \times 10 =$ _____ | 38. $20,011 \times 100 =$ _____ |
| 19. $4,305 \times 10 =$ _____ | 39. $4,302 \times 100 =$ _____ |
| 20. $4,020 \times 1,000 =$ _____ | 40. $10,001 \times 100 =$ _____ |

Multiplication of Whole Numbers

EXAMPLE

Write the problem in vertical form. Multiply.

$52 \times 42 = \underline{\quad 2,184 \quad}$

$$\begin{array}{r} 52 \\ \times 42 \\ \hline 104 \\ + 208 \\ \hline 2,184 \end{array}$$

Directions Rewrite these multiplication problems in the vertical form and multiply.

- | | |
|--------------------------------|----------------------------------|
| 1. $24 \times 22 =$ _____ | 15. $920 \times 724 =$ _____ |
| 2. $61 \times 18 =$ _____ | 16. $856 \times 326 =$ _____ |
| 3. $201 \times 43 =$ _____ | 17. $3,021 \times 307 =$ _____ |
| 4. $85 \times 72 =$ _____ | 18. $638 \times 800 =$ _____ |
| 5. $712 \times 66 =$ _____ | 19. $4,160 \times 110 =$ _____ |
| 6. $819 \times 94 =$ _____ | 20. $8,522 \times 574 =$ _____ |
| 7. $465 \times 20 =$ _____ | 21. $5,021 \times 4,000 =$ _____ |
| 8. $762 \times 300 =$ _____ | 22. $7,000 \times 387 =$ _____ |
| 9. $301 \times 300 =$ _____ | 23. $5,448 \times 673 =$ _____ |
| 10. $784 \times 100 =$ _____ | 24. $7,361 \times 6,000 =$ _____ |
| 11. $629 \times 150 =$ _____ | 25. $4,000 \times 3,000 =$ _____ |
| 12. $607 \times 515 =$ _____ | 26. $4,000 \times 4,000 =$ _____ |
| 13. $5,763 \times 501 =$ _____ | 27. $3,500 \times 5,100 =$ _____ |
| 14. $7,114 \times 35 =$ _____ | 28. $6,702 \times 1,023 =$ _____ |

Directions Solve the following word problems with multiplication.

29. Leah runs 4 miles every day before school for exercise.

If she runs 179 days, how many miles will she run? _____

30. Each student in Mr. Brown's class donates 15 sandwiches to the school picnic. If 38 students are in Mr. Brown's class, how many sandwiches are donated? _____

Division of Whole Numbers

EXAMPLE

Write the problem in standard form. Divide.

$$168 \div 6 = \underline{\quad 28 \quad}$$

$$\begin{array}{r} 28 \\ 6 \overline{)168} \\ \underline{-12} \\ 48 \\ \underline{-48} \\ 0 \end{array}$$

Directions Rewrite the following division problems in the standard form and divide.

- | | |
|-----------------------------|------------------------------|
| 1. $128 \div 4 =$ _____ | 15. $3,036 \div 6 =$ _____ |
| 2. $477 \div 9 =$ _____ | 16. $8,844 \div 11 =$ _____ |
| 3. $266 \div 7 =$ _____ | 17. $6,030 \div 3 =$ _____ |
| 4. $480 \div 5 =$ _____ | 18. $5,400 \div 6 =$ _____ |
| 5. $824 \div 8 =$ _____ | 19. $1,710 \div 6 =$ _____ |
| 6. $864 \div 4 =$ _____ | 20. $1,820 \div 13 =$ _____ |
| 7. $1,290 \div 10 =$ _____ | 21. $14,910 \div 21 =$ _____ |
| 8. $1,771 \div 7 =$ _____ | 22. $15,625 \div 25 =$ _____ |
| 9. $1,008 \div 9 =$ _____ | 23. $12,720 \div 12 =$ _____ |
| 10. $3,069 \div 9 =$ _____ | 24. $13,797 \div 27 =$ _____ |
| 11. $948 \div 12 =$ _____ | 25. $27,060 \div 60 =$ _____ |
| 12. $1,472 \div 16 =$ _____ | 26. $21,350 \div 35 =$ _____ |
| 13. $1,360 \div 16 =$ _____ | 27. $11,216 \div 16 =$ _____ |
| 14. $2,160 \div 12 =$ _____ | 28. $12,030 \div 30 =$ _____ |

Directions Solve these word problems with division.

29. The Jiffy Messenger Service travels a total of 2,954 miles in one 7-day week. How many miles do the messengers average each day? _____
30. Marvin collects 1,170 bottle tops over a 45-day period. How many bottle tops does he average per day? _____

More Division of Whole Numbers

EXAMPLE

Write the problem in standard form.

$1,333 \div 9 = \underline{\hspace{2cm}} \quad \text{Divide.}$

Express the remainder as a fraction.

Write the remainder over the divisor.

$$\begin{array}{r} 148 \frac{1}{9} \\ 9 \overline{) 1,333} \\ \underline{- 9} \\ 43 \\ \underline{- 36} \\ 73 \\ \underline{- 72} \\ 1 \end{array}$$

Directions Rewrite the following division problems in the standard form and divide. Express the remainders in fractional form.

- | | |
|-----------------------------|------------------------------|
| 1. $1,237 \div 6 =$ _____ | 15. $8,175 \div 35 =$ _____ |
| 2. $898 \div 6 =$ _____ | 16. $7,167 \div 20 =$ _____ |
| 3. $415 \div 6 =$ _____ | 17. $9,063 \div 75 =$ _____ |
| 4. $2,115 \div 11 =$ _____ | 18. $10,613 \div 53 =$ _____ |
| 5. $749 \div 6 =$ _____ | 19. $8,891 \div 22 =$ _____ |
| 6. $1,218 \div 12 =$ _____ | 20. $7,776 \div 78 =$ _____ |
| 7. $863 \div 7 =$ _____ | 21. $3,820 \div 45 =$ _____ |
| 8. $3,017 \div 15 =$ _____ | 22. $29,666 \div 30 =$ _____ |
| 9. $6,915 \div 4 =$ _____ | 23. $6,770 \div 65 =$ _____ |
| 10. $812 \div 82 =$ _____ | 24. $41,080 \div 80 =$ _____ |
| 11. $1,367 \div 17 =$ _____ | 25. $12,161 \div 11 =$ _____ |
| 12. $3,575 \div 28 =$ _____ | 26. $58,775 \div 40 =$ _____ |
| 13. $1,992 \div 10 =$ _____ | 27. $23,815 \div 15 =$ _____ |
| 14. $2,115 \div 63 =$ _____ | 28. $91,090 \div 90 =$ _____ |

Directions Solve these word problems with division. Express remainders in fractional form.

29. Maija's mother owned her car for 9 years, driving a total of 136,910 miles. Find the average number of miles driven per year. _____
30. Daniel drove his car 816 miles using 22 gallons of gas. Compute Daniel's gas mileage by dividing the number of miles driven by the number of gallons used. _____

Dividing Numbers by Powers of Ten

EXAMPLE

Write the problem in standard form and divide.

$$480 \div 10 =$$

 Or move the decimal point one place to the left
for each zero in the divisor.

$$48.0 \div 10 =$$

$$\begin{array}{r} 48 \\ 10 \overline{) 480} \\ \underline{- 40} \\ 80 \\ \underline{- 80} \\ 0 \end{array}$$

Directions Divide by these powers of ten.

- | | |
|-------------------------------------|-------------------------------------|
| 1. $840 \div 10 =$ _____ | 21. $451,000 \div 1,000 =$ _____ |
| 2. $65,000 \div 100 =$ _____ | 22. $390,000 \div 10 =$ _____ |
| 3. $2,000 \div 100 =$ _____ | 23. $680,000 \div 100 =$ _____ |
| 4. $4,630 \div 10 =$ _____ | 24. $4,060,300 \div 10 =$ _____ |
| 5. $9,600 \div 100 =$ _____ | 25. $19,600 \div 10 =$ _____ |
| 6. $140,000 \div 1,000 =$ _____ | 26. $9,603,000 \div 1,000 =$ _____ |
| 7. $191,000 \div 10 =$ _____ | 27. $5,000,000 \div 100 =$ _____ |
| 8. $920,000 \div 100 =$ _____ | 28. $7,000,000 \div 10 =$ _____ |
| 9. $62,000 \div 100 =$ _____ | 29. $8,000,000 \div 100 =$ _____ |
| 10. $35,600 \div 100 =$ _____ | 30. $123,000 \div 1,000 =$ _____ |
| 11. $385,000 \div 100 =$ _____ | 31. $96,000,000 \div 1,000 =$ _____ |
| 12. $25,000,000 \div 1,000 =$ _____ | 32. $43,000 \div 1,000 =$ _____ |
| 13. $4,000,000 \div 1,000 =$ _____ | 33. $43,070,600 \div 10 =$ _____ |
| 14. $806,000 \div 10 =$ _____ | 34. $8,000,000 \div 10,000 =$ _____ |
| 15. $962,000 \div 100 =$ _____ | 35. $902,000 \div 100 =$ _____ |
| 16. $305,000 \div 100 =$ _____ | 36. $304,000,000 \div 100 =$ _____ |
| 17. $1,800,000 \div 1,000 =$ _____ | 37. $201,111,000 \div 10 =$ _____ |
| 18. $600,000 \div 1,000 =$ _____ | 38. $76,000,000 \div 1,000 =$ _____ |
| 19. $581,000 \div 10 =$ _____ | 39. $50,000 \div 10,000 =$ _____ |
| 20. $720,600 \div 100 =$ _____ | 40. $240,000 \div 10,000 =$ _____ |

Basic Operations with Whole Numbers

EXAMPLES

Add.

$$\begin{array}{r} 22 \\ 354 \\ 356 \\ 765 \\ + 87 \\ \hline 1,562 \end{array}$$

Subtract.

$$\begin{array}{r} 112914 \\ \cancel{2,304} \\ - 567 \\ \hline 1,737 \end{array}$$

Multiply.

$$\begin{array}{r} 23 \\ \times 44 \\ \hline 092 \\ + 92 \\ \hline 1,012 \end{array}$$

Divide.

$$\begin{array}{r} 1,145 \\ 3 \overline{) 3,435} \\ \underline{- 3} \\ 0 \\ 4 \\ \underline{- 3} \\ 13 \\ \underline{- 12} \\ 15 \\ \underline{- 15} \\ 0 \end{array}$$

Directions Add.

- $243 + 321 + 132 + 68 =$ _____
- $5,067 + 23 + 505 + 40 =$ _____
- $1,102 + 705 + 4,033 =$ _____
- $5,122 + 567 + 504 + 3,402 =$ _____
- $30,304 + 4,030 + 20,300 + 1,102 =$ _____
- $203,340 + 94,059 + 304,450 =$ _____
- $2,000 + 90,089 + 50,481 =$ _____
- $10,223 + 4,055 + 506 + 8,690 =$ _____

Directions Subtract.

- $2,304 - 567 =$ _____
- $304,119 - 4,053 =$ _____
- $30,400 - 19,234 =$ _____
- $102,556 - 9,806 =$ _____
- $134,505 - 5,968 =$ _____
- $900,800 - 203,788 =$ _____
- $6,578,009 - 456,801 =$ _____
- $340,599 - 9,875 =$ _____

Directions Multiply.

- $23 \times 44 =$ _____
- $304 \times 32 =$ _____
- $579 \times 23 =$ _____
- $3,011 \times 44 =$ _____
- $4,503 \times 23 =$ _____
- $4,053 \times 206 =$ _____
- $5,098 \times 2,304 =$ _____
- $40,577 \times 3,092 =$ _____

Directions Divide. Write the remainders in the fractional form.

- $3,435 \div 3 =$ _____
- $2,034 \div 9 =$ _____
- $49,571 \div 9 =$ _____
- $30,455 \div 5 =$ _____
- $46,570 \div 45 =$ _____
- $30,575 \div 25 =$ _____

Averages

EXAMPLE

Find the average of these numbers: 25, 73, 80, 73, 33, 95

Step 1 Add.

$$\begin{array}{r} 25 \\ 73 \\ 80 \\ 73 \\ 33 \\ + 95 \\ \hline 379 \end{array}$$

Step 2 Divide.

$$\begin{array}{r} 63.16 \approx 63.2 \\ 6 \overline{) 379.00} \\ \underline{- 36} \\ 19 \\ \underline{- 18} \\ 10 \\ \underline{- 6} \\ 40 \\ \underline{- 36} \end{array}$$

Directions Compute the averages for the sets of numbers. Round to the nearest tenth.

- | | | | |
|---|-------|--|-------|
| 1. 14, 12, 15, 11, 12, 13 | _____ | 11. 3,004, 3,210, 3,387, 3,652, | _____ |
| 2. 83, 78, 53, 92, 67, 27 | _____ | 3,470, 3,521, 3,980, 3,922 | _____ |
| 3. 20, 28, 19, 31, 22, 18, 17, 30 | _____ | 12. 5,738, 5,755, 5,746, 5,789, | _____ |
| 4. 78, 98, 77, 67, 75, 90, 80, | _____ | 5,736, 5,725, 5,756, 5,731 | _____ |
| 90, 80, 75, 70 | _____ | 13. 230, 310, 222, 725, 600, 390, | _____ |
| 5. 30, 31, 37, 33, 38, 35, 32, | _____ | 512, 525, 510, 400, 500, 683 | _____ |
| 39, 34, 36 | _____ | 14. 3,021, 5,361, 2,630, 6,110, | _____ |
| 6. 44, 46, 64, 66, 62, 69, 41, 40 | _____ | 4,002, 3,006, 4,102, 4,120, | _____ |
| 7. 103, 110, 152, 173, 177, 100, | _____ | 4,972, 3,500, 2,310 | _____ |
| 150, 175, 152 | _____ | 15. 4,589, 4,530, 4,520, 4,500, | _____ |
| 8. 205, 273, 198, 350, 220, 180, | _____ | 4,530, 4,528, 4,501, 4,554 | _____ |
| 280, 220 | _____ | 16. 7,800, 7,853, 7,835, 7,850, | _____ |
| 9. 58, 74, 47, 83, 65, 36, 45, 46, | _____ | 7,812, 7,856, 7,851, 7,820 | _____ |
| 70, 53, 55, 38 | _____ | 17. 35, 78, 95, 83, 62, 89, 35, 60, | _____ |
| 10. 163, 219, 300, 512, 375, 602, | _____ | 40, 66, 10, 31, 62, 89, 95 | _____ |
| 735, 638, 881 | _____ | 18. 1,239, 1,264, 1,220, 1,250, | _____ |
| | | 1,235, 1,260, 1,285, 1,240, | _____ |
| | | 1,200, 1,290, 1,206 | _____ |

Directions Solve these word problems by computing the average.
Round the answers to the nearest tenth.

- 19.** Deborah works as a part-time car mechanic. She works 26 hours her first week. What is her average number of hours worked per day for four days? _____
- 20.** The band sells 523 tickets to its annual concert. There are 13 ticket sellers. Find the average number of tickets sold by each seller. _____

Exponents

EXAMPLE

Read the number. Change the number into a problem and write the amount.

$$2^3 = 2 \times 2 \times 2 = \underline{\quad 8 \quad}$$

Directions Express the following without exponents.

- | | | |
|--------------------|--------------------|---------------------|
| 1. $3^2 =$ _____ | 21. $20^3 =$ _____ | 41. $4^5 =$ _____ |
| 2. $4^2 =$ _____ | 22. $3^2 =$ _____ | 42. $21^2 =$ _____ |
| 3. $5^3 =$ _____ | 23. $5^4 =$ _____ | 43. $3^3 =$ _____ |
| 4. $4^3 =$ _____ | 24. $12^2 =$ _____ | 44. $10^6 =$ _____ |
| 5. $6^2 =$ _____ | 25. $10^3 =$ _____ | 45. $23^2 =$ _____ |
| 6. $10^2 =$ _____ | 26. $3^5 =$ _____ | 46. $14^2 =$ _____ |
| 7. $8^2 =$ _____ | 27. $22^3 =$ _____ | 47. $50^2 =$ _____ |
| 8. $2^5 =$ _____ | 28. $17^2 =$ _____ | 48. $100^2 =$ _____ |
| 9. $9^3 =$ _____ | 29. $15^2 =$ _____ | 49. $19^2 =$ _____ |
| 10. $5^2 =$ _____ | 30. $10^4 =$ _____ | 50. $33^2 =$ _____ |
| 11. $4^4 =$ _____ | 31. $12^3 =$ _____ | 51. $13^3 =$ _____ |
| 12. $2^4 =$ _____ | 32. $13^2 =$ _____ | 52. $16^2 =$ _____ |
| 13. $8^3 =$ _____ | 33. $20^2 =$ _____ | 53. $25^3 =$ _____ |
| 14. $9^2 =$ _____ | 34. $25^2 =$ _____ | 54. $17^3 =$ _____ |
| 15. $7^2 =$ _____ | 35. $15^3 =$ _____ | 55. $14^3 =$ _____ |
| 16. $10^5 =$ _____ | 36. $22^2 =$ _____ | 56. $5^5 =$ _____ |
| 17. $3^4 =$ _____ | 37. $11^3 =$ _____ | 57. $10^7 =$ _____ |
| 18. $6^3 =$ _____ | 38. $6^4 =$ _____ | 58. $11^4 =$ _____ |
| 19. $7^3 =$ _____ | 39. $2^6 =$ _____ | 59. $12^4 =$ _____ |
| 20. $11^2 =$ _____ | 40. $18^2 =$ _____ | 60. $10^9 =$ _____ |

Order of Operations

EXAMPLE

Follow the order of operations.

$2 + 4 \times 2 = \underline{\hspace{2cm}}$

$2 + 8 = \underline{10}$

Directions Find the answers. Perform the operations in the correct order.

- | | |
|---|---|
| 1. $3 + 5 \times 6 =$ _____ | 21. $8 \times 6 \div 4 - 12 \div 6 =$ _____ |
| 2. $3 \times 4 + 6 - 4 =$ _____ | 22. $2^3 \times 3 \div 6 + 12 - 3 =$ _____ |
| 3. $4 \times 8 + 16 \div 2 =$ _____ | 23. $45 \div 15 + 10 - 2^3 =$ _____ |
| 4. $5 \times 2 - 6 \div 2 =$ _____ | 24. $15 \div 3 - 5 + 10^2 =$ _____ |
| 5. $4^2 \times 2 + 5 - 32 =$ _____ | 25. $12^2 \div 6 - 20 + 7 =$ _____ |
| 6. $3 \times 2 \times 2^3 - 4^2 =$ _____ | 26. $8^2 + 9 \times 3 - 10 =$ _____ |
| 7. $7 + 6 \times 2 - 2 + 2^3 =$ _____ | 27. $18 \div 3^2 - 2 + 5^2 =$ _____ |
| 8. $18 - 2 \times 4^2 \div 4 =$ _____ | 28. $5^3 \div 5 - 10 + 2^3 =$ _____ |
| 9. $10 + 8 \times 6 \div 12 - 2 =$ _____ | 29. $81 \div 3^2 - 6 + 12 \div 2 =$ _____ |
| 10. $13 - 4 \times 5 \div 2 + 10 =$ _____ | 30. $3 \times 6 \div 2 - 5 + 7 =$ _____ |
| 11. $15 \times 3 - 5^2 + 10 =$ _____ | 31. $10^2 \div 5^2 + 5 \times 6 \div 2 =$ _____ |
| 12. $7^2 + 2^4 - 2^3 =$ _____ | 32. $25 \div 5^2 \times 5 + 5 - 10 =$ _____ |
| 13. $4 + 17 - 3 \times 7 =$ _____ | 33. $100 \div 10 \times 2^2 + 8 =$ _____ |
| 14. $12^2 - 10^2 + 5 \times 2 =$ _____ | 34. $18 - 9 \times 2 \div 3 + 3^2 =$ _____ |
| 15. $10^2 - 2 \times 4 + 3^2 =$ _____ | 35. $50 - 40 + 4 \times 7 =$ _____ |
| 16. $11^2 + 23 - 2^3 + 9 =$ _____ | 36. $28 \div 4 \times 6 - 20 =$ _____ |
| 17. $20 - 12 \div 6 \times 3 =$ _____ | 37. $3^3 \times 2^2 + 20 \div 2 =$ _____ |
| 18. $4^3 - 3 \times 12 \div 6 =$ _____ | 38. $6^2 \times 3 \div 2 - 4^2 =$ _____ |
| 19. $15 + 4 - 11 + 2^5 =$ _____ | 39. $14 \div 2 \times 3 - 21 =$ _____ |
| 20. $12 \times 2 \div 3 \times 2 + 3 =$ _____ | 40. $16 \times 2 \div 4 - 2 + 10 =$ _____ |

Factors

EXAMPLE

Factor the number.

$$F_{15} \quad 1 \times 15$$
$$3 \times 5$$

Choose the correct factors.

- a. 1, 5, 10, 15
- b. 1, 2, 3, 5
- c. 1, 3, 5, 15
- d. 1, 3, 6, 12

Directions Circle the answer that has the correct factors.

1. 24

- a. 1, 2, 4, 6, 8, 12, 14
- b. 1, 2, 4, 10, 12, 24
- c. 1, 2, 3, 4, 6, 8, 12, 24
- d. 2, 4, 6, 8, 10, 12, 24

6. 52

- a. 1, 12, 24, 26, 30, 52
- b. 26, 52
- c. 1, 2, 4, 13, 26, 52
- d. 1, 13, 15, 52

11. 36

- a. 2, 3, 4, 6, 8, 12, 24
- b. 1, 2, 3, 4, 6, 9, 12, 18, 36
- c. 1, 2, 4, 6, 8, 12, 36
- d. 1, 3, 4, 6, 8, 12, 36

2. 16

- a. 1, 4, 8, 16
- b. 1, 2, 4, 16
- c. 1, 2, 4, 8, 16
- d. 1, 2, 4, 8, 16, 32

7. 14

- a. 2, 7, 11, 14
- b. 1, 2, 7, 14, 28
- c. 2, 4, 7, 14
- d. 1, 2, 7, 14

12. 12

- a. 2, 3, 4, 6, 12
- b. 3, 4, 6, 12, 24
- c. 2, 4, 6, 24
- d. 1, 2, 3, 4, 6, 12

3. 32

- a. 1, 2, 8, 16, 32
- b. 1, 2, 8, 16, 32, 64
- c. 1, 2, 4, 8, 16, 32
- d. 2, 4, 6, 8, 10, 32

8. 42

- a. 1, 6, 7, 12, 21, 42
- b. 1, 2, 3, 6, 7, 14, 21, 42
- c. 1, 6, 12, 42
- d. 1, 2, 4, 12, 21, 42

13. 18

- a. 1, 2, 3, 6, 9, 18
- b. 1, 2, 3, 6, 9, 18, 32
- c. 1, 2, 3, 6, 9, 18, 36
- d. 1, 2, 3, 4, 6, 7, 18

4. 8

- a. 2, 4, 8
- b. 1, 2, 4, 8
- c. 1, 2, 4, 8, 16
- d. 1, 2, 4, 8, 12, 24

9. 13

- a. 1, 7, 13
- b. 1, 13
- c. 1, 7, 13, 26
- d. 1, 2, 13, 19

14. 20

- a. 2, 20
- b. 2, 5, 10, 15, 20
- c. 1, 2, 5, 10, 15, 20
- d. 1, 2, 4, 5, 10, 20

5. 10

- a. 2, 5
- b. 1, 2, 5, 10
- c. 1, 2, 5, 10, 20
- d. 1, 2, 5

10. 26

- a. 1, 2, 20, 26
- b. 1, 13, 26
- c. 1, 2, 13, 26
- d. 1, 26

15. 22

- a. 1, 11, 22
- b. 1, 11, 22, 44
- c. 1, 2, 11, 22
- d. 1, 22, 44



Multiples

EXAMPLE M_4

Find the multiples of 4.

$$\begin{array}{ccccc} 4 \times 0 & 4 \times 1 & 4 \times 2 & 4 \times 3 & 4 \times 4 \\ 0 & 4 & 8 & 12 & 16 \end{array}$$

Choose the correct multiples.

- a. 0, 1, 2, 4
- b. 0, 4, 10, 12
- c. 0, 1, 4, 8
- d. 0, 4, 8, 12**

Directions Circle the answer that has the correct multiples. Note: Some multiples may be missing from a correct answer.

1. M_2

- a. 2, 4, 6, 8, 11
- b. 0, 4, 6, 8, 12
- c. 0, 2, 4, 5, 6, 8
- d. 0, 2, 3, 4, 5, 6

6. M_3

- a. 0, 3, 5, 6, 9, 12
- b. 3, 6, 9, 12, 14
- c. 0, 3, 6, 12, 15
- d. 1, 3, 6, 9, 12, 15

11. M_5

- a. 0, 5, 10, 12, 15
- b. 0, 10, 15, 20, 30
- c. 1, 5, 10, 15, 20
- d. 0, 10, 18, 20, 25

2. M_{11}

- a. 0, 1, 11, 22, 121
- b. 0, 11, 22, 33, 44, 56
- c. 11, 22, 33, 111
- d. 0, 11, 22, 33, 121

7. M_7

- a. 0, 7, 14, 28, 56, 112
- b. 0, 3, 7, 14, 28, 35
- c. 0, 7, 11, 22, 33, 44
- d. 1, 7, 14, 28, 35, 40

12. M_{10}

- a. 0, 10, 15, 20, 25
- b. 0, 5, 10, 15, 20
- c. 10, 15, 20, 25, 30
- d. 0, 10, 30, 50, 100

3. M_4

- a. 0, 2, 4, 6, 8, 16
- b. 4, 8, 16, 32, 36
- c. 0, 4, 6, 8, 12, 20
- d. 0, 14, 28, 56, 100

8. M_9

- a. 0, 9, 18, 27, 36
- b. 0, 9, 27, 38, 45
- c. 0, 19, 38, 76
- d. 0, 1, 2, 3, 4, 5

13. M_{12}

- a. 0, 12, 24, 36, 44
- b. 0, 12, 16, 24, 28
- c. 0, 12, 24, 36, 48
- d. 0, 10, 12, 14, 16

4. M_6

- a. 0, 2, 4, 6, 8, 9
- b. 0, 6, 12, 18, 24
- c. 1, 6, 12, 18, 24
- d. 1, 3, 6, 9, 18, 24

9. M_{20}

- a. 0, 20, 40, 60, 80
- b. 0, 20, 30, 40, 50
- c. 1, 20, 40, 60, 80
- d. 1, 10, 20, 30, 40

14. M_{13}

- a. 13, 29, 39, 52
- b. 0, 13, 23, 39
- c. 1, 13, 26, 52
- d. 0, 13, 26, 39

5. M_{30}

- a. 0, 10, 30, 60, 90
- b. 0, 30, 60, 90, 120
- c. 0, 15, 30, 45, 60
- d. 1, 15, 30, 40, 60

10. M_{40}

- a. 0, 40, 80, 120, 160
- b. 1, 40, 80, 120, 160
- c. 1, 20, 40, 60, 80
- d. 0, 20, 40, 60, 80

15. M_{50}

- a. 1, 50, 100, 150
- b. 0, 50, 100, 150
- c. 1, 25, 50, 75
- d. 0, 10, 15, 25

Prime and Composite Numbers

EXAMPLE

Identify all the factors of a number. $F_9 = 1, 3, 9$

Tell whether the number is a prime or composite number.

9 has three factors, so it is a composite number.

Directions Write *prime* or *composite* for each number given.

- | | | |
|---------------|---------------|---------------|
| 1. 23 _____ | 19. 21 _____ | 37. 12 _____ |
| 2. 25 _____ | 20. 44 _____ | 38. 7 _____ |
| 3. 45 _____ | 21. 17 _____ | 39. 58 _____ |
| 4. 19 _____ | 22. 26 _____ | 40. 98 _____ |
| 5. 84 _____ | 23. 102 _____ | 41. 62 _____ |
| 6. 29 _____ | 24. 77 _____ | 42. 60 _____ |
| 7. 73 _____ | 25. 42 _____ | 43. 22 _____ |
| 8. 37 _____ | 26. 54 _____ | 44. 49 _____ |
| 9. 55 _____ | 27. 4 _____ | 45. 31 _____ |
| 10. 78 _____ | 28. 100 _____ | 46. 1 _____ |
| 11. 15 _____ | 29. 27 _____ | 47. 400 _____ |
| 12. 220 _____ | 30. 79 _____ | 48. 2 _____ |
| 13. 110 _____ | 31. 55 _____ | 49. 3 _____ |
| 14. 6 _____ | 32. 204 _____ | 50. 300 _____ |
| 15. 120 _____ | 33. 41 _____ | |
| 16. 72 _____ | 34. 155 _____ | |
| 17. 350 _____ | 35. 29 _____ | |
| 18. 410 _____ | 36. 57 _____ | |

Sets of Numbers

EXAMPLE

Identify the set of even numbers. Even numbers are multiples of 2.

1, 2, 3, 5, 6, 8, 10, 12

Set of even numbers 2, 6, 8, 10, 12

Directions Write the sets from the given numbers.

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20,

21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37,

38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50

1. The set of even numbers

2. The set of odd numbers

3. The set of prime numbers

4. The set of numbers that will divide into 100 with zero as a remainder

5. The set of numbers that is multiples of 3

6. The set of numbers that is multiples of 6

7. The set of numbers that is multiples of 10

8. The set of numbers that is multiples of 100

9. The set of numbers that is factors of 100

10. The set of numbers that is factors of 20

11. The set of numbers that is factors of 10

12. The set of numbers that is factors of 8

13. The set of numbers that is factors of 6

14. The set of numbers that is factors of 30

15. The set of numbers that is factors of 12

Prime Numbers

EXAMPLE

List prime numbers from the given set.

2, 3, 4, 5

Identify prime numbers, which are numbers that have exactly 2 factors.

2 has 2 factors

3 has 2 factors

4 has 3 factors

5 has 2 factors

Prime numbers are 2, 3, 5.

Directions Write the sets from the given numbers.

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20,

21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37,

38, 39, 40, 41, 42, 43, 44, 45

1. List the prime numbers in order from smallest to largest from the set given.

2. List the even numbers in order from smallest to largest from the set given.

3. List the odd numbers in order from smallest to largest from the set given.

4. Add pairs of prime numbers. Exclude 2 from your additions.

Can you predict an odd or even answer? _____ Summarize your results.

5. Add pairs of odd numbers. Can you predict an odd or even answer? _____

Summarize your results.

6. Add pairs of even numbers. Can you predict an odd or even answer? _____

Summarize your results.

Find the three prime addends for each of the following numbers.

7. $12 =$ _____

9. $14 =$ _____

8. $19 =$ _____

10. $21 =$ _____

Divisibility Tests

EXAMPLE

Use the divisibility test to determine if this number is divisible by 3.

$$123 \quad \text{Add the digits.} \quad 1 + 2 + 3 = 6$$

Determine if the sum is a multiple of 3. 6 is a multiple of 3.

123 is divisible by 3.

Directions Perform the divisibility test to complete the chart.
Write *Yes* or *No* for each space.

Number	Divisible by 2?	Divisible by 3?	Divisible by 5?
1. 12,034			
2. 31,241			
3. 21,453			
4. 3,040,511			
5. 989,798			
6. 10,233			
7. 20,394			
8. 3,012,211			
9. 50,321			
10. 293,100			

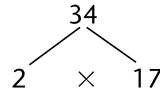
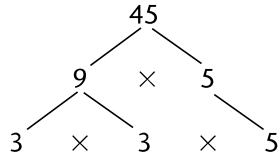
Number	Divisible by 4?	Divisible by 9?	Divisible by 10?
11. 20,349			
12. 13,536			
13. 12,350			
14. 182,340			
15. 125,350			
16. 30,451			
17. 10,800			
18. 100,237			
19. 584,750			
20. 95,832			

Prime Factorization

EXAMPLES

Complete factor trees to find prime factorization.

Find prime factors for 45 and 34.



Directions Complete factor trees for these numbers.

1. 48

4. 36

7. 39

9. 72

2. 44

5. 32

8. 38

10. 52

3. 64

6. 28

Least Common Multiple

EXAMPLE

Find the LCM (12, 6).

$$M_{12} = 12, 24, 36$$

$$M_6 = 6, 12, 18, 24$$

$$\text{LCM}(12, 6) = 12$$

Directions Find the least common multiple and show the steps.

- 1.**
- Find the LCM (10, 15).

- 6.**
- Find the LCM (36, 12).

- 2.**
- Find the LCM (12, 16).

- 7.**
- Find the LCM (7, 6).

- 3.**
- Find the LCM (3, 8).

- 8.**
- Find the LCM (5, 8).

- 4.**
- Find the LCM (8, 9).

- 9.**
- Find the LCM (4, 6).

- 5.**
- Find the LCM (3, 7).

- 10.**
- Find the LCM (5, 7).

Least Common Multiple/Greatest Common Factor

EXAMPLES

Find the factors. Underline greatest common numbers in both sets.

$$\text{LCM } (3, 5)$$

$$\text{GCF } (10, 25)$$

$$M_3 = \{0, 3, 9, 12, \underline{15}, \dots\}$$

$$F_{10} = \{1, 2, \underline{5}, 10\}$$

$$M_5 = \{0, 5, 10, \underline{15}, 20, \dots\}$$

$$F_{25} = \{1, \underline{5}, 25\}$$

$$\text{LCM } (3, 5) = 15$$

$$\text{GCF} = 5$$

Directions Find the least common multiple and show the steps.

1. Find the LCM (11, 33).

3. Find the LCM (15, 12).

2. Find the LCM (5, 16).

4. Find the LCM (12, 10).

Directions Find the greatest common factor.

5. GCF (18, 16) _____

11. GCF (12, 20) _____

6. GCF (8, 36) _____

12. GCF (32, 36) _____

7. GCF (12, 15) _____

13. GCF (12, 16) _____

8. GCF (6, 26) _____

14. GCF (20, 8) _____

9. GCF (18, 4) _____

15. GCF (20, 15) _____

10. GCF (14, 4) _____

Using Prime Factorization

EXAMPLES

LCM (10, 15)

$$\begin{array}{r}
 10 \\
 \swarrow \quad \searrow \\
 2 \quad \times \quad 5 \\
 \\
 10 = 2 \quad \times \quad 5 \\
 \\
 15 = \quad \quad 3 \quad \times \quad 5 \\
 \downarrow \quad \quad \downarrow \quad \times \quad \downarrow \\
 2 \quad \times \quad 3 \quad \times \quad 5 = 30
 \end{array}$$

GCF (10, 15)

$$\begin{array}{r}
 10 \\
 \swarrow \quad \searrow \\
 2 \quad \times \quad 5 \\
 \\
 10 = 2 \quad \times \quad 5 \\
 \\
 15 = \quad \quad 3 \quad \times \quad 5 \\
 \quad \quad \quad \quad \quad \downarrow \\
 \quad \quad \quad \quad \quad 5 \quad \text{GCF} = 5
 \end{array}$$

Directions Find the least common multiple (LCM) for these pairs of numbers.

1. Find the LCM (25, 15).
2. Find the LCM (5, 12).
3. Find the LCM (16, 18).
4. Find the LCM (27, 9).

Directions Find the greatest common factor (GCF) for each pair of numbers.

5. GCF (10, 25)
6. GCF (20, 30)
7. GCF (22, 77)
8. GCF (14, 8)
9. GCF (22, 55)
10. GCF (44, 48)

Comparing Fractions

EXAMPLE

Cross-multiply numerators and denominators. Compare the products.

$$\frac{2}{3} < \frac{4}{5}$$

$$3 \times 4 = 12$$

$$\frac{2}{3} < \frac{4}{5}$$

$$2 \times 5 = 10$$

$$\frac{10}{3} < \frac{12}{5}$$

$$10 < 12$$

Directions Compare the fractions in each pair. Use $<$ or $>$ for each pair.

- | | | | | | | | |
|---------------------|-----------------|--------------------|-----------------|---------------------|-----------------|---------------------|-----------------|
| 1. $\frac{3}{5}$ | $\frac{4}{7}$ | 16. $\frac{7}{13}$ | $\frac{6}{32}$ | 31. $\frac{9}{10}$ | $\frac{4}{5}$ | 46. $\frac{6}{10}$ | $\frac{2}{4}$ |
| 2. $\frac{5}{6}$ | $\frac{7}{8}$ | 17. $\frac{1}{5}$ | $\frac{1}{9}$ | 32. $\frac{7}{12}$ | $\frac{7}{10}$ | 47. $\frac{11}{23}$ | $\frac{22}{31}$ |
| 3. $\frac{5}{7}$ | $\frac{7}{8}$ | 18. $\frac{2}{21}$ | $\frac{3}{31}$ | 33. $\frac{6}{9}$ | $\frac{12}{17}$ | 48. $\frac{9}{15}$ | $\frac{18}{31}$ |
| 4. $\frac{2}{5}$ | $\frac{4}{1}$ | 19. $\frac{1}{3}$ | $\frac{2}{7}$ | 34. $\frac{4}{12}$ | $\frac{2}{7}$ | 49. $\frac{10}{11}$ | $\frac{20}{23}$ |
| 5. $\frac{3}{13}$ | $\frac{6}{20}$ | 20. $\frac{6}{7}$ | $\frac{8}{1}$ | 35. $\frac{3}{13}$ | $\frac{1}{6}$ | 50. $\frac{4}{8}$ | $\frac{5}{11}$ |
| 6. $\frac{3}{8}$ | $\frac{9}{20}$ | 21. $\frac{3}{5}$ | $\frac{1}{2}$ | 36. $\frac{8}{15}$ | $\frac{15}{16}$ | 51. $\frac{10}{23}$ | $\frac{15}{32}$ |
| 7. $\frac{6}{11}$ | $\frac{5}{9}$ | 22. $\frac{2}{8}$ | $\frac{4}{17}$ | 37. $\frac{3}{8}$ | $\frac{5}{13}$ | 52. $\frac{11}{13}$ | $\frac{5}{17}$ |
| 8. $\frac{5}{8}$ | $\frac{10}{17}$ | 23. $\frac{6}{10}$ | $\frac{1}{5}$ | 38. $\frac{10}{12}$ | $\frac{14}{16}$ | 53. $\frac{9}{10}$ | $\frac{13}{14}$ |
| 9. $\frac{1}{2}$ | $\frac{5}{11}$ | 24. $\frac{5}{10}$ | $\frac{10}{21}$ | 39. $\frac{2}{6}$ | $\frac{4}{14}$ | 54. $\frac{7}{11}$ | $\frac{8}{12}$ |
| 10. $\frac{2}{13}$ | $\frac{4}{15}$ | 25. $\frac{4}{7}$ | $\frac{5}{11}$ | 40. $\frac{1}{12}$ | $\frac{4}{24}$ | 55. $\frac{3}{7}$ | $\frac{5}{9}$ |
| 11. $\frac{15}{16}$ | $\frac{16}{17}$ | 26. $\frac{3}{5}$ | $\frac{6}{11}$ | 41. $\frac{6}{11}$ | $\frac{5}{13}$ | 56. $\frac{5}{6}$ | $\frac{16}{17}$ |
| 12. $\frac{2}{13}$ | $\frac{3}{14}$ | 27. $\frac{4}{5}$ | $\frac{2}{20}$ | 42. $\frac{2}{4}$ | $\frac{10}{22}$ | 57. $\frac{2}{11}$ | $\frac{2}{3}$ |
| 13. $\frac{1}{8}$ | $\frac{2}{13}$ | 28. $\frac{6}{11}$ | $\frac{5}{22}$ | 43. $\frac{8}{10}$ | $\frac{4}{40}$ | 58. $\frac{1}{8}$ | $\frac{5}{45}$ |
| 14. $\frac{5}{21}$ | $\frac{18}{31}$ | 29. $\frac{1}{2}$ | $\frac{2}{8}$ | 44. $\frac{6}{7}$ | $\frac{18}{20}$ | 59. $\frac{13}{20}$ | $\frac{1}{5}$ |
| 15. $\frac{2}{15}$ | $\frac{6}{21}$ | 30. $\frac{4}{11}$ | $\frac{8}{21}$ | 45. $\frac{4}{6}$ | $\frac{8}{10}$ | 60. $\frac{7}{10}$ | $\frac{6}{15}$ |

Working with Fractions

EXAMPLE

Divide to find out how many times one denominator goes into the other.
Multiply the numerator by the quotient.

$$\frac{2}{5} = \frac{\quad}{25} \quad \text{Divide 25 by 5. } 25 \div 5 = 5$$

$$\frac{2}{5} \times \frac{5}{5} = \frac{10}{25}$$

$$\frac{2}{5} = \frac{10}{25}$$

Directions Express these fractions in higher terms.

- | | | | |
|--|---|--|---|
| 1. $\frac{3}{5} = \frac{\quad}{50}$ | 16. $\frac{6}{7} = \frac{\quad}{42}$ | 31. $\frac{5}{14} = \frac{\quad}{56}$ | 46. $\frac{5}{8} = \frac{\quad}{96}$ |
| 2. $\frac{1}{3} = \frac{\quad}{18}$ | 17. $\frac{7}{13} = \frac{\quad}{39}$ | 32. $\frac{2}{23} = \frac{\quad}{92}$ | 47. $\frac{5}{21} = \frac{\quad}{105}$ |
| 3. $\frac{5}{6} = \frac{\quad}{24}$ | 18. $\frac{5}{8} = \frac{\quad}{64}$ | 33. $\frac{5}{7} = \frac{\quad}{210}$ | 48. $\frac{5}{32} = \frac{\quad}{160}$ |
| 4. $\frac{7}{8} = \frac{\quad}{32}$ | 19. $\frac{2}{13} = \frac{\quad}{52}$ | 34. $\frac{4}{13} = \frac{\quad}{39}$ | 49. $\frac{6}{38} = \frac{\quad}{380}$ |
| 5. $\frac{7}{8} = \frac{\quad}{56}$ | 20. $\frac{1}{9} = \frac{\quad}{99}$ | 35. $\frac{5}{10} = \frac{\quad}{1,000}$ | 50. $\frac{35}{70} = \frac{\quad}{280}$ |
| 6. $\frac{3}{7} = \frac{\quad}{21}$ | 21. $\frac{11}{12} = \frac{\quad}{60}$ | 36. $\frac{9}{17} = \frac{\quad}{51}$ | 51. $\frac{6}{30} = \frac{\quad}{390}$ |
| 7. $\frac{2}{9} = \frac{\quad}{36}$ | 22. $\frac{8}{15} = \frac{\quad}{45}$ | 37. $\frac{4}{11} = \frac{\quad}{99}$ | 52. $\frac{3}{13} = \frac{\quad}{65}$ |
| 8. $\frac{1}{5} = \frac{\quad}{30}$ | 23. $\frac{6}{19} = \frac{\quad}{76}$ | 38. $\frac{23}{30} = \frac{\quad}{90}$ | 53. $\frac{5}{11} = \frac{\quad}{121}$ |
| 9. $\frac{1}{4} = \frac{\quad}{20}$ | 24. $\frac{4}{7} = \frac{\quad}{63}$ | 39. $\frac{3}{7} = \frac{\quad}{84}$ | 54. $\frac{45}{60} = \frac{\quad}{480}$ |
| 10. $\frac{5}{11} = \frac{\quad}{121}$ | 25. $\frac{13}{15} = \frac{\quad}{105}$ | 40. $\frac{3}{16} = \frac{\quad}{80}$ | 55. $\frac{15}{18} = \frac{\quad}{72}$ |
| 11. $\frac{4}{9} = \frac{\quad}{72}$ | 26. $\frac{8}{17} = \frac{\quad}{34}$ | 41. $\frac{12}{15} = \frac{\quad}{60}$ | 56. $\frac{8}{52} = \frac{\quad}{156}$ |
| 12. $\frac{3}{11} = \frac{\quad}{44}$ | 27. $\frac{10}{19} = \frac{\quad}{38}$ | 42. $\frac{5}{6} = \frac{\quad}{54}$ | 57. $\frac{6}{16} = \frac{\quad}{80}$ |
| 13. $\frac{2}{3} = \frac{\quad}{18}$ | 28. $\frac{1}{13} = \frac{\quad}{65}$ | 43. $\frac{8}{14} = \frac{\quad}{42}$ | 58. $\frac{7}{12} = \frac{\quad}{156}$ |
| 14. $\frac{7}{10} = \frac{\quad}{80}$ | 29. $\frac{10}{11} = \frac{\quad}{55}$ | 44. $\frac{18}{23} = \frac{\quad}{92}$ | 59. $\frac{9}{29} = \frac{\quad}{145}$ |
| 15. $\frac{3}{4} = \frac{\quad}{16}$ | 30. $\frac{15}{16} = \frac{\quad}{64}$ | 45. $\frac{9}{22} = \frac{\quad}{220}$ | 60. $\frac{5}{21} = \frac{\quad}{126}$ |



Renaming Fractions

EXAMPLE

Rename fractions by expressing them in lowest terms.
Divide the numerator and denominator by their greatest common factor.

$$\frac{10}{14} = \frac{10 \div 2}{14 \div 2} = \frac{5}{7}$$

Directions Express these fractions and mixed numbers in their lowest terms.

- | | | | |
|---------------------------------|---------------------------------|---------------------------------|-------------------------------|
| 1. $\frac{9}{15} =$ _____ | 16. $\frac{150}{200} =$ _____ | 31. $11 \frac{62}{92} =$ _____ | 46. $\frac{18}{450} =$ _____ |
| 2. $\frac{9}{27} =$ _____ | 17. $20 \frac{18}{57} =$ _____ | 32. $18 \frac{35}{225} =$ _____ | 47. $\frac{210}{280} =$ _____ |
| 3. $\frac{18}{22} =$ _____ | 18. $\frac{46}{52} =$ _____ | 33. $\frac{28}{54} =$ _____ | 48. $\frac{64}{160} =$ _____ |
| 4. $13 \frac{10}{15} =$ _____ | 19. $\frac{28}{120} =$ _____ | 34. $\frac{20}{55} =$ _____ | 49. $\frac{30}{72} =$ _____ |
| 5. $2 \frac{12}{14} =$ _____ | 20. $\frac{102}{128} =$ _____ | 35. $\frac{36}{38} =$ _____ | 50. $\frac{450}{480} =$ _____ |
| 6. $\frac{10}{20} =$ _____ | 21. $\frac{178}{220} =$ _____ | 36. $\frac{42}{150} =$ _____ | 51. $\frac{22}{42} =$ _____ |
| 7. $\frac{13}{39} =$ _____ | 22. $8 \frac{23}{92} =$ _____ | 37. $\frac{20}{25} =$ _____ | 52. $\frac{140}{280} =$ _____ |
| 8. $\frac{28}{40} =$ _____ | 23. $51 \frac{66}{121} =$ _____ | 38. $\frac{11}{88} =$ _____ | 53. $\frac{150}{300} =$ _____ |
| 9. $\frac{10}{50} =$ _____ | 24. $9 \frac{15}{33} =$ _____ | 39. $\frac{33}{39} =$ _____ | 54. $\frac{84}{96} =$ _____ |
| 10. $6 \frac{5}{40} =$ _____ | 25. $\frac{44}{108} =$ _____ | 40. $\frac{88}{112} =$ _____ | 55. $\frac{50}{68} =$ _____ |
| 11. $13 \frac{70}{80} =$ _____ | 26. $9 \frac{31}{62} =$ _____ | 41. $\frac{38}{56} =$ _____ | 56. $\frac{78}{104} =$ _____ |
| 12. $27 \frac{52}{104} =$ _____ | 27. $6 \frac{7}{63} =$ _____ | 42. $\frac{15}{54} =$ _____ | 57. $\frac{41}{205} =$ _____ |
| 13. $\frac{30}{33} =$ _____ | 28. $\frac{16}{64} =$ _____ | 43. $\frac{56}{108} =$ _____ | 58. $\frac{69}{207} =$ _____ |
| 14. $9 \frac{24}{46} =$ _____ | 29. $\frac{88}{121} =$ _____ | 44. $\frac{38}{106} =$ _____ | 59. $\frac{42}{122} =$ _____ |
| 15. $\frac{9}{21} =$ _____ | 30. $\frac{58}{64} =$ _____ | 45. $\frac{25}{155} =$ _____ | 60. $\frac{55}{300} =$ _____ |

Mixed Numbers

EXAMPLERename $1\frac{2}{3}$ as an improper fraction $3 \times 1 = 3$ $3 + 2 = 5$ $1\frac{2}{3} = \frac{5}{3}$ Multiply the whole number by the denominator. Then, add the numerator.
Write the new numerator over the same denominator.**Directions** Rename these mixed numbers as improper fractions.

- | | | | |
|-----------------------------|------------------------------|------------------------------|------------------------------|
| 1. $2\frac{1}{6} =$ _____ | 16. $2\frac{2}{3} =$ _____ | 31. $3\frac{16}{17} =$ _____ | 46. $7\frac{20}{23} =$ _____ |
| 2. $1\frac{1}{2} =$ _____ | 17. $15\frac{1}{3} =$ _____ | 32. $4\frac{2}{19} =$ _____ | 47. $5\frac{5}{60} =$ _____ |
| 3. $2\frac{1}{5} =$ _____ | 18. $6\frac{4}{11} =$ _____ | 33. $5\frac{7}{9} =$ _____ | 48. $1\frac{2}{13} =$ _____ |
| 4. $1\frac{5}{6} =$ _____ | 19. $15\frac{3}{4} =$ _____ | 34. $5\frac{2}{12} =$ _____ | 49. $3\frac{5}{11} =$ _____ |
| 5. $4\frac{1}{5} =$ _____ | 20. $6\frac{2}{5} =$ _____ | 35. $6\frac{3}{13} =$ _____ | 50. $7\frac{2}{25} =$ _____ |
| 6. $3\frac{2}{5} =$ _____ | 21. $7\frac{1}{5} =$ _____ | 36. $4\frac{1}{13} =$ _____ | 51. $4\frac{3}{29} =$ _____ |
| 7. $1\frac{1}{6} =$ _____ | 22. $33\frac{2}{3} =$ _____ | 37. $7\frac{10}{11} =$ _____ | 52. $4\frac{2}{32} =$ _____ |
| 8. $9\frac{2}{7} =$ _____ | 23. $17\frac{1}{2} =$ _____ | 38. $8\frac{13}{15} =$ _____ | 53. $1\frac{7}{18} =$ _____ |
| 9. $4\frac{3}{4} =$ _____ | 24. $2\frac{2}{17} =$ _____ | 39. $1\frac{7}{22} =$ _____ | 54. $11\frac{5}{11} =$ _____ |
| 10. $2\frac{5}{11} =$ _____ | 25. $9\frac{5}{11} =$ _____ | 40. $3\frac{5}{11} =$ _____ | 55. $20\frac{1}{16} =$ _____ |
| 11. $1\frac{5}{9} =$ _____ | 26. $8\frac{5}{13} =$ _____ | 41. $4\frac{5}{20} =$ _____ | 56. $10\frac{2}{17} =$ _____ |
| 12. $13\frac{2}{7} =$ _____ | 27. $18\frac{3}{5} =$ _____ | 42. $2\frac{3}{22} =$ _____ | 57. $11\frac{5}{21} =$ _____ |
| 13. $20\frac{1}{2} =$ _____ | 28. $3\frac{2}{19} =$ _____ | 43. $5\frac{11}{16} =$ _____ | 58. $5\frac{11}{12} =$ _____ |
| 14. $6\frac{2}{9} =$ _____ | 29. $9\frac{10}{11} =$ _____ | 44. $21\frac{2}{61} =$ _____ | 59. $7\frac{2}{30} =$ _____ |
| 15. $3\frac{4}{7} =$ _____ | 30. $2\frac{13}{14} =$ _____ | 45. $5\frac{13}{20} =$ _____ | 60. $2\frac{6}{23} =$ _____ |

Renaming Improper Fractions

EXAMPLE

Express the improper fractions as mixed numbers.
Divide the numerator by the denominator.
Simplify if necessary.

$$\frac{78}{9}$$

$$\begin{array}{r} 8 \\ 9 \overline{)78} \\ \underline{-72} \\ 6 \end{array}$$

remainder is 6

Solution: $8\frac{6}{9}$ or $8\frac{2}{3}$

Directions Rename the improper fractions as mixed numbers.
Simplify if necessary.

1. $\frac{15}{7} =$ _____ 9. $\frac{57}{8} =$ _____ 17. $\frac{18}{11} =$ _____ 25. $\frac{53}{10} =$ _____

2. $\frac{29}{6} =$ _____ 10. $\frac{53}{23} =$ _____ 18. $\frac{72}{18} =$ _____ 26. $\frac{34}{12} =$ _____

3. $\frac{51}{30} =$ _____ 11. $\frac{77}{10} =$ _____ 19. $\frac{71}{14} =$ _____ 27. $\frac{63}{8} =$ _____

4. $\frac{33}{8} =$ _____ 12. $\frac{42}{13} =$ _____ 20. $\frac{57}{13} =$ _____ 28. $\frac{64}{9} =$ _____

5. $\frac{44}{10} =$ _____ 13. $\frac{62}{11} =$ _____ 21. $\frac{19}{10} =$ _____ 29. $\frac{29}{18} =$ _____

6. $\frac{20}{10} =$ _____ 14. $\frac{82}{11} =$ _____ 22. $\frac{54}{20} =$ _____ 30. $\frac{98}{9} =$ _____

7. $\frac{35}{2} =$ _____ 15. $\frac{39}{11} =$ _____ 23. $\frac{46}{20} =$ _____

8. $\frac{28}{8} =$ _____ 16. $\frac{87}{33} =$ _____ 24. $\frac{66}{11} =$ _____

Improper Fractions to Mixed Numbers

EXAMPLE

Rename $\frac{13}{5}$. Divide the numerator by the denominator.
Simplify if necessary.

$$\begin{array}{r} 2\frac{3}{5} \\ 5 \overline{)13} \\ \underline{-10} \\ 3 \end{array}$$

Directions Rename these improper fractions as mixed numbers.
Simplify if necessary.

- | | | | |
|-----------------------------|-------------------------------|-----------------------------|------------------------------|
| 1. $\frac{14}{6} =$ _____ | 16. $\frac{72}{19} =$ _____ | 31. $\frac{38}{6} =$ _____ | 46. $\frac{91}{8} =$ _____ |
| 2. $\frac{16}{7} =$ _____ | 17. $\frac{60}{9} =$ _____ | 32. $\frac{17}{5} =$ _____ | 47. $\frac{76}{7} =$ _____ |
| 3. $\frac{28}{7} =$ _____ | 18. $\frac{120}{11} =$ _____ | 33. $\frac{18}{11} =$ _____ | 48. $\frac{89}{11} =$ _____ |
| 4. $\frac{15}{2} =$ _____ | 19. $\frac{36}{17} =$ _____ | 34. $\frac{23}{2} =$ _____ | 49. $\frac{48}{23} =$ _____ |
| 5. $\frac{33}{4} =$ _____ | 20. $\frac{57}{9} =$ _____ | 35. $\frac{54}{11} =$ _____ | 50. $\frac{98}{46} =$ _____ |
| 6. $\frac{18}{5} =$ _____ | 21. $\frac{39}{16} =$ _____ | 36. $\frac{92}{5} =$ _____ | 51. $\frac{88}{23} =$ _____ |
| 7. $\frac{25}{4} =$ _____ | 22. $\frac{37}{5} =$ _____ | 37. $\frac{36}{13} =$ _____ | 52. $\frac{105}{15} =$ _____ |
| 8. $\frac{62}{6} =$ _____ | 23. $\frac{17}{2} =$ _____ | 38. $\frac{39}{5} =$ _____ | 53. $\frac{28}{6} =$ _____ |
| 9. $\frac{30}{7} =$ _____ | 24. $\frac{60}{28} =$ _____ | 39. $\frac{51}{11} =$ _____ | 54. $\frac{100}{7} =$ _____ |
| 10. $\frac{35}{8} =$ _____ | 25. $\frac{33}{10} =$ _____ | 40. $\frac{46}{14} =$ _____ | 55. $\frac{49}{3} =$ _____ |
| 11. $\frac{18}{8} =$ _____ | 26. $\frac{135}{9} =$ _____ | 41. $\frac{22}{5} =$ _____ | 56. $\frac{65}{2} =$ _____ |
| 12. $\frac{30}{4} =$ _____ | 27. $\frac{200}{120} =$ _____ | 42. $\frac{87}{12} =$ _____ | 57. $\frac{85}{17} =$ _____ |
| 13. $\frac{75}{25} =$ _____ | 28. $\frac{25}{21} =$ _____ | 43. $\frac{57}{12} =$ _____ | 58. $\frac{59}{9} =$ _____ |
| 14. $\frac{72}{10} =$ _____ | 29. $\frac{63}{12} =$ _____ | 44. $\frac{62}{11} =$ _____ | 59. $\frac{99}{10} =$ _____ |
| 15. $\frac{26}{3} =$ _____ | 30. $\frac{130}{12} =$ _____ | 45. $\frac{73}{10} =$ _____ | 60. $\frac{46}{3} =$ _____ |

Multiplication of Fractions

EXAMPLE

Multiply numerators. Multiply denominators.
Simplify if necessary.

$$\frac{3}{5} \times \frac{7}{8} = \frac{3 \times 7}{5 \times 8} = \frac{21}{40}$$

Directions Multiply these fractions. Simplify the answers to the lowest terms.

- | | | |
|---|--|---|
| 1. $\frac{1}{5} \times \frac{3}{4} =$ _____ | 16. $\frac{35}{38} \times \frac{4}{5} =$ _____ | 31. $2\frac{1}{20} \times 20\frac{5}{10} =$ _____ |
| 2. $\frac{4}{5} \times \frac{10}{11} =$ _____ | 17. $\frac{6}{11} \times 2\frac{5}{6} =$ _____ | 32. $5\frac{6}{13} \times 1\frac{1}{2} =$ _____ |
| 3. $\frac{6}{9} \times \frac{1}{3} =$ _____ | 18. $\frac{7}{12} \times \frac{3}{7} =$ _____ | 33. $7\frac{1}{5} \times \frac{65}{72} =$ _____ |
| 4. $\frac{2}{5} \times \frac{4}{10} =$ _____ | 19. $\frac{1}{6} \times \frac{2}{5} =$ _____ | 34. $5\frac{2}{7} \times 1\frac{1}{2} =$ _____ |
| 5. $8 \times \frac{6}{7} =$ _____ | 20. $\frac{2}{5} \times 2\frac{2}{5} =$ _____ | 35. $7\frac{5}{8} \times 2\frac{3}{4} =$ _____ |
| 6. $\frac{7}{9} \times 1\frac{1}{2} =$ _____ | 21. $1\frac{3}{7} \times \frac{5}{8} =$ _____ | 36. $5\frac{2}{12} \times 1\frac{1}{2} =$ _____ |
| 7. $\frac{2}{9} \times 1\frac{1}{8} =$ _____ | 22. $\frac{6}{13} \times 2\frac{1}{6} =$ _____ | 37. $5\frac{4}{11} \times 1\frac{1}{3} =$ _____ |
| 8. $\frac{3}{11} \times 3\frac{2}{3} =$ _____ | 23. $3\frac{1}{5} \times \frac{3}{11} =$ _____ | 38. $3\frac{4}{5} \times 1\frac{1}{2} =$ _____ |
| 9. $\frac{7}{13} \times \frac{13}{5} =$ _____ | 24. $4\frac{1}{5} \times 7 =$ _____ | 39. $8\frac{8}{9} \times \frac{18}{20} =$ _____ |
| 10. $\frac{8}{11} \times \frac{1}{5} =$ _____ | 25. $5\frac{2}{5} \times 10 =$ _____ | 40. $3\frac{1}{5} \times 5\frac{1}{3} =$ _____ |
| 11. $\frac{2}{5} \times \frac{2}{17} =$ _____ | 26. $5\frac{2}{13} \times \frac{1}{6} =$ _____ | 41. $3\frac{1}{3} \times \frac{1}{5} =$ _____ |
| 12. $\frac{5}{8} \times \frac{3}{8} =$ _____ | 27. $3\frac{4}{5} \times 65 =$ _____ | 42. $2\frac{3}{7} \times \frac{14}{17} =$ _____ |
| 13. $\frac{4}{6} \times \frac{2}{3} =$ _____ | 28. $2\frac{1}{4} \times 4 =$ _____ | 43. $3\frac{5}{6} \times \frac{12}{46} =$ _____ |
| 14. $\frac{1}{3} \times \frac{6}{10} =$ _____ | 29. $2\frac{1}{5} \times 5\frac{1}{2} =$ _____ | 44. $5\frac{2}{7} \times 5 =$ _____ |
| 15. $\frac{1}{2} \times \frac{3}{5} =$ _____ | 30. $7\frac{2}{5} \times 5\frac{2}{7} =$ _____ | 45. $7\frac{2}{5} \times 1\frac{1}{5} =$ _____ |

Multiplying Mixed Numbers

EXAMPLE

Change mixed numbers to improper fractions.
Multiply. Simplify if necessary.

$$2\frac{1}{5} \times \frac{1}{5} =$$

$$\frac{11}{5} \times \frac{1}{5} = \frac{11}{25}$$

Directions Multiply these fractions.

1. $4\frac{2}{5} \times 1\frac{3}{5} =$

6. $1\frac{1}{13} \times 2\frac{3}{7} =$

11. $\frac{1}{5} \times 2\frac{1}{3} =$

2. $1\frac{1}{6} \times 1\frac{2}{7} =$

7. $2\frac{1}{4} \times 2\frac{1}{3} =$

12. $2\frac{5}{6} \times 1\frac{5}{7} =$

3. $3\frac{1}{3} \times 1\frac{3}{5} =$

8. $1\frac{1}{3} \times 3\frac{1}{2} =$

13. $2\frac{1}{3} \times 3\frac{1}{5} =$

4. $\frac{3}{7} \times 1\frac{1}{5} =$

9. $2\frac{2}{3} \times \frac{1}{6} =$

14. $2\frac{2}{3} \times 3\frac{1}{3} =$

5. $\frac{1}{7} \times 2\frac{1}{4} =$

10. $1\frac{1}{3} \times 2\frac{2}{5} =$

15. $\frac{3}{5} \times 3\frac{1}{3} =$

Dividing Fractions

EXAMPLE

Invert the divisor. Multiply. Simplify if necessary.

$$\frac{2}{5} \div \frac{3}{7} =$$

$$\frac{2}{5} \times \frac{7}{3} = \frac{14}{15}$$

Directions Divide these fractions. Remember to invert the divisor.
Show your work. See the example.

1. $\frac{3}{10} \div \frac{4}{5} =$

8. $\frac{7}{10} \div \frac{10}{15} =$

15. $\frac{4}{5} \div \frac{16}{20} =$

2. $\frac{13}{12} \div \frac{15}{18} =$

9. $\frac{2}{7} \div \frac{7}{8} =$

16. $\frac{1}{6} \div \frac{5}{12} =$

3. $\frac{5}{9} \div \frac{8}{12} =$

10. $\frac{1}{7} \div \frac{3}{14} =$

17. $\frac{1}{5} \div \frac{3}{5} =$

4. $\frac{7}{5} \div \frac{10}{15} =$

11. $\frac{9}{14} \div \frac{18}{21} =$

18. $\frac{14}{15} \div \frac{14}{15} =$

5. $\frac{4}{12} \div \frac{6}{8} =$

12. $\frac{12}{14} \div \frac{6}{7} =$

19. $\frac{3}{7} \div \frac{9}{10} =$

6. $\frac{8}{9} \div \frac{6}{7} =$

13. $\frac{8}{9} \div \frac{6}{9} =$

20. $\frac{14}{16} \div \frac{15}{20} =$

7. $\frac{5}{12} \div \frac{7}{8} =$

14. $\frac{6}{7} \div \frac{2}{9} =$



Division of Fractions

EXAMPLE

Invert the divisor. Multiply and simplify if necessary.

$$\begin{aligned} \frac{3}{5} \div \frac{2}{5} &= \frac{3}{5} \times \frac{5}{2} \\ &= \frac{\cancel{3}^1 \times \cancel{5}_1}{1 \times 2} \\ &= \frac{3 \times 1}{1 \times 2} \\ &= \frac{3}{2} = 1 \frac{1}{2} \end{aligned}$$

Directions Divide these fractions. Simplify the answers to the lowest terms.

- | | | |
|--|---|---|
| 1. $\frac{3}{7} \div \frac{1}{7} =$ _____ | 15. $\frac{2}{5} \div \frac{1}{8} =$ _____ | 29. $2 \frac{1}{6} \div 1 \frac{1}{2} =$ _____ |
| 2. $\frac{6}{7} \div \frac{2}{9} =$ _____ | 16. $5 \frac{2}{8} \div \frac{1}{8} =$ _____ | 30. $3 \frac{5}{13} \div \frac{22}{39} =$ _____ |
| 3. $\frac{5}{13} \div \frac{25}{26} =$ _____ | 17. $\frac{12}{17} \div \frac{15}{21} =$ _____ | 31. $5 \div 1 \frac{1}{6} =$ _____ |
| 4. $\frac{15}{16} \div \frac{3}{8} =$ _____ | 18. $\frac{1}{3} \div 2 \frac{1}{2} =$ _____ | 32. $11 \div 3 \frac{4}{33} =$ _____ |
| 5. $\frac{6}{13} \div \frac{2}{13} =$ _____ | 19. $2 \frac{3}{4} \div \frac{11}{16} =$ _____ | 33. $4 \frac{3}{11} \div 6 =$ _____ |
| 6. $\frac{3}{10} \div 1 \frac{4}{5} =$ _____ | 20. $5 \frac{3}{5} \div 2 \frac{1}{10} =$ _____ | 34. $4 \frac{1}{2} \div \frac{36}{38} =$ _____ |
| 7. $\frac{6}{11} \div 2 \frac{1}{5} =$ _____ | 21. $2 \frac{1}{5} \div \frac{1}{5} =$ _____ | 35. $3 \frac{2}{7} \div 1 \frac{1}{2} =$ _____ |
| 8. $\frac{4}{5} \div \frac{24}{25} =$ _____ | 22. $3 \frac{2}{7} \div \frac{46}{21} =$ _____ | 36. $2 \frac{5}{6} \div 17 =$ _____ |
| 9. $\frac{5}{7} \div \frac{14}{15} =$ _____ | 23. $1 \frac{2}{5} \div 2 \frac{2}{3} =$ _____ | 37. $1 \frac{5}{9} \div 1 \frac{2}{5} =$ _____ |
| 10. $\frac{1}{2} \div \frac{1}{3} =$ _____ | 24. $1 \frac{2}{8} \div 2 \frac{1}{2} =$ _____ | 38. $2 \frac{3}{5} \div \frac{1}{5} =$ _____ |
| 11. $\frac{5}{2} \div 1 \frac{1}{2} =$ _____ | 25. $\frac{5}{16} \div 1 \frac{1}{2} =$ _____ | 39. $5 \frac{3}{8} \div 1 \frac{1}{16} =$ _____ |
| 12. $\frac{4}{3} \div 2 \frac{1}{5} =$ _____ | 26. $7 \frac{1}{2} \div 22 \frac{1}{2} =$ _____ | 40. $1 \frac{3}{11} \div 5 =$ _____ |
| 13. $\frac{1}{5} \div \frac{3}{4} =$ _____ | 27. $5 \frac{2}{3} \div 1 \frac{5}{12} =$ _____ | |
| 14. $\frac{9}{10} \div \frac{2}{5} =$ _____ | 28. $\frac{3}{7} \div 1 \frac{3}{11} =$ _____ | |

Addition of Fractions with Like Denominators

EXAMPLE

Add numerators. Keep the denominator.

$$\begin{array}{r} \frac{5}{12} \\ + \frac{6}{12} \\ \hline \frac{11}{12} \end{array}$$

Directions Add these fractions. Simplify the answers.

1.
$$\begin{array}{r} \frac{2}{7} \\ + \frac{4}{7} \\ \hline \end{array}$$

6.
$$\begin{array}{r} 5\frac{2}{3} \\ + 2\frac{1}{3} \\ \hline \end{array}$$

11.
$$\begin{array}{r} 6\frac{7}{10} \\ + \frac{9}{10} \\ \hline \end{array}$$

16.
$$\begin{array}{r} 4\frac{6}{23} \\ + 5\frac{17}{23} \\ \hline \end{array}$$

2.
$$\begin{array}{r} \frac{3}{16} \\ + \frac{2}{16} \\ \hline \end{array}$$

7.
$$\begin{array}{r} \frac{2}{9} \\ + \frac{3}{9} \\ \hline \end{array}$$

12.
$$\begin{array}{r} 12\frac{7}{11} \\ + 3\frac{2}{11} \\ \hline \end{array}$$

17.
$$\begin{array}{r} 5\frac{5}{26} \\ + \frac{24}{26} \\ \hline \end{array}$$

3.
$$\begin{array}{r} \frac{5}{15} \\ + \frac{3}{15} \\ \hline \end{array}$$

8.
$$\begin{array}{r} \frac{2}{17} \\ + \frac{5}{17} \\ \hline \end{array}$$

13.
$$\begin{array}{r} \frac{5}{13} \\ + \frac{8}{13} \\ \hline \end{array}$$

18.
$$\begin{array}{r} 35\frac{5}{6} \\ + 5 \\ \hline \end{array}$$

4.
$$\begin{array}{r} \frac{7}{21} \\ + \frac{7}{21} \\ \hline \end{array}$$

9.
$$\begin{array}{r} \frac{3}{20} \\ + \frac{2}{20} \\ \hline \end{array}$$

14.
$$\begin{array}{r} \frac{7}{18} \\ + \frac{2}{18} \\ \hline \end{array}$$

19.
$$\begin{array}{r} 4 \\ + 6\frac{2}{5} \\ \hline \end{array}$$

5.
$$\begin{array}{r} \frac{8}{9} \\ + \frac{5}{9} \\ \hline \end{array}$$

10.
$$\begin{array}{r} 2\frac{2}{18} \\ + 3\frac{3}{18} \\ \hline \end{array}$$

15.
$$\begin{array}{r} \frac{6}{20} \\ + \frac{5}{20} \\ \hline \end{array}$$

20.
$$\begin{array}{r} 7\frac{2}{13} \\ + \frac{11}{13} \\ \hline \end{array}$$

Addition of Fractions with Unlike Denominators

EXAMPLE

To add fractions and mixed numbers with unlike denominators, find the least common multiple of the denominators. Raise the fraction to higher terms and add.

$$\begin{array}{r} \frac{5}{6} = \frac{15}{18} \\ + \frac{2}{18} = + \frac{2}{18} \\ \hline = \frac{17}{18} \end{array}$$

Directions Add these fractions. Simplify the answers.

$$\begin{array}{r} \mathbf{1.} \quad \frac{4}{9} \\ + \frac{1}{3} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{6.} \quad \frac{5}{9} \\ + \frac{4}{18} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{11.} \quad \frac{6}{25} \\ + \frac{4}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{16.} \quad \frac{12}{35} \\ + 7\frac{7}{210} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{2.} \quad \frac{7}{18} \\ + \frac{1}{3} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{7.} \quad \frac{4}{21} \\ + \frac{1}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{12.} \quad \frac{8}{35} \\ + \frac{2}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{17.} \quad 18\frac{1}{6} \\ + 3\frac{1}{72} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{3.} \quad 5\frac{3}{7} \\ + 2\frac{1}{14} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{8.} \quad 6\frac{3}{20} \\ + 4\frac{2}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{13.} \quad 8\frac{3}{20} \\ + \frac{3}{4} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{18.} \quad 8\frac{3}{21} \\ + 2\frac{1}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{4.} \quad 10\frac{2}{7} \\ + 3\frac{5}{34} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{9.} \quad 23\frac{1}{7} \\ + 2\frac{5}{14} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{14.} \quad 37\frac{4}{8} \\ + 5\frac{7}{24} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{19.} \quad 8\frac{1}{5} \\ + 10\frac{1}{55} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{5.} \quad 25\frac{6}{35} \\ + 4\frac{3}{70} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{10.} \quad 38\frac{1}{12} \\ + 2\frac{4}{60} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{15.} \quad 3\frac{3}{5} \\ + 2\frac{1}{20} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{20.} \quad 12\frac{5}{28} \\ + 4\frac{5}{56} \\ \hline \end{array}$$

More Addition of Fractions

EXAMPLE

To add fractions and mixed numbers with unlike denominators, find the least common multiple of the denominators. Raise the fraction to higher terms and add.

$$\begin{array}{r} \frac{5}{9} = \frac{35}{63} \\ + \frac{3}{7} = + \frac{27}{63} \\ \hline = \frac{62}{63} \end{array}$$

Directions Add these fractions. Simplify the answers.

$$\begin{array}{r} \mathbf{1.} \quad \frac{11}{20} \\ + \frac{4}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{6.} \quad \frac{3}{13} \\ + \frac{1}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{11.} \quad \frac{6}{22} \\ + \frac{4}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{16.} \quad 3\frac{4}{7} \\ + 7\frac{3}{8} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{2.} \quad \frac{5}{11} \\ + \frac{4}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{7.} \quad \frac{3}{7} \\ + \frac{9}{9} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{12.} \quad \frac{7}{11} \\ + \frac{10}{12} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{17.} \quad 28\frac{5}{7} \\ + 6\frac{4}{9} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{3.} \quad 2\frac{5}{7} \\ + 5\frac{6}{8} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{8.} \quad \frac{5}{12} \\ + 6\frac{4}{10} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{13.} \quad 2\frac{7}{13} \\ + 9\frac{3}{10} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{18.} \quad 4\frac{1}{12} \\ + 6\frac{2}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{4.} \quad 5\frac{4}{9} \\ + 3\frac{2}{11} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{9.} \quad 6\frac{3}{13} \\ + 4\frac{5}{6} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{14.} \quad 3\frac{5}{7} \\ + 2\frac{9}{11} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{19.} \quad 35\frac{4}{19} \\ + 2\frac{3}{10} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{5.} \quad 16\frac{5}{12} \\ + 4\frac{3}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{10.} \quad 9\frac{5}{11} \\ + 6\frac{2}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{15.} \quad 4\frac{7}{13} \\ + 2\frac{3}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{20.} \quad 12\frac{8}{15} \\ + \frac{1}{4} \\ \hline \end{array}$$

Addition of Mixed Numbers

EXAMPLE

Add the fractions. Find the lowest common multiple if necessary.
Add the whole numbers. Simplify to lowest terms.

$$\begin{array}{r} 3\frac{2}{13} \\ + 4\frac{1}{13} \\ \hline 7\frac{3}{13} \end{array}$$

Directions Add these fractions. Simplify the answers to the lowest terms.

$$\begin{array}{r} \mathbf{1.} \quad 2\frac{3}{10} \\ + 3\frac{1}{10} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{6.} \quad 4\frac{2}{5} \\ + 3\frac{1}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{11.} \quad 6\frac{5}{21} \\ + 2\frac{1}{7} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{2.} \quad 18\frac{5}{16} \\ + 3\frac{1}{8} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{7.} \quad 7\frac{1}{4} \\ + \frac{1}{3} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{12.} \quad 13\frac{5}{16} \\ + 2\frac{1}{4} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{3.} \quad 81\frac{2}{15} \\ + 2\frac{2}{3} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{8.} \quad 17 \\ + 2\frac{1}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{13.} \quad 10\frac{3}{7} \\ + 2\frac{4}{5} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{4.} \quad 18\frac{2}{11} \\ + 4\frac{5}{6} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{9.} \quad 29\frac{2}{5} \\ + 3\frac{5}{6} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{14.} \quad 13\frac{3}{22} \\ + 5\frac{3}{44} \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{5.} \quad 23\frac{4}{7} \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} \mathbf{10.} \quad 16\frac{3}{13} \\ + \frac{4}{39} \\ \hline \end{array}$$

Directions Rewrite the fractions in the standard form and add.
Simplify the answers to the lowest terms.

$$\mathbf{15.} \quad 1\frac{1}{2} + 2\frac{3}{11} = \underline{\hspace{2cm}} \quad \mathbf{17.} \quad 7\frac{1}{7} + 5\frac{1}{8} = \underline{\hspace{2cm}} \quad \mathbf{19.} \quad 10 + 2\frac{1}{6} = \underline{\hspace{2cm}}$$

$$\mathbf{16.} \quad 2\frac{3}{5} + 4\frac{1}{6} = \underline{\hspace{2cm}} \quad \mathbf{18.} \quad 6\frac{2}{9} + 1\frac{3}{10} = \underline{\hspace{2cm}} \quad \mathbf{20.} \quad 5\frac{2}{12} + \frac{1}{10} = \underline{\hspace{2cm}}$$

Subtraction of Fractions with Like Denominators

EXAMPLE

Subtract numerators. Keep denominators.
Simplify if necessary.

$$\begin{array}{r} \frac{7}{8} \\ - \frac{3}{8} \\ \hline \frac{4}{8} = \frac{1}{2} \end{array}$$

Directions Subtract these fractions and simplify your answers.

$$\begin{array}{r} 1. \quad \frac{18}{35} \\ - \quad \frac{9}{35} \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad \frac{13}{16} \\ - \quad \frac{5}{16} \\ \hline \end{array}$$

$$\begin{array}{r} 11. \quad \frac{10}{21} \\ - \quad \frac{7}{21} \\ \hline \end{array}$$

$$\begin{array}{r} 16. \quad 13\frac{4}{29} \\ - \quad 3\frac{2}{29} \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 3\frac{7}{12} \\ - \quad 2\frac{2}{12} \\ \hline \end{array}$$

$$\begin{array}{r} 7. \quad 5\frac{15}{18} \\ - \quad 2\frac{3}{18} \\ \hline \end{array}$$

$$\begin{array}{r} 12. \quad 11\frac{4}{10} \\ - \quad \frac{1}{10} \\ \hline \end{array}$$

$$\begin{array}{r} 17. \quad 8\frac{33}{56} \\ - \quad 2\frac{5}{56} \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 8\frac{13}{15} \\ - \quad 3\frac{4}{15} \\ \hline \end{array}$$

$$\begin{array}{r} 8. \quad 11\frac{12}{41} \\ - \quad 5\frac{6}{41} \\ \hline \end{array}$$

$$\begin{array}{r} 13. \quad 30\frac{18}{33} \\ - \quad 5\frac{7}{33} \\ \hline \end{array}$$

$$\begin{array}{r} 18. \quad 33\frac{37}{45} \\ - \quad \frac{2}{45} \\ \hline \end{array}$$

$$\begin{array}{r} 4. \quad 16\frac{11}{20} \\ - \quad \frac{6}{20} \\ \hline \end{array}$$

$$\begin{array}{r} 9. \quad 8\frac{5}{28} \\ - \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} 14. \quad 31\frac{14}{27} \\ - \quad 4\frac{5}{27} \\ \hline \end{array}$$

$$\begin{array}{r} 19. \quad 13\frac{17}{38} \\ - \quad \frac{7}{38} \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 7\frac{2}{33} \\ - \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} 10. \quad 13\frac{17}{18} \\ - \quad 4\frac{8}{18} \\ \hline \end{array}$$

$$\begin{array}{r} 15. \quad 15\frac{3}{16} \\ - \quad 4\frac{1}{16} \\ \hline \end{array}$$

$$\begin{array}{r} 20. \quad 25\frac{7}{33} \\ - \quad 4\frac{4}{33} \\ \hline \end{array}$$

Subtraction of Fractions Without Renaming

EXAMPLE

Raise fractions to higher terms. Subtract numerators and whole numbers. Simplify if necessary.

$$\begin{array}{r} 15 \frac{2}{3} = 15 \frac{14}{21} \\ - 6 \frac{2}{7} = - 6 \frac{6}{21} \\ \hline = 9 \frac{8}{21} \end{array}$$

Directions Subtract these fractions. Simplify the answers to the lowest terms.

$$\begin{array}{r} 1. \quad 25 \frac{1}{8} \\ - 24 \frac{1}{9} \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad 22 \frac{7}{8} \\ - 3 \frac{1}{24} \\ \hline \end{array}$$

$$\begin{array}{r} 11. \quad 25 \frac{12}{38} \\ - 9 \frac{3}{19} \\ \hline \end{array}$$

$$\begin{array}{r} 16. \quad 8 \frac{1}{2} \\ - 5 \frac{3}{9} \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 28 \frac{12}{15} \\ - 4 \frac{2}{5} \\ \hline \end{array}$$

$$\begin{array}{r} 7. \quad 26 \frac{4}{9} \\ - 4 \frac{1}{8} \\ \hline \end{array}$$

$$\begin{array}{r} 12. \quad 33 \frac{4}{7} \\ - 6 \frac{1}{7} \\ \hline \end{array}$$

$$\begin{array}{r} 17. \quad 42 \frac{6}{7} \\ - 5 \frac{1}{6} \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 52 \frac{3}{10} \\ - 2 \frac{5}{17} \\ \hline \end{array}$$

$$\begin{array}{r} 8. \quad 14 \frac{5}{11} \\ - 7 \frac{2}{7} \\ \hline \end{array}$$

$$\begin{array}{r} 13. \quad 4 \frac{11}{16} \\ - 2 \frac{3}{32} \\ \hline \end{array}$$

$$\begin{array}{r} 18. \quad 2 \frac{1}{3} \\ - 1 \frac{2}{15} \\ \hline \end{array}$$

$$\begin{array}{r} 4. \quad 3 \frac{15}{21} \\ - 1 \frac{1}{5} \\ \hline \end{array}$$

$$\begin{array}{r} 9. \quad 7 \frac{2}{18} \\ - 5 \frac{1}{20} \\ \hline \end{array}$$

$$\begin{array}{r} 14. \quad 16 \frac{7}{28} \\ - 5 \frac{3}{28} \\ \hline \end{array}$$

$$\begin{array}{r} 19. \quad 5 \frac{1}{13} \\ - 2 \frac{1}{15} \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 51 \frac{5}{9} \\ - 4 \frac{4}{10} \\ \hline \end{array}$$

$$\begin{array}{r} 10. \quad 28 \frac{4}{21} \\ - 4 \frac{1}{7} \\ \hline \end{array}$$

$$\begin{array}{r} 15. \quad 16 \frac{3}{10} \\ - 2 \frac{1}{5} \\ \hline \end{array}$$

$$\begin{array}{r} 20. \quad 14 \frac{2}{15} \\ - \frac{1}{16} \\ \hline \end{array}$$

Subtraction of Fractions with Renaming

EXAMPLE

Rename the fractions and subtract them. Subtract the whole numbers. Simplify if necessary.

$$\begin{array}{r} 19\frac{1}{5} = 18\frac{6}{5} \\ - 2\frac{3}{5} = - 2\frac{3}{5} \\ \hline 16\frac{3}{5} \end{array}$$

Directions Subtract these fractions. Simplify the answers to the lowest terms.

$$\begin{array}{r} 1. \quad 13\frac{1}{8} \\ - 1\frac{7}{8} \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad 28\frac{2}{7} \\ - 5\frac{5}{7} \\ \hline \end{array}$$

$$\begin{array}{r} 11. \quad 12\frac{2}{17} \\ - 3\frac{5}{17} \\ \hline \end{array}$$

$$\begin{array}{r} 16. \quad 7 \\ - 5\frac{11}{12} \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 28\frac{1}{3} \\ - 5\frac{2}{3} \\ \hline \end{array}$$

$$\begin{array}{r} 7. \quad 4\frac{3}{9} \\ - \frac{5}{9} \\ \hline \end{array}$$

$$\begin{array}{r} 12. \quad 6 \\ - \frac{3}{12} \\ \hline \end{array}$$

$$\begin{array}{r} 17. \quad 67 \\ - 5\frac{17}{18} \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 13\frac{2}{19} \\ - 2\frac{5}{19} \\ \hline \end{array}$$

$$\begin{array}{r} 8. \quad 6\frac{4}{11} \\ - 1\frac{6}{11} \\ \hline \end{array}$$

$$\begin{array}{r} 13. \quad 8\frac{3}{21} \\ - 5\frac{7}{21} \\ \hline \end{array}$$

$$\begin{array}{r} 18. \quad 8\frac{7}{20} \\ - 5\frac{11}{20} \\ \hline \end{array}$$

$$\begin{array}{r} 4. \quad 14\frac{2}{17} \\ - 5\frac{3}{17} \\ \hline \end{array}$$

$$\begin{array}{r} 9. \quad 29\frac{5}{17} \\ - 28\frac{9}{17} \\ \hline \end{array}$$

$$\begin{array}{r} 14. \quad 32\frac{13}{35} \\ - 5\frac{15}{35} \\ \hline \end{array}$$

$$\begin{array}{r} 19. \quad 5 \\ - 2\frac{17}{20} \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 26\frac{5}{28} \\ - 4\frac{6}{28} \\ \hline \end{array}$$

$$\begin{array}{r} 10. \quad 42\frac{16}{50} \\ - 2\frac{25}{50} \\ \hline \end{array}$$

$$\begin{array}{r} 15. \quad 32 \\ - 4\frac{5}{22} \\ \hline \end{array}$$

$$\begin{array}{r} 20. \quad 9\frac{11}{20} \\ - 5\frac{12}{20} \\ \hline \end{array}$$

More Subtraction of Fractions with Renaming

EXAMPLE

Rename the fractions and subtract them. Subtract the whole numbers. Simplify if necessary.

$$\begin{array}{r} 3\frac{2}{5} = 3\frac{16}{40} = 2\frac{56}{40} \\ - 2\frac{7}{8} = - 2\frac{35}{40} = - 2\frac{35}{40} \\ \hline \frac{21}{40} \end{array}$$

Directions Subtract these fractions. Simplify the answers.

$$\begin{array}{r} 1. \quad 4\frac{3}{4} \\ - 3\frac{5}{6} \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad 6\frac{4}{13} \\ - 5\frac{25}{26} \\ \hline \end{array}$$

$$\begin{array}{r} 11. \quad 4 \\ - 2\frac{3}{5} \\ \hline \end{array}$$

$$\begin{array}{r} 16. \quad 9\frac{1}{3} \\ - 4\frac{11}{13} \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 14\frac{2}{9} \\ - 5\frac{7}{8} \\ \hline \end{array}$$

$$\begin{array}{r} 7. \quad 16\frac{9}{13} \\ - 4\frac{18}{26} \\ \hline \end{array}$$

$$\begin{array}{r} 12. \quad 3\frac{1}{2} \\ - 2\frac{6}{7} \\ \hline \end{array}$$

$$\begin{array}{r} 17. \quad 12\frac{14}{15} \\ - 10\frac{29}{30} \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 11\frac{1}{5} \\ - \frac{1}{4} \\ \hline \end{array}$$

$$\begin{array}{r} 8. \quad 29\frac{1}{15} \\ - 2\frac{3}{4} \\ \hline \end{array}$$

$$\begin{array}{r} 13. \quad 18\frac{2}{15} \\ - 5\frac{3}{4} \\ \hline \end{array}$$

$$\begin{array}{r} 18. \quad 10\frac{2}{5} \\ - 5\frac{10}{11} \\ \hline \end{array}$$

$$\begin{array}{r} 4. \quad 38\frac{2}{11} \\ - 4\frac{5}{22} \\ \hline \end{array}$$

$$\begin{array}{r} 9. \quad 12 \\ - 2\frac{10}{11} \\ \hline \end{array}$$

$$\begin{array}{r} 14. \quad 13\frac{3}{16} \\ - 4\frac{7}{8} \\ \hline \end{array}$$

$$\begin{array}{r} 19. \quad 10\frac{2}{7} \\ - 8\frac{11}{14} \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 45\frac{9}{11} \\ - 4\frac{21}{22} \\ \hline \end{array}$$

$$\begin{array}{r} 10. \quad 11\frac{1}{16} \\ - \frac{1}{2} \\ \hline \end{array}$$

$$\begin{array}{r} 15. \quad 23\frac{4}{7} \\ - 22\frac{9}{14} \\ \hline \end{array}$$

$$\begin{array}{r} 20. \quad 4\frac{5}{16} \\ - 2\frac{3}{8} \\ \hline \end{array}$$

Subtraction of Fractions

EXAMPLE

Change to common denominators if necessary. Rename top mixed number if necessary. Subtract numerators. Simplify if necessary.

$$\begin{array}{r} 1\frac{7}{18} \\ - \frac{5}{9} \\ \hline \end{array} = \begin{array}{r} 1\frac{7}{18} \\ - \frac{10}{18} \\ \hline \end{array} = \begin{array}{r} \frac{25}{18} \\ - \frac{10}{18} \\ \hline \end{array} = \begin{array}{r} \frac{15}{18} \\ = \frac{5}{6} \end{array}$$

Directions Subtract these fractions. Simplify the answers to the lowest terms.

1.
$$\begin{array}{r} \frac{7}{18} \\ - \frac{3}{18} \\ \hline \end{array}$$

5.
$$\begin{array}{r} 2\frac{5}{13} \\ - \frac{4}{13} \\ \hline \end{array}$$

9.
$$\begin{array}{r} 16\frac{2}{7} \\ - 2\frac{3}{7} \\ \hline \end{array}$$

13.
$$\begin{array}{r} 16\frac{3}{10} \\ - 1\frac{5}{10} \\ \hline \end{array}$$

2.
$$\begin{array}{r} 16\frac{12}{13} \\ - 3\frac{1}{26} \\ \hline \end{array}$$

6.
$$\begin{array}{r} 4\frac{15}{16} \\ - 2\frac{3}{8} \\ \hline \end{array}$$

10.
$$\begin{array}{r} 10\frac{13}{24} \\ - 2\frac{1}{6} \\ \hline \end{array}$$

14.
$$\begin{array}{r} 7\frac{5}{11} \\ - 3 \\ \hline \end{array}$$

3.
$$\begin{array}{r} 33\frac{1}{5} \\ - 2\frac{3}{4} \\ \hline \end{array}$$

7.
$$\begin{array}{r} 18 \\ - 5\frac{2}{7} \\ \hline \end{array}$$

11.
$$\begin{array}{r} 13 \\ - 2\frac{3}{11} \\ \hline \end{array}$$

15.
$$\begin{array}{r} 59\frac{1}{15} \\ - 2\frac{3}{45} \\ \hline \end{array}$$

4.
$$\begin{array}{r} 23\frac{7}{18} \\ - \frac{3}{72} \\ \hline \end{array}$$

8.
$$\begin{array}{r} 5\frac{1}{10} \\ - 2\frac{7}{15} \\ \hline \end{array}$$

12.
$$\begin{array}{r} 12 \\ - 6\frac{3}{13} \\ \hline \end{array}$$

16.
$$\begin{array}{r} 12\frac{3}{16} \\ - 5\frac{11}{48} \\ \hline \end{array}$$

Directions Rewrite the fractions in the standard form and subtract. Simplify the answers to the lowest terms.

17. $3\frac{1}{4} - 2\frac{7}{8} =$ _____

19. $6\frac{5}{12} - 4\frac{1}{5} =$ _____

18. $13\frac{2}{15} - 3\frac{4}{5} =$ _____

20. $38 - 2\frac{3}{7} =$ _____

Basic Operations with Fractions and Mixed Numbers

	Add.	Subtract.	Multiply.	Divide.
EXAMPLES	$\begin{array}{r} \frac{3}{4} \\ + \frac{3}{4} \\ \hline \frac{6}{4} = 1\frac{1}{2} \end{array}$	$\begin{array}{r} 1\frac{5}{8} \\ - 1\frac{3}{8} \\ \hline \frac{2}{8} = \frac{1}{4} \end{array}$	$1\frac{2}{3} \times \frac{3}{10} = \frac{1}{5}$	$\frac{1}{4} \div \frac{7}{8} = \frac{1}{4} \times \frac{8^2}{7} = \frac{2}{7}$

Directions Add.

1. $2\frac{1}{3} + 3\frac{1}{3} =$ _____

2. $4\frac{1}{8} + 2\frac{2}{8} =$ _____

3. $1\frac{1}{5} + \frac{1}{10} =$ _____

4. $2\frac{1}{6} + 3\frac{2}{3} =$ _____

5. $4\frac{1}{7} + 1\frac{3}{14} =$ _____

6. $1\frac{1}{8} + 2\frac{1}{6} =$ _____

Directions Subtract.

7. $5\frac{2}{8} - 1\frac{1}{4} =$ _____

8. $2\frac{2}{3} - 1\frac{1}{2} =$ _____

9. $4\frac{7}{8} - 1\frac{3}{4} =$ _____

10. $6\frac{2}{8} - 2\frac{3}{4} =$ _____

11. $35 - 6\frac{2}{7} =$ _____

12. $41\frac{3}{5} - 6 =$ _____

Directions Multiply.

13. $\frac{5}{6} \times \frac{2}{3} =$ _____

14. $\frac{4}{11} \times \frac{22}{10} =$ _____

15. $\frac{1}{2} \times \frac{2}{3} =$ _____

16. $2\frac{3}{5} \times 1\frac{1}{3} =$ _____

17. $6\frac{2}{9} \times \frac{1}{2} =$ _____

18. $1\frac{1}{8} \times 2\frac{3}{5} =$ _____

Directions Divide.

19. $\frac{6}{8} \div \frac{18}{24} =$ _____

20. $\frac{5}{6} \div \frac{25}{30} =$ _____

21. $\frac{4}{11} \div \frac{18}{20} =$ _____

22. $1\frac{1}{2} \div \frac{3}{6} =$ _____

23. $2\frac{1}{4} \div \frac{9}{10} =$ _____

24. $2\frac{3}{5} \div \frac{26}{30} =$ _____

25. $1\frac{2}{9} \div 1\frac{1}{2} =$ _____

Place Value

EXAMPLE

Look at the underlined digit. Write the place value for the underlined digit.

3.754 _____ hundredths _____

Directions Write the place value for each underlined digit.

- | | | | |
|-----------------------|-------|-----------------------|-------|
| 1. 2. <u>3</u> 4 | _____ | 9. 2.107 <u>6</u> 9 | _____ |
| 2. 1.2 <u>0</u> 345 | _____ | 10. 502.0 <u>0</u> 1 | _____ |
| 3. 1.02 <u>3</u> 01 | _____ | 11. 3.40 <u>0</u> 1 | _____ |
| 4. 12. <u>0</u> 1012 | _____ | 12. 7. <u>3</u> 309 | _____ |
| 5. 0.0 <u>0</u> 12 | _____ | 13. 1.0 <u>0</u> 23 | _____ |
| 6. 12.00 <u>2</u> 00 | _____ | 14. 0.002 <u>0</u> 03 | _____ |
| 7. 1.2 <u>2</u> 008 | _____ | 15. 3.004 <u>1</u> 0 | _____ |
| 8. 840. <u>8</u> 8940 | _____ | 16. 23.000 <u>1</u> 9 | _____ |

Directions Underline the place value indicated.

- | | | | |
|-----------------------|---------------------|------------------------|---------------------|
| 17. 12.000 <u>2</u> | ten-thousandths | 24. 0.0101 <u>0</u> 2 | millionths |
| 18. 0.0 <u>1</u> 2 | tenths | 25. 2.090 <u>7</u> 7 | hundred-thousandths |
| 19. 0.000 <u>2</u> 3 | hundred-thousandths | 26. 10.102 <u>3</u> 0 | hundred-thousandths |
| 20. 0.000 <u>1</u> 2 | thousandths | 27. 530.000 <u>2</u> | tenths |
| 21. 1.02 <u>3</u> 04 | tenths | 28. 2.9 <u>3</u> 001 | ten-thousandths |
| 22. 102.00 <u>2</u> 3 | tenths | 29. 0.0112 <u>8</u> 87 | millionths |
| 23. 3.04 <u>9</u> 58 | ten-thousandths | 30. 1.02 <u>3</u> 4 | tenths |

Reading and Writing Numerals

EXAMPLES

Look at the underlined digit. Write the name of the place.

3.143 _____ thousandths _____

Start at the left. Write the word for the numerals.
Use *and* to stand for the decimal point.

1.63 _____ one and sixty-three hundredths _____

Directions Write the name of the place for each underlined digit.

- | | | |
|--|--|---|
| 1. 12. <u>1</u> 8 _____ | 9. 8.0 <u>2</u> 63 _____ | 17. 3. <u>0</u> 4 _____ |
| 2. 0.9 <u>2</u> 0 _____ | 10. 4.0 <u>0</u> 05 _____ | 18. 0.003 <u>7</u> 05 _____ |
| 3. 1.0 <u>3</u> 4 _____ | 11. 4.590 <u>2</u> 1 _____ | 19. 0.003 <u>0</u> 4 _____ |
| 4. 3.05 <u>7</u> 8 _____ | 12. 295. <u>1</u> 1 _____ | 20. 59.04 <u>9</u> 2 _____ |
| 5. 64.23 <u>8</u> 1 _____ | 13. 5.02 <u>8</u> 48 _____ | 21. 83.3 <u>9</u> 051 _____ |
| 6. 0.0 <u>0</u> 3 _____ | 14. 45.922 <u>1</u> 0 _____ | 22. 19.460 <u>3</u> 1 _____ |
| 7. 152. <u>9</u> _____ | 15. 394.0 <u>2</u> 64 _____ | 23. 44. <u>9</u> 12 _____ |
| 8. 24.022 <u>3</u> 1 _____ | 16. 385.044 <u>8</u> 5 _____ | 24. 5.610 <u>5</u> 6 _____ |

Directions Write the following numerals in words.

- 25.** 9.032 _____

- 26.** 0.0024 _____

- 27.** 102.10245 _____

- 28.** 0.010139 _____

- 29.** 40.044 _____

- 30.** 410.00003 _____

Translation of Decimal Numbers

EXAMPLE

Read the amount. Write it in numerals. Remember, *and* stands for the decimal point.

Five and seventy-one hundredths 5.71

Directions Write the following amounts in numerals.

1. Twenty-three and six tenths _____
2. Forty-one and three hundredths _____
3. Seventy-two thousandths _____
4. Five and eight tenths _____
5. Six and three thousandths _____
6. One hundred two thousandths _____
7. Four hundred three thousandths _____
8. Two and two hundredths _____
9. Six hundred thirty-four ten-thousandths _____
10. Six thousand, three hundred forty-eight hundred-thousandths _____
11. Twenty thousand, four hundred five hundred-thousandths _____
12. One hundred two and seven hundredths _____
13. Eight hundred two and seven hundred fifty-one thousandths _____
14. One thousand, nine hundred three and seven hundredths _____
15. Two thousand and twenty-six thousandths _____
16. Four thousand three and seven ten-thousandths _____
17. Two hundred six thousandths _____
18. Three hundred-thousandths _____
19. Thirty-four hundred-thousandths _____
20. One and fifty-nine hundredths _____

Comparing and Rounding Decimals

EXAMPLE

Order numbers from least to greatest.

1.059 0.0159 0.159 Least \longrightarrow Greatest
 0.0159 0.159 1.059

Directions Arrange each set in order from least to greatest.

- | | | | | | |
|-------------|----------|----------|-------|-------|-------|
| 1. 0.6234 | 62.350 | 0.7406 | _____ | _____ | _____ |
| 2. 0.0045 | 0.0450 | 0.0040 | _____ | _____ | _____ |
| 3. 2.0049 | 2.0050 | 2.034 | _____ | _____ | _____ |
| 4. 0.1024 | 0.1031 | 0.113 | _____ | _____ | _____ |
| 5. 23.0045 | 23.004 | 2.30045 | _____ | _____ | _____ |
| 6. 304.097 | 300.999 | 304.102 | _____ | _____ | _____ |
| 7. 3.00495 | 30.0495 | 0.300495 | _____ | _____ | _____ |
| 8. 9.00603 | 9.00599 | 9.000999 | _____ | _____ | _____ |
| 9. 0.356924 | 0.350899 | 0.400001 | _____ | _____ | _____ |
| 10. 5.04592 | 6.001 | 0.939401 | _____ | _____ | _____ |

EXAMPLE

Round to the nearest hundredth. Round up if thousandth is 5 or greater.

5.136
5.14

Directions Round the following numbers to the nearest:

- | | Tenth | | Hundredth | | Thousandth |
|--------------|-------|----------------|-----------|----------------|------------|
| 11. 245.44 | _____ | 19. 0.0394 | _____ | 28. 0.08931 | _____ |
| 12. 4.091 | _____ | 20. 199.051 | _____ | 29. 0.00592 | _____ |
| 13. 2.0399 | _____ | 21. 6.34499 | _____ | 30. 10.122309 | _____ |
| 14. 0.048 | _____ | 22. 0.995 | _____ | 31. 0.39 | _____ |
| 15. 30.9199 | _____ | 23. 666.034 | _____ | 32. 390.0485 | _____ |
| 16. 0.048539 | _____ | 24. 394.091999 | _____ | 33. 3,998.0002 | _____ |
| 17. 5.0555 | _____ | 25. 0.0951 | _____ | 34. 8.89099 | _____ |
| 18. 49.952 | _____ | 26. 495.0495 | _____ | 35. 4.76842 | _____ |
| | | 27. 40.0495 | _____ | | |

Addition of Decimals

EXAMPLE

Write the problem in vertical form. Then add.

$$\begin{array}{r}
 2.3 + 4 + 0.09 + 59 = \\
 \begin{array}{r}
 2.3 \\
 4. \\
 0.09 \\
 + 59. \\
 \hline
 65.39
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 2.30 \\
 4.00 \\
 0.09 \\
 + 59.00 \\
 \hline
 65.39
 \end{array}$$

Directions Rewrite the following addends in vertical form and add.

- | | |
|--|---|
| 1. $3.4 + 5 + 0.18 + 17 =$ _____ | 15. $4.4 + 3.5 + 23.49 + 6 =$ _____ |
| 2. $0.056 + 3.02 + 4 + 1.2 =$ _____ | 16. $6.06 + 33 + 0.045 + 3 =$ _____ |
| 3. $19 + 9.3 + 0.049 + 3 =$ _____ | 17. $5 + 6 + 6.9 + 0.082 =$ _____ |
| 4. $30.9 + 5 + 0.91 + 0.922 =$ _____ | 18. $6.112 + 4.7 + 6 + 0.0001 =$ _____ |
| 5. $0.08 + 1 + 1.1 + 6.2 =$ _____ | 19. $9.9 + 5.03 + 5.5 + 0.002 =$ _____ |
| 6. $2.331 + 0.1123 + 7 + 1.8 =$ _____ | 20. $47.05 + 6.2 + 0.4 + 1 =$ _____ |
| 7. $16 + 4.05 + 5 + 4.77 =$ _____ | 21. $54 + 2.2 + 0.01 + 6.9 =$ _____ |
| 8. $65.94 + 4.7 + 1 + 7.2 =$ _____ | 22. $2.334 + 0.1128 + 8.3 =$ _____ |
| 9. $5.906 + 0.071 + 44.581 =$ _____ | 23. $4.056 + 3.5 + 7 + 0.92 =$ _____ |
| 10. $3.045 + 0.045 + 84.3 =$ _____ | 24. $5 + 6.1 + 55.6 + 0.01 =$ _____ |
| 11. $0.9639 + 0.0082 + 5.03 =$ _____ | 25. $6.001 + 4.9 + 3 + 0.05 =$ _____ |
| 12. $7.304 + 1.5 + 8.33 + 2 =$ _____ | 26. $1 + 2.1 + 5.66 + 0.031 =$ _____ |
| 13. $7004.1 + 35.066 + 0.06 =$ _____ | 27. $9.9 + 3.4 + 0.56 + 0.012 =$ _____ |
| 14. $93 + 0.739 + 2.38 + 0.1 =$ _____ | 28. $6.035 + 3.4 + 5 + 0.057 =$ _____ |

Directions Solve the following word problems with addition.

- 29.** Compute the total amount deposited if Lance's deposits are \$15, \$1.90, \$121, and \$2.65. _____
- 30.** It rains three times during the first week of summer vacation. Compute the total amount if it rains 2.05 inches, 0.29 inches, and 3 inches. _____

Subtraction of Decimals

EXAMPLE

Write the problem in vertical form. Then subtract.

$$\begin{array}{r}
 1.03 - 0.94 = \\
 \begin{array}{r}
 0913 \\
 \cancel{1}.\cancel{0}\cancel{3} \\
 - 0.94 \\
 \hline
 0.09
 \end{array}
 \end{array}$$

Directions Rewrite these problems in vertical form. Then subtract.

- | | |
|---------------------------------------|--------------------------------------|
| 1. $6.34 - 0.14 =$ _____ | 15. $58.3 - 12.923 =$ _____ |
| 2. From 23.034 subtract 0.0341 _____ | 16. From 4.95 subtract 2.5 _____ |
| 3. $20 - 0.934 =$ _____ | 17. $71 - 5.341 =$ _____ |
| 4. Subtract 12.92 from 27.104 _____ | 18. Subtract 0.3945 from 6 _____ |
| 5. $103.506 - 94 =$ _____ | 19. $0.304 - 0.0433 =$ _____ |
| 6. Subtract 0.607 from 2 _____ | 20. From 205.5 subtract 0.56 _____ |
| 7. $2.3941 - 0.2852 =$ _____ | 21. $4.59 - 2.4 =$ _____ |
| 8. From 1.0182 subtract 0.81818 _____ | 22. Subtract 2.3 from 5 _____ |
| 9. $34.8 - 5.0837 =$ _____ | 23. $4.5 - 0.0954 =$ _____ |
| 10. From 2 subtract 1.9283 _____ | 24. From 6.94 subtract 0.9567 _____ |
| 11. $0.0238 - 0.003856 =$ _____ | 25. $49 - 5.607 =$ _____ |
| 12. Subtract 9.9 from 10.005 _____ | 26. Subtract 0.0384 from 1.991 _____ |
| 13. $1.3 - 1.0953 =$ _____ | 27. $3 - 0.4581 =$ _____ |
| 14. Subtract 0.0056 from 0.9 _____ | 28. From 86 subtract 0.86 _____ |

Directions Solve the following word problems with subtraction.

29. Diana saves \$25 for school clothes and purchases a blouse costing \$9.96. How much money does she have left? _____
30. Ross drives 298.6 miles on a two-day vacation. If he drives 150 miles on the first day, how many miles does he drive on the second day? _____

Multiplication of Decimals by Powers of Ten

EXAMPLE

Write the problem in vertical form.
Then multiply. Remember the decimal point.

$$2.63 \times 10 =$$

$$\begin{array}{r} 2.63 \\ \times 10 \\ \hline 26.30 \end{array}$$

Directions Rewrite the following problems in vertical form and multiply.

- | | |
|--|--|
| 1. $6.25 \times 10 =$ _____ | 24. $0.028 \times 10 =$ _____ |
| 2. $5.638 \times 10 =$ _____ | 25. $0.002 \times 1,000 =$ _____ |
| 3. $0.06 \times 100 =$ _____ | 26. $1.1 \times 1,000 =$ _____ |
| 4. $0.072 \times 100 =$ _____ | 27. $10 \times 1.67 =$ _____ |
| 5. $1.061 \times 10 =$ _____ | 28. $1,000 \times 0.003 =$ _____ |
| 6. $5.63 \times 100 =$ _____ | 29. $100 \times 0.1505 =$ _____ |
| 7. $3.14 \times 100 =$ _____ | 30. $10 \times 1.688 =$ _____ |
| 8. $1.414 \times 1,000 =$ _____ | 31. $1,000 \times 3.9 =$ _____ |
| 9. $0.00627 \times 1,000 =$ _____ | 32. $100 \times 3.702 =$ _____ |
| 10. $0.2802 \times 10 =$ _____ | 33. $10 \times 0.1 =$ _____ |
| 11. $0.0605 \times 100 =$ _____ | 34. $1,000 \times 0.11 =$ _____ |
| 12. $0.7701 \times 100 =$ _____ | 35. $3.44 \times 100 =$ _____ |
| 13. $1.101 \times 1,000 =$ _____ | 36. $1.112 \times 1,000 =$ _____ |
| 14. $7.6 \times 100 =$ _____ | 37. $0.00232 \times 10,000 =$ _____ |
| 15. $5.1 \times 1,000 =$ _____ | 38. $0.012 \times 10,000 =$ _____ |
| 16. $8.81 \times 10,000 =$ _____ | 39. $3.033 \times 10 =$ _____ |
| 17. $3.7 \times 10,000 =$ _____ | 40. $8.014 \times 1,000 =$ _____ |
| 18. $2.05 \times 10,000 =$ _____ | 41. $0.0556 \times 10,000 =$ _____ |
| 19. $0.0001 \times 1,000 =$ _____ | 42. $5.5 \times 100 =$ _____ |
| 20. $5.6 \times 100 =$ _____ | 43. $0.6709 \times 100 =$ _____ |
| 21. $69.1 \times 1,000 =$ _____ | 44. $0.0021 \times 1,000 =$ _____ |
| 22. $0.777 \times 1,000 =$ _____ | 45. $23.1 \times 100 =$ _____ |
| 23. $0.201 \times 10,000 =$ _____ | |

Multiplication of Decimals

EXAMPLE

Write the problem in vertical form.
Then multiply. Remember the decimal point.
 $1.2 \times 0.04 =$

$$\begin{array}{r} 1.2 \\ \times .04 \\ \hline 48 \\ 00 \\ \hline 0.048 \end{array}$$

Directions Rewrite the following problems in vertical form and multiply.

- | | |
|---------------------------------------|---|
| 1. $3.5 \times 0.11 =$ _____ | 15. $0.09 \times 0.04 =$ _____ |
| 2. $48 \times 1.5 =$ _____ | 16. $7.05 \times 0.3 =$ _____ |
| 3. $4.05 \times 0.03 =$ _____ | 17. $98 \times 0.11 =$ _____ |
| 4. $3.6 \times 0.93 =$ _____ | 18. $0.931 \times 100 =$ _____ |
| 5. $56.7 \times 0.31 =$ _____ | 19. $7.02 \times 5.1 =$ _____ |
| 6. $0.059 \times 0.12 =$ _____ | 20. $0.034 \times 0.0048 =$ _____ |
| 7. $9.01 \times 1.03 =$ _____ | 21. $1,000 \times 0.00342 =$ _____ |
| 8. $5.8 \times 0.0004 =$ _____ | 22. $405 \times 1.52 =$ _____ |
| 9. $0.0034 \times 23 =$ _____ | 23. $8.8 \times 6.7 =$ _____ |
| 10. $6.12 \times 3.4 =$ _____ | 24. $13.5 \times 4.7 =$ _____ |
| 11. $7.81 \times 56 =$ _____ | 25. $69.1 \times 0.001 =$ _____ |
| 12. $5.25 \times 0.01 =$ _____ | 26. $10.4 \times 10.5 =$ _____ |
| 13. $6.79 \times 8.3 =$ _____ | 27. $0.059 \times 0.0691 =$ _____ |
| 14. $0.044 \times 0.9 =$ _____ | 28. $0.101 \times 121.1 =$ _____ |

Directions Solve the following word problems with multiplication.

- 29.** Lionel works part-time with a construction company and earns \$24.50 per day. How much will Lionel earn working 5 days? _____
- 30.** Regina earns \$7.50 per hour straight time. Compute Regina's time and one-half rate by finding the product of \$7.50 and 1.5. _____

Scientific Notation with Positive Exponents

EXAMPLE

Write in scientific notation.

$$2,300,000 = 2.3 \times 10^6$$

↑
 a number
 between one
 and ten

← an exponent
 ← a power of ten

Directions Rewrite the following numbers using scientific notation.

- | | |
|---|--|
| <p>1. 4,200 = _____</p> <p>2. 6,250 = _____</p> <p>3. 82,100 = _____</p> <p>4. 50,000 = _____</p> <p>5. 72,300 = _____</p> <p>6. 15,080 = _____</p> <p>7. 1,800 = _____</p> <p>8. 29,000 = _____</p> <p>9. 500,000 = _____</p> <p>10. 600,000 = _____</p> <p>11. 700,000,000 = _____</p> <p>12. 7,800,000 = _____</p> <p>13. 10,000 = _____</p> <p>14. 35,600 = _____</p> <p>15. 81.52 = _____</p> <p>16. 17.63 = _____</p> <p>17. 236.5 = _____</p> <p>18. 3,800 = _____</p> <p>19. 19,000 = _____</p> <p>20. 16.12 = _____</p> <p>21. 610,000,000 = _____</p> <p>22. 400,000,000 = _____</p> <p>23. 790,000 = _____</p> | <p>24. 25.33 = _____</p> <p>25. 1,420,000 = _____</p> <p>26. 1,000,000,000 = _____</p> <p>27. 34,000,000 = _____</p> <p>28. 103,000 = _____</p> <p>29. 23,000 = _____</p> <p>30. 450,000,000 = _____</p> <p>31. 11,000 = _____</p> <p>32. 401,300 = _____</p> <p>33. 311,400 = _____</p> <p>34. 102.3 = _____</p> <p>35. 927,000 = _____</p> <p>36. 211,400 = _____</p> <p>37. 100,000 = _____</p> <p>38. 10,000 = _____</p> <p>39. 344,000,000,000 = _____</p> <p>40. 42,000,000,000 = _____</p> <p>41. 12,000,000 = _____</p> <p>42. 41,000,000 = _____</p> <p>43. 764,200,000 = _____</p> <p>44. 911,400,000 = _____</p> <p>45. 102,000 = _____</p> |
|---|--|

Scientific Notation with Negative Exponents

EXAMPLE

Write in scientific notation.

$$0.006 = 6 \times 10^{-3}$$

↑ ←
 a number a negative exponent
 between one and ten

Directions Rewrite the following numbers using scientific notation.

- | | |
|--|---|
| <p>1. 0.008 = _____</p> <p>2. 0.0715 = _____</p> <p>3. 0.0062 = _____</p> <p>4. 0.0007 = _____</p> <p>5. 0.02 = _____</p> <p>6. 0.0321 = _____</p> <p>7. 0.0805 = _____</p> <p>8. 0.0006 = _____</p> <p>9. 0.00005 = _____</p> <p>10. 0.03051 = _____</p> <p>11. 0.00091 = _____</p> <p>12. 0.0000007 = _____</p> <p>13. 0.000003 = _____</p> <p>14. 0.00000021 = _____</p> <p>15. 0.0061 = _____</p> <p>16. 0.00054 = _____</p> <p>17. 0.000003 = _____</p> <p>18. 0.00101 = _____</p> <p>19. 0.000005 = _____</p> <p>20. 0.000052 = _____</p> <p>21. 0.000735 = _____</p> <p>22. 0.0001433 = _____</p> <p>23. 0.00021 = _____</p> | <p>24. 0.00093 = _____</p> <p>25. 0.000000004 = _____</p> <p>26. 0.00000000062 = _____</p> <p>27. 0.423 = _____</p> <p>28. 0.00316 = _____</p> <p>29. 0.005071 = _____</p> <p>30. 0.000078 = _____</p> <p>31. 0.002103 = _____</p> <p>32. 0.0000000005 = _____</p> <p>33. 0.00000123 = _____</p> <p>34. 0.00203 = _____</p> <p>35. 0.000222 = _____</p> <p>36. 0.0121 = _____</p> <p>37. 0.10203 = _____</p> <p>38. 0.000204 = _____</p> <p>39. 0.0691 = _____</p> <p>40. 0.0000203 = _____</p> <p>41. 0.0000000304 = _____</p> <p>42. 0.3044 = _____</p> <p>43. 0.00077 = _____</p> <p>44. 0.002058 = _____</p> <p>45. 0.0004058 = _____</p> |
|--|---|

Scientific Notation in Standard Form

EXAMPLES

Write in standard form.

$$5.1 \times 10^2$$

$$5 \cdot \overset{1}{\underbrace{10}} = 510$$

$$5.1 \times 10^{-2}$$

$$0 \cdot \overset{2}{\underbrace{05}} \cdot 1 = 0.051$$

Directions Rewrite each scientific notation in standard form.

- | | |
|----------------------------------|------------------------------------|
| 1. $5.6 \times 10^2 =$ _____ | 24. $7 \times 10^{10} =$ _____ |
| 2. $1.5 \times 10^2 =$ _____ | 25. $1.9 \times 10^{-8} =$ _____ |
| 3. $2 \times 10^4 =$ _____ | 26. $3 \times 10^{-9} =$ _____ |
| 4. $8 \times 10^3 =$ _____ | 27. $5.03 \times 10^{-1} =$ _____ |
| 5. $4.65 \times 10^3 =$ _____ | 28. $4.06 \times 10^{-4} =$ _____ |
| 6. $1.73 \times 10^4 =$ _____ | 29. $6.003 \times 10^{-5} =$ _____ |
| 7. $6.203 \times 10^5 =$ _____ | 30. $1.01 \times 10^{-5} =$ _____ |
| 8. $2.414 \times 10^5 =$ _____ | 31. $4.5 \times 10^{-5} =$ _____ |
| 9. $8.5 \times 10^7 =$ _____ | 32. $5.012 \times 10^{-3} =$ _____ |
| 10. $3 \times 10^7 =$ _____ | 33. $6 \times 10^{-5} =$ _____ |
| 11. $2 \times 10^1 =$ _____ | 34. $7.01 \times 10^{-4} =$ _____ |
| 12. $5.16 \times 10^2 =$ _____ | 35. $2.34 \times 10^{-3} =$ _____ |
| 13. $8.2 \times 10^3 =$ _____ | 36. $4.535 \times 10^{-2} =$ _____ |
| 14. $1.2 \times 10^1 =$ _____ | 37. $1 \times 10^{-8} =$ _____ |
| 15. $7.502 \times 10^2 =$ _____ | 38. $1.024 \times 10^{-2} =$ _____ |
| 16. $3.0052 \times 10^2 =$ _____ | 39. $4.441 \times 10^{-5} =$ _____ |
| 17. $2.61 \times 10^3 =$ _____ | 40. $7.002 \times 10^{-4} =$ _____ |
| 18. $5.85 \times 10^4 =$ _____ | 41. $2.001 \times 10^{-8} =$ _____ |
| 19. $7.05 \times 10^4 =$ _____ | 42. $3.3 \times 10^{-3} =$ _____ |
| 20. $6 \times 10^4 =$ _____ | 43. $6.77 \times 10^{-4} =$ _____ |
| 21. $3.008 \times 10^3 =$ _____ | 44. $4.001 \times 10^{-3} =$ _____ |
| 22. $1.9 \times 10^2 =$ _____ | 45. $5 \times 10^{-10} =$ _____ |
| 23. $4.002 \times 10^4 =$ _____ | |

Scientific Notation

EXAMPLE

Write in scientific notation. $0.00563 = 0.\underbrace{005}_{1\ 2\ 3}.63 = 5.63 \times 10^{-3}$

Directions Rewrite the following numbers using scientific notation.

- | | |
|---------------------------|---------------------------------|
| 1. 2,300,000 = _____ | 9. 1,900,000,000 = _____ |
| 2. 59,000 = _____ | 10. 39,400,000 = _____ |
| 3. 0.0005 = _____ | 11. 0.00000837 = _____ |
| 4. 0.0000039 = _____ | 12. 567.2 = _____ |
| 5. 23.41 = _____ | 13. 0.0001 = _____ |
| 6. 453 = _____ | 14. 4,000 = _____ |
| 7. 25,400,000 = _____ | 15. 0.00495 = _____ |
| 8. 0.000000000843 = _____ | 16. 567,000,000,000,000 = _____ |

EXAMPLE

Write in standard form. $5.63 \times 10^{-3} = 0.\underbrace{005}_{3\ 2\ 1}.63 = 0.00563$

Directions Write the following numbers in standard form without exponents.

- | | |
|-----------------------------------|-----------------------------------|
| 17. $2.3 \times 10^3 =$ _____ | 24. $5.5 \times 10^{-3} =$ _____ |
| 18. $4.29 \times 10^5 =$ _____ | 25. $6.832 \times 10^6 =$ _____ |
| 19. $8 \times 10^6 =$ _____ | 26. $8.11 \times 10^{-2} =$ _____ |
| 20. $5.7 \times 10^5 =$ _____ | 27. $3 \times 10^{12} =$ _____ |
| 21. $4.94 \times 10^{-8} =$ _____ | 28. $1.35 \times 10^{-5} =$ _____ |
| 22. $7.03 \times 10^{-7} =$ _____ | 29. $1.39 \times 10^7 =$ _____ |
| 23. $6.1 \times 10^{10} =$ _____ | 30. $9.04 \times 10^{-4} =$ _____ |

Division of Decimals by Powers of Ten

EXAMPLEWrite in standard form. Divide $53 \div 10 =$

$$\begin{array}{r} 5.3 \\ 10 \overline{)53.0} \\ \underline{-50} \\ 30 \\ \underline{-30} \\ 0 \end{array}$$

Directions Rewrite the following division problems in the standard form and divide.

- | | |
|--------------------------------|-----------------------------------|
| 1. $62 \div 10 =$ _____ | 24. $2,963 \div 1,000 =$ _____ |
| 2. $7.7 \div 100 =$ _____ | 25. $8,203 \div 10,000 =$ _____ |
| 3. $0.07 \div 100 =$ _____ | 26. $4,002 \div 100 =$ _____ |
| 4. $39 \div 1,000 =$ _____ | 27. $0.706 \div 10 =$ _____ |
| 5. $3 \div 10 =$ _____ | 28. $9 \div 1,000 =$ _____ |
| 6. $4.07 \div 100 =$ _____ | 29. $0.04 \div 100 =$ _____ |
| 7. $3.02 \div 100 =$ _____ | 30. $0.3006 \div 100 =$ _____ |
| 8. $8.4 \div 1,000 =$ _____ | 31. $0.35 \div 1,000 =$ _____ |
| 9. $100 \div 1,000 =$ _____ | 32. $4.02 \div 100 =$ _____ |
| 10. $5.6 \div 10 =$ _____ | 33. $17 \div 1,000 =$ _____ |
| 11. $7 \div 100 =$ _____ | 34. $1 \div 1,000 =$ _____ |
| 12. $6.2 \div 1,000 =$ _____ | 35. $4.2 \div 10,000 =$ _____ |
| 13. $1.8 \div 1,000 =$ _____ | 36. $0.02 \div 10,000 =$ _____ |
| 14. $94 \div 100 =$ _____ | 37. $45.7 \div 10,000 =$ _____ |
| 15. $5 \div 1,000 =$ _____ | 38. $5,023.5 \div 10,000 =$ _____ |
| 16. $13 \div 1,000 =$ _____ | 39. $51.5 \div 1,000 =$ _____ |
| 17. $2.6 \div 1,000 =$ _____ | 40. $6.66 \div 10,000 =$ _____ |
| 18. $8.6 \div 100 =$ _____ | 41. $3.02 \div 1,000 =$ _____ |
| 19. $0.0023 \div 10 =$ _____ | 42. $728 \div 10 =$ _____ |
| 20. $2 \div 1,000 =$ _____ | 43. $936 \div 10,000 =$ _____ |
| 21. $3.8 \div 100 =$ _____ | 44. $641.02 \div 10,000 =$ _____ |
| 22. $4.02 \div 10,000 =$ _____ | 45. $5.5 \div 100 =$ _____ |
| 23. $566 \div 1,000 =$ _____ | |

Division of Decimals

EXAMPLE

Write in standard form.
Move decimal. Divide 23.4 by 0.1 =

$$\begin{array}{r} 234 \\ 0.1 \overline{)23.4} \\ \underline{-2} \\ 03 \\ \underline{-3} \\ 04 \\ \underline{-4} \\ 0 \end{array}$$

Directions Rewrite the following division problems in the standard form and divide. Round each quotient to the nearest hundredth.

- | | |
|------------------------------|--------------------------------|
| 1. $14.4 \div 0.7 =$ _____ | 15. $3.5 \div 3 =$ _____ |
| 2. $0.46 \div 0.4 =$ _____ | 16. $6.33 \div 0.07 =$ _____ |
| 3. $0.98 \div 0.8 =$ _____ | 17. $1 \div 0.9 =$ _____ |
| 4. $10 \div 5.5 =$ _____ | 18. $2.2 \div 13 =$ _____ |
| 5. $1.5 \div 0.9 =$ _____ | 19. $30 \div 89 =$ _____ |
| 6. $2.6 \div 1.5 =$ _____ | 20. $5.06 \div 1.2 =$ _____ |
| 7. $0.06 \div 0.7 =$ _____ | 21. $5 \div 1.5 =$ _____ |
| 8. $40 \div 1.2 =$ _____ | 22. $49.9 \div 3.4 =$ _____ |
| 9. $7.7 \div 0.03 =$ _____ | 23. $2 \div 4.5 =$ _____ |
| 10. $5.6 \div 0.12 =$ _____ | 24. $0.506 \div 0.403 =$ _____ |
| 11. $12.3 \div 1.1 =$ _____ | 25. $4.06 \div 2.02 =$ _____ |
| 12. $6.99 \div 1.2 =$ _____ | 26. $0.0008 \div 0.04 =$ _____ |
| 13. $9.12 \div 0.9 =$ _____ | 27. $0.045 \div 0.08 =$ _____ |
| 14. $28.04 \div 0.7 =$ _____ | 28. $3.91 \div 2.6 =$ _____ |

Directions Solve the following word problems with division.

29. Kathleen purchases tomatoes for lunch. If the tomatoes are priced at 4 pounds for \$4.24, how much will she pay for one pound?
30. A carton of six colas sells for \$4.62. How much does one cola cost?

Basic Operations with Decimals

EXAMPLES

Add.

$$\begin{array}{r} 2.3 \\ + 5.67 \\ \hline 7.97 \end{array}$$

Subtract.

$$\begin{array}{r} 5910 \\ 36.00 \\ - 0.93 \\ \hline 35.07 \end{array}$$

Multiply.

$$\begin{array}{r} 2.2 \\ \times .9 \\ \hline 1.98 \end{array}$$

Divide.

$$\begin{array}{r} .3822 \\ 9 \overline{)3.4400} \\ \underline{-27} \\ 74 \\ \underline{-72} \\ 20 \\ \underline{-18} \\ 20 \\ \underline{-18} \\ 2 \end{array}$$

Directions Add.

- | | |
|---|--|
| 1. $2.3 + 5.67 =$ _____ | 5. $0.0745 + 0.45 + 0.087202 =$ _____ |
| 2. $45 + 9.97 + 0.055 =$ _____ | 6. $3.45 + 0.0923 + 3.07 =$ _____ |
| 3. $3.04 + 0.056 + 0.7 =$ _____ | 7. $2.33 + 0.76 + 74.9 + 4.4 =$ _____ |
| 4. $67.3 + 34.09 + 4.45 =$ _____ | 8. $0.0348 + 0.2 + 4 + 4.45 =$ _____ |

Directions Subtract.

- | | |
|-------------------------------------|-----------------------------------|
| 9. $36 - 0.93 =$ _____ | 13. $2.9 - 0.8033 =$ _____ |
| 10. $4.5 - 2.09 =$ _____ | 14. $50.4 - 28.48 =$ _____ |
| 11. $5.943 - 0.56 =$ _____ | 15. $1 - 0.97 =$ _____ |
| 12. $0.0982 - 0.039 =$ _____ | 16. $345 - 23.9 =$ _____ |

Directions Multiply.

- | | |
|---------------------------------------|--|
| 17. $2.2 \times 0.9 =$ _____ | 21. $30.5 \times 4.5 =$ _____ |
| 18. $34 \times 5.2 =$ _____ | 22. $3.409 \times 0.42 =$ _____ |
| 19. $6.7 \times 0.67 =$ _____ | 23. $90.4 \times 2.11 =$ _____ |
| 20. $45.3 \times 0.23 =$ _____ | 24. $5.63 \times 0.941 =$ _____ |

Directions Divide. Round the quotients to the nearest hundredths.

- | | |
|-------------------------------------|------------------------------------|
| 25. $3.44 \div 9 =$ _____ | 28. $36 \div 0.7 =$ _____ |
| 26. $98.3 \div 20 =$ _____ | 29. $3 \div 1.7 =$ _____ |
| 27. $1.304 \div 1.1 =$ _____ | 30. $5.606 \div 25 =$ _____ |

Decimals to Fractions

EXAMPLE

Rename 0.6 as a fraction. Simplify if necessary.

$$0.6 = \frac{6}{10} = \frac{3}{5}$$

Directions Rewrite each decimal as a fraction or a mixed number.
Simplify the answers to the lowest terms.

- | | | |
|--------------------|--------------------|--------------------|
| 1. 0.51 = _____ | 25. 0.9 = _____ | 49. 0.353 = _____ |
| 2. 0.07 = _____ | 26. 0.102 = _____ | 50. 7.2 = _____ |
| 3. 0.5 = _____ | 27. 0.052 = _____ | 51. 0.0004 = _____ |
| 4. 0.2 = _____ | 28. 0.0071 = _____ | 52. 0.1004 = _____ |
| 5. 0.003 = _____ | 29. 0.004 = _____ | 53. 46.85 = _____ |
| 6. 0.007 = _____ | 30. 0.38 = _____ | 54. 0.999 = _____ |
| 7. 0.75 = _____ | 31. 15.1 = _____ | 55. 0.122 = _____ |
| 8. 0.82 = _____ | 32. 3.75 = _____ | 56. 0.01 = _____ |
| 9. 0.15 = _____ | 33. 0.25 = _____ | 57. 0.106 = _____ |
| 10. 1.5 = _____ | 34. 2.25 = _____ | 58. 0.004 = _____ |
| 11. 0.62 = _____ | 35. 1.82 = _____ | 59. 0.147 = _____ |
| 12. 0.085 = _____ | 36. 0.21 = _____ | 60. 54.06 = _____ |
| 13. 0.008 = _____ | 37. 1.002 = _____ | 61. 1.85 = _____ |
| 14. 0.001 = _____ | 38. 0.52 = _____ | 62. 9.43 = _____ |
| 15. 2.6 = _____ | 39. 0.42 = _____ | 63. 7.78 = _____ |
| 16. 0.022 = _____ | 40. 2.125 = _____ | 64. 4.14 = _____ |
| 17. 0.04 = _____ | 41. 0.54 = _____ | 65. 0.335 = _____ |
| 18. 20.6 = _____ | 42. 0.0085 = _____ | 66. 1.38 = _____ |
| 19. 5.03 = _____ | 43. 4.48 = _____ | 67. 0.34 = _____ |
| 20. 4.1 = _____ | 44. 1.53 = _____ | 68. 0.554 = _____ |
| 21. 200.6 = _____ | 45. 10.5 = _____ | 69. 0.332 = _____ |
| 22. 0.0012 = _____ | 46. 1.18 = _____ | 70. 0.246 = _____ |
| 23. 0.041 = _____ | 47. 24.5 = _____ | |
| 24. 0.101 = _____ | 48. 0.0002 = _____ | |

Fractions to Decimals

EXAMPLE

 Rename $\frac{2}{3}$ as a decimal.

Round to nearest hundredth.

$$\begin{array}{r} .\overline{666} \rightarrow 0.67 \\ 3 \overline{)2.000} \\ \underline{-18} \\ 20 \\ \underline{-18} \\ 20 \\ \underline{-18} \\ 2 \end{array}$$

Directions Write each fraction as a decimal rounded to the nearest hundredth.

- | | | |
|-----------------------------|-----------------------------|-----------------------------|
| 1. $\frac{1}{15} =$ _____ | 16. $\frac{3}{11} =$ _____ | 31. $\frac{2}{17} =$ _____ |
| 2. $\frac{3}{16} =$ _____ | 17. $\frac{1}{20} =$ _____ | 32. $\frac{1}{3} =$ _____ |
| 3. $\frac{1}{10} =$ _____ | 18. $\frac{14}{15} =$ _____ | 33. $\frac{2}{19} =$ _____ |
| 4. $\frac{4}{5} =$ _____ | 19. $\frac{2}{5} =$ _____ | 34. $\frac{1}{6} =$ _____ |
| 5. $\frac{1}{17} =$ _____ | 20. $\frac{5}{21} =$ _____ | 35. $\frac{3}{20} =$ _____ |
| 6. $\frac{13}{14} =$ _____ | 21. $\frac{3}{12} =$ _____ | 36. $\frac{11}{20} =$ _____ |
| 7. $\frac{6}{9} =$ _____ | 22. $\frac{6}{7} =$ _____ | 37. $\frac{9}{11} =$ _____ |
| 8. $\frac{1}{9} =$ _____ | 23. $\frac{3}{7} =$ _____ | 38. $\frac{6}{19} =$ _____ |
| 9. $\frac{9}{10} =$ _____ | 24. $\frac{1}{11} =$ _____ | 39. $\frac{7}{11} =$ _____ |
| 10. $\frac{3}{5} =$ _____ | 25. $\frac{1}{8} =$ _____ | 40. $\frac{10}{11} =$ _____ |
| 11. $\frac{5}{14} =$ _____ | 26. $\frac{2}{15} =$ _____ | 41. $\frac{5}{6} =$ _____ |
| 12. $\frac{3}{4} =$ _____ | 27. $\frac{15}{17} =$ _____ | 42. $\frac{7}{16} =$ _____ |
| 13. $\frac{1}{2} =$ _____ | 28. $\frac{3}{13} =$ _____ | 43. $\frac{5}{13} =$ _____ |
| 14. $\frac{6}{16} =$ _____ | 29. $\frac{3}{16} =$ _____ | 44. $\frac{6}{13} =$ _____ |
| 15. $\frac{11}{12} =$ _____ | 30. $\frac{5}{16} =$ _____ | 45. $\frac{8}{9} =$ _____ |

Changing Fractions to Decimals

EXAMPLE

Change the fraction to a decimal. Divide to 3 decimal places. Then round to 2 places.

Hint: Try to simplify the fraction before division.

$$\frac{2}{12} = \frac{1}{6} = 6\overline{)1.000} = 0.166 = 0.17$$

Directions Change these fractions to decimals. Divide to 3 places. Then round to 2 places.

1. $\frac{7}{9} =$ _____

2. $\frac{5}{9} =$ _____

3. $\frac{6}{11} =$ _____

4. $\frac{7}{9} =$ _____

5. $\frac{10}{11} =$ _____

6. $\frac{11}{12} =$ _____

7. $\frac{7}{8} =$ _____

8. $\frac{12}{13} =$ _____

9. $\frac{2}{10} =$ _____

10. $\frac{4}{9} =$ _____

11. $\frac{3}{12} =$ _____

12. $\frac{2}{15} =$ _____

13. $\frac{1}{8} =$ _____

14. $\frac{1}{9} =$ _____

15. $\frac{20}{30} =$ _____

16. $\frac{25}{75} =$ _____

17. $\frac{50}{60} =$ _____

18. $\frac{12}{36} =$ _____

19. $\frac{12}{24} =$ _____

20. $\frac{55}{110} =$ _____

21. $\frac{35}{40} =$ _____

22. $\frac{22}{33} =$ _____

23. $\frac{7}{28} =$ _____

24. $\frac{9}{36} =$ _____

25. $\frac{20}{75} =$ _____

26. $\frac{3}{13} =$ _____

27. $\frac{17}{34} =$ _____

28. $\frac{3}{14} =$ _____

29. $\frac{5}{30} =$ _____

30. $\frac{4}{25} =$ _____

Writing Ratios

EXAMPLE

Show a ratio in its three forms.

$$\frac{1}{2} = 1:2 = 1 \text{ to } 2$$

Directions Express the ratios using the other two forms.

- | | | | |
|---------------------|-------|---------------------|-------|
| 1. $\frac{4}{3}$ | _____ | 11. 23:80 | _____ |
| 2. 4:7 | _____ | 12. 3 to 7 | _____ |
| 3. 9 to 12 | _____ | 13. 4 to 9 | _____ |
| 4. $\frac{5}{8}$ | _____ | 14. 5 to 18 | _____ |
| 5. 12:16 | _____ | 15. 26:27 | _____ |
| 6. 5 to 15 | _____ | 16. 32:42 | _____ |
| 7. $\frac{9}{3}$ | _____ | 17. $\frac{34}{45}$ | _____ |
| 8. $\frac{12}{15}$ | _____ | 18. 2 to 18 | _____ |
| 9. $\frac{16}{17}$ | _____ | 19. 33:34 | _____ |
| 10. $\frac{22}{11}$ | _____ | 20. $\frac{7}{23}$ | _____ |

Directions Count the number of like symbols and write the ratios for each.

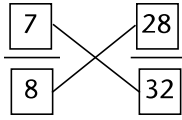
21. Write the ratio of the number of @'s to #'s. _____
22. Write the ratio of the number of @'s to %'s. _____
23. Write the ratio of the number of @'s to \$'s. _____
24. Write the ratio of the number of @'s to *'s. _____
25. Write the ratio of the number of #'s to %'s. _____
26. Write the ratio of the number of #'s to *'s. _____
27. Write the ratio of the number of #'s to @'s. _____
28. Write the ratio of the number of *'s to @'s. _____
29. Write the ratio of the number of *'s to \$'s. _____
30. Write the ratio of the number of %'s to #'s. _____

@ # % \$ # * & \$ \$
@ \$ * & & # @
@ * & * * # @
& # @ \$ \$ \$ \$ #
@ @ \$ % % & * *
& * % % \$ # \$ %
& * & \$ # @ @ #
\$ \$ % % * & * &
* & * & * * * & \$ \$
@ @ # # * *

Proportions

EXAMPLE

Do $\frac{7}{8}$ and $\frac{28}{32}$ form a proportion?



The cross products are both 224. The cross products are equal, so the ratios form a proportion.

$$\frac{7}{8} = \frac{28}{32}$$

$$8 \times 28 \\ 224$$

$$7 \times 32 \\ 224$$

Directions Use cross products to decide if the ratios are equal. Write an equal sign (=) if the ratios form a proportion. Write an inequality symbol (\neq) if the ratios do not form a proportion.

1. $\frac{1}{3}$ $\frac{4}{12}$

14. $\frac{9}{12}$ $\frac{27}{36}$

2. $\frac{15}{80}$ $\frac{4}{75}$

15. $\frac{3}{15}$ $\frac{9}{45}$

3. $\frac{2}{7}$ $\frac{24}{86}$

16. $\frac{72}{54}$ $\frac{9}{7}$

4. $\frac{108}{18}$ $\frac{18}{3}$

17. $\frac{3}{9}$ $\frac{9}{27}$

5. $\frac{5}{25}$ $\frac{25}{150}$

18. $\frac{1}{4}$ $\frac{2}{4}$

6. $\frac{2}{3}$ $\frac{9}{12}$

19. $\frac{1}{3}$ $\frac{5}{6}$

7. $\frac{10}{16}$ $\frac{5}{8}$

20. $\frac{4}{5}$ $\frac{20}{25}$

8. $\frac{7}{8}$ $\frac{15}{16}$

21. $\frac{10}{19}$ $\frac{30}{39}$

9. $\frac{3}{4}$ $\frac{6}{8}$

22. $\frac{3}{6}$ $\frac{5}{10}$

10. $\frac{5}{16}$ $\frac{25}{86}$

23. $\frac{1}{4}$ $\frac{2}{8}$

11. $\frac{96}{180}$ $\frac{16}{30}$

24. $\frac{5}{8}$ $\frac{3}{4}$

12. $\frac{2}{4}$ $\frac{4}{8}$

25. $\frac{2}{7}$ $\frac{24}{84}$

13. $\frac{4}{32}$ $\frac{16}{64}$

Ratios and Proportions

EXAMPLE

14 books to 2 readers

Write the ratio as a fraction. Simplify if necessary.

$$\frac{14}{2} = \frac{7}{1}$$

Directions Write a ratio to compare each of the following. Simplify to lowest terms.

1. 12 music CD's to 4 tapes

2. 10 automobiles to 13 bikes

3. 24 apples to 8 oranges

4. 125 miles to 5 gallons of gas

5. 22 cats to 33 dogs

6. 24 baseballs to 38 players

7. 14 lb of flour to 7 shoppers

8. 8 students to 18 tables

9. 28 TV's to 56 radios

10. 22 planes to 11 trains

EXAMPLE

Cross-multiply. Divide.

$$\frac{72}{n} = \frac{8}{2}$$

$$8n = 72 \times 2 \quad 8n = 144 \quad n = 144 \div 8$$
$$n = 18$$

Directions Solve these proportions using the cross-product method.

Express improper fractions as mixed numbers.

11. $\frac{7}{n} = \frac{14}{10}$

14. $\frac{11}{13} = \frac{n}{39}$

12. $\frac{18}{24} = \frac{2}{n}$

15. $\frac{48}{10} = \frac{n}{5}$

13. $\frac{10}{15} = \frac{25}{n}$

Using Proportions

EXAMPLE

Cross-multiply. Compare products.

$$\begin{array}{ccc} \overset{30}{\frac{2}{3}} & \overset{33}{\frac{11}{15}} & 2 \times 15 = 30 \quad 3 \times 11 = 33 \\ \frac{2}{3} < \frac{11}{15} \end{array}$$

Directions Use cross products and use $<$, $>$, or $=$ for each.

1. $\frac{12}{11}$ $\frac{10}{9}$

3. $\frac{22}{40}$ $\frac{20}{33}$

5. $\frac{8}{9}$ $\frac{13}{15}$

2. $\frac{7}{10}$ $\frac{20}{32}$

4. $\frac{8}{13}$ $\frac{22}{30}$

6. $\frac{15}{21}$ $\frac{17}{18}$

Directions Use the cross-product method to solve for the unknown.

7. $\frac{14}{30} = \frac{n}{90}$

9. $\frac{n}{27} = \frac{6}{9}$

11. $\frac{7}{n} = \frac{28}{56}$

8. $\frac{n}{3} = \frac{25}{12}$

10. $\frac{18}{n} = \frac{3}{12}$

12. $\frac{56}{9} = \frac{n}{4}$

Directions Write and solve proportions using the cross-product method.
Round your answers to the nearest tenths place.

13. Eldo can ride his bike 15 miles in 2 hours. How many miles can he ride in 7 hours?
14. Lacy can in-line skate 9 miles an hour. How many hours will it take her to do 30 miles?
15. Karen and Patrick worked together stringing beads for necklaces. If they can string 50 beads in 9 minutes, how long will it take for them to string 725 beads?

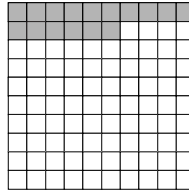
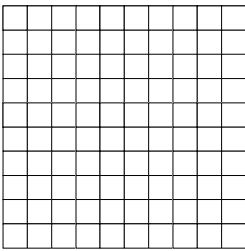
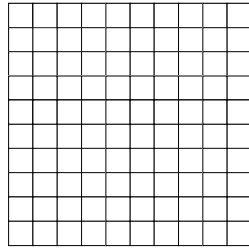
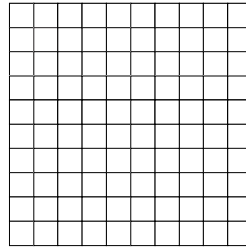
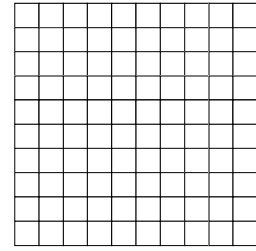
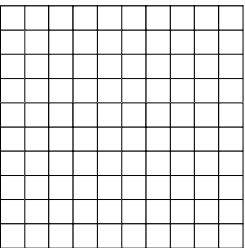
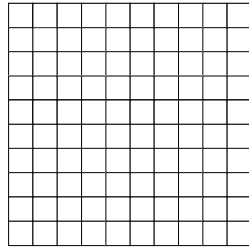
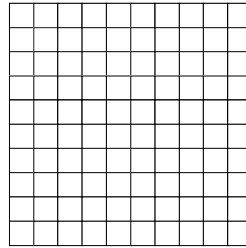
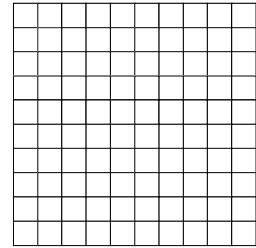
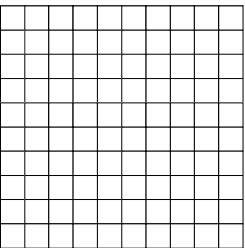
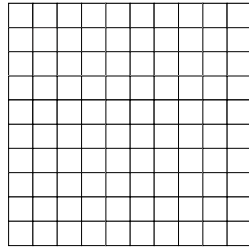
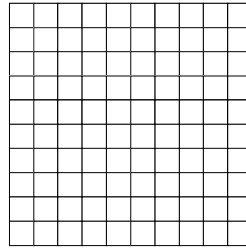
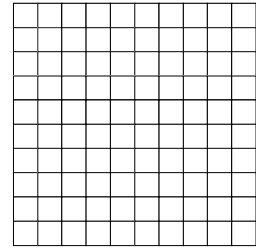
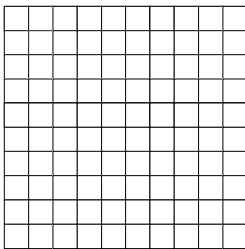
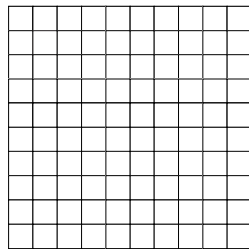
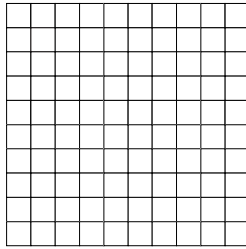
Meaning of Percent

EXAMPLE

Shade the boxes to show percent.

$$16\% = 16 \text{ out of } 100$$

Shade 16 boxes.

**Directions** Shade these percents.**1.** 23%**5.** 33%**9.** 95%**13.** 55%**2.** 75%**6.** 80%**10.** 45%**14.** 12%**3.** 30%**7.** 9%**11.** 60%**15.** 68%**4.** 40%**8.** 17%**12.** 100%

Changing Percents to Decimals and Fractions

EXAMPLES

14% Write as a decimal. Drop percent sign. Add decimal point.
 $14\% = 0.14$

14% Write as a fraction. Drop percent sign.
Write number as a numerator over denominator of 100.
Simplify if necessary.
 $14\% = \frac{14}{100} = \frac{7}{50}$

Directions Write these percents as decimals.

- | | | |
|----------------|-----------------|------------------|
| 1. 17% = _____ | 7. 90% = _____ | 13. 39% = _____ |
| 2. 33% = _____ | 8. 37% = _____ | 14. 66% = _____ |
| 3. 60% = _____ | 9. 55% = _____ | 15. 48% = _____ |
| 4. 22% = _____ | 10. 75% = _____ | 16. 34% = _____ |
| 5. 41% = _____ | 11. 61% = _____ | 17. 100% = _____ |
| 6. 46% = _____ | 12. 80% = _____ | 18. 1% = _____ |

Directions Write these decimals as fractions. Simplify your answers.

- | | | |
|------------------|------------------|------------------|
| 19. 0.37 = _____ | 25. 0.33 = _____ | 31. 0.02 = _____ |
| 20. 0.18 = _____ | 26. 0.09 = _____ | 32. 0.88 = _____ |
| 21. 0.11 = _____ | 27. 0.40 = _____ | 33. 0.25 = _____ |
| 22. 0.05 = _____ | 28. 0.50 = _____ | 34. 0.35 = _____ |
| 23. 0.08 = _____ | 29. 0.68 = _____ | 35. 0.90 = _____ |
| 24. 0.01 = _____ | 30. 0.10 = _____ | 36. 0.55 = _____ |

Directions Write these percents as decimals and fractions.
Simplify your answers.

- | | |
|-----------------|-----------------|
| 37. 24% = _____ | 42. 72% = _____ |
| 38. 30% = _____ | 43. 87% = _____ |
| 39. 23% = _____ | 44. 95% = _____ |
| 40. 33% = _____ | 45. 74% = _____ |
| 41. 70% = _____ | |

Decimals to Percents

EXAMPLE

Rename 0.63 as a percent by moving the decimal point two places to the right and adding the percent symbol.

$$0.63 = 63\%$$

Directions Rewrite each decimal as a percent.

- | | | |
|--------------------|--------------------|--------------------|
| 1. 0.36 = _____ | 21. 0.0045 = _____ | 41. 25.0 = _____ |
| 2. 1.35 = _____ | 22. 0.6031 = _____ | 42. 3.44 = _____ |
| 3. 0.05 = _____ | 23. 5.05 = _____ | 43. 22.332 = _____ |
| 4. 0.6 = _____ | 24. 0.2207 = _____ | 44. 5.556 = _____ |
| 5. 0.78 = _____ | 25. 0.41 = _____ | 45. 2.33 = _____ |
| 6. 0.45 = _____ | 26. 0.2246 = _____ | 46. 0.75 = _____ |
| 7. 0.0088 = _____ | 27. 0.032 = _____ | 47. 15.02 = _____ |
| 8. 0.035 = _____ | 28. 0.01 = _____ | 48. 0.0062 = _____ |
| 9. 0.122 = _____ | 29. 0.1 = _____ | 49. 30.452 = _____ |
| 10. 0.02 = _____ | 30. 0.112 = _____ | 50. 73.1 = _____ |
| 11. 0.4 = _____ | 31. 0.172 = _____ | 51. 33.4 = _____ |
| 12. 0.21 = _____ | 32. 1.75 = _____ | 52. 1.433 = _____ |
| 13. 2.09 = _____ | 33. 2 = _____ | 53. 43.14 = _____ |
| 14. 2.3 = _____ | 34. 62 = _____ | 54. 12.06 = _____ |
| 15. 6.12 = _____ | 35. 4.09 = _____ | 55. 48.045 = _____ |
| 16. 4.5 = _____ | 36. 3.1 = _____ | 56. 2.332 = _____ |
| 17. 0.065 = _____ | 37. 9.21 = _____ | 57. 2.398 = _____ |
| 18. 0.0081 = _____ | 38. 0.155 = _____ | 58. 12.124 = _____ |
| 19. 0.205 = _____ | 39. 80.0 = _____ | 59. 42.46 = _____ |
| 20. 0.244 = _____ | 40. 7.02 = _____ | 60. 0.0056 = _____ |

Major Elements of a Percent Sentence

EXAMPLES

15% of what number is 52?	Rate	Base	Percentage
	15%	n	52
What percent of 22 is 11?	n	22	11

Directions Identify the rate, base, and percentage for the following percent sentences. Use the letter n to represent a missing value.

	Rate	Base	Percentage
1. 56% of 90 is what number?	_____	_____	_____
2. What percent of 50 is 40?	_____	_____	_____
3. What percent of 86 is 43?	_____	_____	_____
4. 88% of 50 is what number?	_____	_____	_____
5. 100% of what number is 176?	_____	_____	_____
6. 200% of 50 is what number?	_____	_____	_____
7. 90% of what number is 64?	_____	_____	_____
8. What percent of 49 is 100?	_____	_____	_____
9. 70% of 50 is what number?	_____	_____	_____
10. 80% of 20 is what number?	_____	_____	_____
11. What percent of 120 is 90?	_____	_____	_____
12. What percent of 48 is 96?	_____	_____	_____
13. 150% of what number is 300?	_____	_____	_____
14. 6% of 33 is what number?	_____	_____	_____
15. 12% of what number is 70?	_____	_____	_____
16. What percent of 200 is 300?	_____	_____	_____
17. What percent of 5 is 30?	_____	_____	_____
18. 9% of 56 is what number?	_____	_____	_____
19. 33% of 129 is what number?	_____	_____	_____
20. 3% of what number is 27?	_____	_____	_____

Find the Percentage

EXAMPLE

8% of 20 is _____

8% of 20 is n

$$0.08 \times 20 = n$$

$$1.6 = n$$

Directions Solve for the percentage.

- | | |
|--------------------------|---------------------------|
| 1. 9% of 50 is _____ | 24. 1.6% of 1.4 is _____ |
| 2. 4% of 53 is _____ | 25. 2.8% of 9.02 is _____ |
| 3. 28% of 4 is _____ | 26. 2.4% of 76 is _____ |
| 4. 6% of 125 is _____ | 27. 5% of 0.083 is _____ |
| 5. 2% of 86 is _____ | 28. 0.6% of 435 is _____ |
| 6. 43% of 14 is _____ | 29. 0.7% of 7.49 is _____ |
| 7. 75% of 92 is _____ | 30. 129% of 4.2 is _____ |
| 8. 21% of 34 is _____ | 31. 0.03% of 141 is _____ |
| 9. 92% of 62 is _____ | 32. 0.8% of 0.2 is _____ |
| 10. 53% of 80 is _____ | 33. 0.82% of 403 is _____ |
| 11. 15% of 28 is _____ | 34. 245% of 2.6 is _____ |
| 12. 92% of 65 is _____ | 35. 10% of 45 is _____ |
| 13. 3% of 2.1 is _____ | 36. 3.4% of 500 is _____ |
| 14. 40% of 3.5 is _____ | 37. 45% of 100 is _____ |
| 15. 7% of 0.7 is _____ | 38. 23.4% of 300 is _____ |
| 16. 6% of 2.3 is _____ | 39. 140% of 62 is _____ |
| 17. 122% of 42 is _____ | 40. 7% of 250 is _____ |
| 18. 136% of 5 is _____ | 41. 0.46% of 746 is _____ |
| 19. 200% of 73 is _____ | 42. 6.5% of 30 is _____ |
| 20. 0.4% of 96 is _____ | 43. 7.9% of 500 is _____ |
| 21. 7.2% of 48 is _____ | 44. 200% of 0.33 is _____ |
| 22. 5.3% of 70 is _____ | 45. 9% of 9 is _____ |
| 23. 0.8% of 245 is _____ | |

Find the Base

EXAMPLE

5% of _____ is 1.4

5% of n is 1.4

$$0.05 \times n = 1.4$$

$$n = 1.4 \div 0.05$$

$$n = 28$$

$$\begin{array}{r} 28 \\ 0.5 \overline{)1.40} \\ \underline{-10} \\ 40 \\ \underline{-40} \\ 0 \end{array}$$

Directions Solve for the base.

1. 5% of _____ is 4.1
2. 2% of _____ is 3.6
3. 6% of _____ is 1.8
4. 3% of _____ is 0.27
5. 7% of _____ is 0.196
6. 4% of _____ is 1.28
7. 50% of _____ is 2.7
8. 35% of _____ is 30.8
9. 6% of _____ is 0.078
10. 8% of _____ is 0.32
11. 2.5% of _____ is 0.15
12. 7.3% of _____ is 2.044
13. 120% of _____ is 50.4
14. 3.4% of _____ is 2.38
15. 9% of _____ is 0.315
16. 5% of _____ is 0.13
17. 5% of _____ is 0.0235
18. 41% of _____ is 0.82
19. 3% of _____ is 0.045
20. 245% of _____ is 191.1
21. 9% of _____ is 0.0594
22. 0.3% of _____ is 0.135
23. 0.75% of _____ is 0.9
24. 0.8% of _____ is 0.4
25. 4% of _____ is 0.0176
26. 0.21% of _____ is 0.0735
27. 150% of _____ is 135
28. 125% of _____ is 62.5
29. 5.2% of _____ is 0.0988
30. 3.4% of _____ is 0.3094
31. 0.5% of _____ is 1.19
32. 0.21% of _____ is 0.0147
33. 0.32% of _____ is 0.32
34. 0.75% of _____ is 7.5
35. 8% of _____ is 0.416
36. 1.4% of _____ is 0.196
37. 6% of _____ is 0.138
38. 5% of _____ is 0.115
39. 120% of _____ is 102
40. 1% of _____ is 0.03
41. 0.9% of _____ is 1.35
42. 6.3% of _____ is 0.252
43. 8% of _____ is 16
44. 4% of _____ is 0.024
45. 1.6% of _____ is 3.376

Find the Rate

EXAMPLE

_____% of 80 is 4.8

 $n\%$ of 80 is 4.8

$$n \times 0.80 = 4.8$$

$$n = 4.8 \div 0.80$$

$$n = 6\%$$

$$\begin{array}{r} 0.80 \overline{)4.8} \\ \underline{4.8} \\ 0 \end{array}$$

or

$$n \times 80 = 4.8$$

$$n = \frac{4.8}{80}$$

$$n = 0.06 = 6\%$$

Directions Solve for the rate.

- | | |
|------------------------------|--------------------------------|
| 1. _____% of 25 is 5 | 24. _____% of 600 is 420 |
| 2. _____% of 35 is 1.05 | 25. _____% of 700 is 9.8 |
| 3. _____% of 70 is 3.5 | 26. _____% of 40 is 0.32 |
| 4. _____% of 30 is 1.8 | 27. _____% of 200 is 0.14 |
| 5. _____% of 80 is 5.6 | 28. _____% of 3,000 is 1.8 |
| 6. _____% of 20 is 1.8 | 29. _____% of 2.5 is 0.9 |
| 7. _____% of 80 is 0.56 | 30. _____% of 4.2 is 0.546 |
| 8. _____% of 200 is 102 | 31. _____% of 4 is 0.12 |
| 9. _____% of 20 is 7 | 32. _____% of 400 is 0.08 |
| 10. _____% of 300 is 45 | 33. _____% of 22 is 56.1 |
| 11. _____% of 100 is 9 | 34. _____% of 30 is 106.5 |
| 12. _____% of 2,000 is 360 | 35. _____% of 80 is 14 |
| 13. _____% of 35 is 2.8 | 36. _____% of 15 is 0.56 |
| 14. _____% of 305 is 48.8 | 37. _____% of 90 is 5.4 |
| 15. _____% of 20 is 30 | 38. _____% of 50 is 100 |
| 16. _____% of 64 is 112 | 39. _____% of 23 is 2.3 |
| 17. _____% of 10.5 is 0.84 | 40. _____% of 120 is 300 |
| 18. _____% of 250 is 70 | 41. _____% of 22 is 0.33 |
| 19. _____% of 38 is 1.14 | 42. _____% of 30 is 2.85 |
| 20. _____% of 72 is 1.08 | 43. _____% of 70 is 4.9 |
| 21. _____% of 206 is 16.48 | 44. _____% of 0.16 is 0.000136 |
| 22. _____% of 500 is 4.5 | 45. _____% of 50 is 9 |
| 23. _____% of 2.06 is 0.1442 | |

Percent Sentences

EXAMPLES

Percentage

$$25\% \text{ of } 80 \text{ is } \underline{\hspace{2cm}}$$

$$25\% \times 80 = n$$

$$0.25 \times 80 = 20$$

Base

$$25\% \text{ of } \underline{\hspace{2cm}} \text{ is } 52$$

$$25\% \times n = 52$$

$$0.25n = 52$$

$$n = 208$$

Rate

$$\underline{\hspace{2cm}}\% \text{ of } 44 \text{ is } 11$$

$$n\% \times 44 = 11$$

$$n \times 0.44 = 11$$

$$n = 11 \div 0.44$$

$$n = 25\%$$

Directions Solve for the percentage.

- | | |
|-----------------------|------------------------|
| 1. 25% of 60 is _____ | 4. 35% of 36 is _____ |
| 2. 82% of 50 is _____ | 5. 92% of 100 is _____ |
| 3. 90% of 60 is _____ | 6. 20% of 30 is _____ |

Directions Solve for the base.

- | | |
|-----------------------|---------------------------|
| 7. 15% of _____ is 9 | 10. 62% of _____ is 10.54 |
| 8. 60% of _____ is 15 | 11. 53% of _____ is 106 |
| 9. 20% of _____ is 8 | 12. 92% of _____ is 23 |

Directions Solve for the rate.

- | | |
|---------------------------|---------------------------|
| 13. _____ % of 9.5 is 7.6 | 16. _____ % of 30 is 21 |
| 14. _____ % of 70 is 21 | 17. _____ % of 80 is 72 |
| 15. _____ % of 45 is 4.05 | 18. _____ % of 26 is 0.65 |

Directions Complete each percent sentence.

- | | |
|-----------------------------|---------------------------|
| 19. _____ % of 2.5 is 0.375 | 23. _____ % of 240 is 192 |
| 20. 5.5% of _____ is 0.2475 | 24. 75% of _____ is 225 |
| 21. 0.5% of 75 is _____ | 25. 10% of _____ is 0.26 |
| 22. 2.8% of _____ is 18.2 | |

Using Proportions

EXAMPLES

Find base.

25% of n is 17.5

$$\frac{25}{100} = \frac{17.5}{n}$$

$$100 \times 17.5 = 25n$$

$$1,750 = 25n$$

$$\frac{1,750}{25} = \frac{25n}{25}$$

$$70 = n$$

Find rate.

 $n\%$ of 40 is 24

$$\frac{n}{100} = \frac{24}{40}$$

$$100 \times 24 = 40n$$

$$2,400 = 40n$$

$$\frac{2,400}{40} = \frac{40n}{40}$$

$$60 = n$$

Find percentage.

7% of 80 is n

$$\frac{7}{100} = \frac{n}{80}$$

$$100n = 7 \times 80$$

$$100n = 560$$

$$\frac{100n}{100} = \frac{560}{100}$$

$$n = 5.6$$

Directions Write proportions and solve for the unknown.

1. 20% of n is 9.6 _____

9. 80% of 40 is n _____

2. $n\%$ of 35 is 5.6 _____

10. 23% of n is 73.6 _____

3. 70% of 32 is n _____

11. $n\%$ of 60 is 24 _____

4. 30% of n is 120 _____

12. 35% of n is 24.5 _____

5. $n\%$ of 50 is 11.5 _____

13. 18% of 350 is n _____

6. 85% of 36 is n _____

14. $n\%$ of 29 is 2.03 _____

7. 90% of n is 270 _____

15. 9% of n is 4.68 _____

8. $n\%$ of 97 is 48.5 _____

Discount

EXAMPLES

Find the sale price of a music CD that lists for \$18.50, if the discount rate is 20%.

$$\begin{array}{r} \text{Step 1} \quad \$18.50 \text{ list price} \\ \quad \times \quad .20 \\ \hline \quad \quad \$3.70 \text{ discount} \end{array}$$

$$\begin{array}{r} \text{Step 2} \quad \$18.50 \text{ list price} \\ \quad - \quad 3.70 \text{ discount} \\ \hline \quad \quad \$14.80 \text{ price after discount} \end{array}$$

Find the discount rate if a \$25.00 DVD is on sale for \$21.25.

$$\begin{array}{r} \text{Step 1} \quad \$25.00 \text{ list price} \\ \quad - \quad 21.25 \text{ discount price} \\ \hline \quad \quad \$3.75 \text{ discount} \end{array}$$

$$\begin{array}{r} \quad \quad .15 = 15\% \text{ discount rate} \\ 25 \overline{)3.75} \\ \quad - \quad 25 \\ \hline \quad \quad 125 \\ \quad - \quad 125 \\ \hline \end{array}$$

Directions Solve these discount problems. When necessary round answers to the nearest cent.

1. \$175.00 list price
10% discount rate
Discount _____
Sale price _____

5. Computer list price \$950.00
Discount rate 10%
Discount _____
Sale price _____

8. Disk drive list price \$150.00
Discount rate 20%
Discount _____
Sale price _____

2. \$80.00 list price
20% discount rate
Discount _____
Sale price _____

6. Radio list price \$75.00
Discount rate 15%
Discount _____
Sale price _____

9. Television list price \$395.00
Discount rate 10%
Discount _____
Sale price _____

3. CD list price \$22.00
15% discount rate
Discount _____
Sale price _____

7. Stereo list price \$150.00
Sale price \$120.00
Discount _____
Discount rate _____

10. Jeans list price \$34.95
Discount rate 10%
Discount _____
Sale price _____

4. Videotape list price \$50.00
Sale price \$20.00
Discount _____
Discount rate _____

Sales Tax

EXAMPLE

Compute 6% sales tax on \$13.05

$$\begin{array}{r}
 \$13.05 \text{ cost before tax} \\
 \times \quad .06 \text{ tax rate} \\
 \hline
 0.7830 \\
 0.79 \leftarrow \text{Tax always rounds up.} \\
 \text{The tax is } \$0.79 \text{ or } 79 \text{ cents.}
 \end{array}$$

Directions Compute sales tax.

- | | | |
|-------------------------------|----------------------------------|--------------------------------|
| 1. \$2.75 at 5% _____ | 4. \$120.00 at 5% _____ | 7. \$100.00 at 6% _____ |
| 2. \$6.15 at 7% _____ | 5. \$1,200.00 at 6% _____ | 8. \$30.10 at 7% _____ |
| 3. \$24.95 at 7% _____ | 6. \$16.75 at 6% _____ | 9. \$0.45 at 5% _____ |

Directions Compute sales tax and total cost.

- 10.**
- A book for \$17.95

6% tax rate

Tax _____

Cost plus tax _____

- 13.**
- Table for \$98.00

5% tax rate

Tax _____

Cost plus tax _____

- 11.**
- Clock for \$75.00

5% tax rate

Tax _____

Cost plus tax _____

- 14.**
- Used car for \$11,960.00

6% tax rate

Tax _____

Cost plus tax _____

- 12.**
- Television for \$299.99

7% tax rate

Tax _____

Cost plus tax _____

- 15.**
- Electric stove for \$699.00

5% tax rate

Tax _____

Cost plus tax _____

Simple Interest

EXAMPLE

Compute the simple interest on a principal of \$125.00 at an interest rate of 7% for 3 years.

$$\begin{array}{r} \$125.00 \text{ principal} \\ \times .07 \\ \hline \end{array}$$

$$\times .07$$

$$\$8.7500 \text{ interest for one year}$$

$$\begin{array}{r} \$8.75 \text{ interest for one year} \\ \times 3 \text{ for 3 years} \\ \hline \end{array}$$

$$\times 3$$

$$\$26.25 \text{ interest for 3 years}$$

Compute the simple interest on \$200.00 at a rate of 6% for 9 months.

$$\begin{array}{r} \$200.00 \text{ principal} \\ \times .06 \\ \hline \end{array}$$

$$\times .06$$

$$\$12.00 \text{ interest for 1 year}$$

$$\frac{\$12}{1} \times \frac{9}{12}$$

$$\frac{12}{1} \times \frac{3}{4} = \frac{36}{4} = 9$$

← Write 9 months over 12 months to express time as years.

\$9.00 is the interest for 9 months.

Directions Compute the simple interest.

1. Compute the simple interest for \$750.00 at 7% for 5 years. _____
2. Compute the simple interest for \$800.00 at 6% for 6 months. _____
3. Compute the simple interest for \$1,200.00 at 9% for 10 years. _____
4. Compute the simple interest for \$5,000.00 at 10% for 5 years. _____
5. Compute the simple interest for \$6,200.00 at 8% for 10 years. _____
6. Compute the simple interest for \$150.00 at 5% for 11 years. _____
7. Compute the simple interest for \$48.00 at 5% for 6 months. _____
8. Compute the simple interest for \$4,500.00 at 7% for 9 months. _____
9. Compute the simple interest for \$395.00 at 3% for 24 months. _____
10. Compute the simple interest for \$245.00 at 5% for 7 years. _____

Installment Buying

EXAMPLE

Find the finance charge and balance with a 2% finance rate for \$400.00.

Step 1	\$400.00	previous balance	Step 2	\$400.00	previous balance
	× .02	finance rate		+ 8.00	finance charge
	\$8.0000	finance charge		\$408.00	

Step 3	\$408.00	
	– 25.00	first month's payment
	\$383.00	new balance

New balance before first payment

Directions Complete the installment chart for a TV that cost \$400.00. The monthly payments will be \$25.00 and a 2% finance charge will be added to the unpaid balance.

Month	Previous Balance	Finance Charge	Before Payment	Monthly Payment	New Balance
June	\$400.00	\$8.00	\$408.00	\$25.00	\$383.00
July	\$383.00				
August					
September					
October					

Directions Complete the installment chart for a TV that cost \$400.00 with a 1% finance charge added to the unpaid balance. The monthly payments are \$25.00.

Month	Previous Balance	Finance Charge	Before Payment	Monthly Payment	New Balance
June					
July					
August					
September					
October					

Commission

EXAMPLE

Compute the commission for a real estate agent who sells a house for \$95,000 and the commission rate is 3%.

$$\begin{array}{r} \$95,000.00 \text{ sale price} \\ \times \quad .03 \text{ commission rate} \\ \hline \$2,850.00 \text{ commission} \end{array}$$

Directions Compute the following sales commissions.

1. Amount is \$4,500.00

Commission rate 5%

Commission _____

6. Amount is \$1,600.00

Commission rate 3%

Commission _____

11. Amount is \$560.00

Commission rate 5%

Commission _____

2. Amount is \$48,000.00

Commission rate 3%

Commission _____

7. Amount is \$450.00

Commission rate 5%

Commission _____

12. Amount is \$880.00

Commission rate 4%

Commission _____

3. Amount is \$3,400.00

Commission rate 3%

Commission _____

8. Amount is \$1,700.00

Commission rate 4%

Commission _____

13. Amount is \$234.00

Commission rate 11%

Commission _____

4. Amount is \$500.00

Commission rate 5%

Commission _____

9. Amount is \$3,400.00

Commission rate 5%

Commission _____

14. Amount is \$911.00

Commission rate 4%

Commission _____

5. Amount is \$1,000.00

Commission rate 3%

Commission _____

10. Amount is \$950.00

Commission rate 10%

Commission _____

15. Amount is \$260.00

Commission rate 9%

Commission _____

Tips

EXAMPLE

Compute a 15% tip on a meal that costs \$23.50.

$$\begin{array}{r} \$23.50 \text{ meal cost} \\ \times .15 \text{ tip rate} \\ \hline 11750 \\ 2350 \\ \hline \end{array}$$

\$3.5250 round to nearest cent

\$3.53 rounded to nearest cent

$$\begin{array}{r} \$23.50 \text{ meal cost} \\ \times 3.53 \text{ tip} \\ \hline \$27.03 \text{ total} \end{array}$$

Directions Compute the tip for each meal. Use 15% as a tip rate for each meal.

1. Meal cost \$20.00

Tip _____

Meal total _____

4. Meal cost \$25.00

Tip _____

Meal total _____

7. Meal cost \$5.50

Tip _____

Meal total _____

2. Meal cost \$27.20

Tip _____

Meal total _____

5. Meal cost \$45.20

Tip _____

Meal total _____

8. Meal cost \$11.90

Tip _____

Meal total _____

3. Meal cost \$37.00

Tip _____

Meal total _____

6. Meal cost \$18.00

Tip _____

Meal total _____

9. Meal cost \$4.50

Tip _____

Meal total _____

Directions Compute the tip for each meal and round to the nearest dollar.

10. Meal cost \$4.60

Tip _____

Meal total _____

12. Meal cost \$11.90

Tip _____

Meal total _____

14. Meal cost \$5.50

Tip _____

Meal total _____

11. Meal cost \$15.50

Tip _____

Meal total _____

13. Meal cost \$14.70

Tip _____

Meal total _____

15. Meal cost \$7.95

Tip _____

Meal total _____

Points, Lines, and Angles

EXAMPLE

Make a construction to represent \overrightarrow{AB} .



Rays can be drawn from either direction.
The beginning point must be A as indicated \overrightarrow{AB} .

Directions Use the baseline provided to construct the following geometric constructions.

1. \overrightarrow{BA} _____

6. Vertex G _____

2. $\angle ABC$ _____

7. Vertex H _____

3. $\angle XYZ$ _____

8. \overleftrightarrow{RT} _____

4. \overrightarrow{AD} _____

9. point B _____

5. \overline{DZ} _____

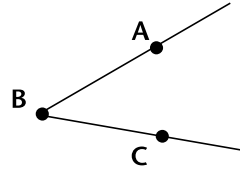
10. $\angle QRS$ _____

Identifying Angles

EXAMPLE

Construct an acute angle.

$\angle ABC$ is acute because $\angle B$ is less than 90 degrees.



Directions Construct these angles on the baselines given.

1. acute

4. reflex

2. straight

5. right

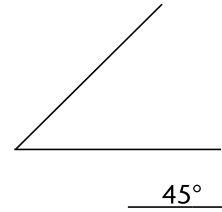
3. obtuse

Measuring Angles

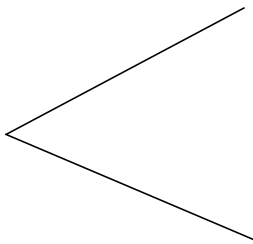
EXAMPLE

Place protractor on the angle so that the center is on the angle's vertex and the baseline is on one of the rays.

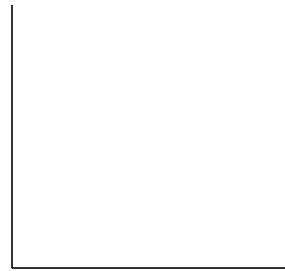
Make sure second ray crosses the scale. Read the scale.



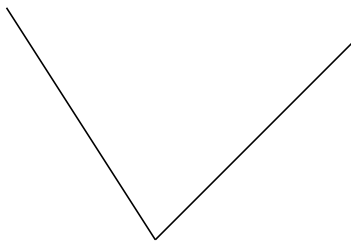
Directions Use a protractor to measure these angles to the nearest degree.
If necessary, use a straightedge to extend the sides of the angle.



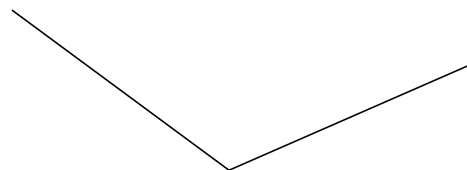
1. _____



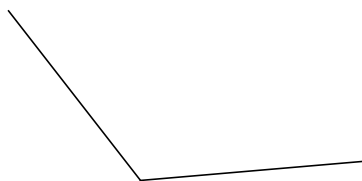
4. _____



2. _____



5. _____



3. _____

Polygons

EXAMPLE

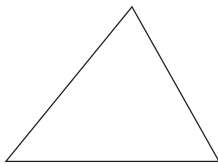
Count the number of sides. Name the polygon.



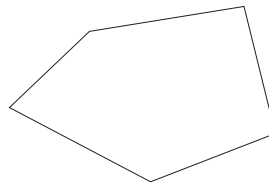
_____ quadrilateral

Directions Count the number of sides for each polygon. Use the chart to classify each polygon.

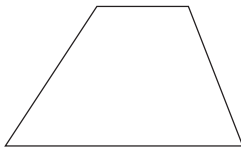
1.



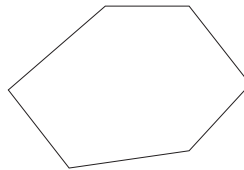
5.



2.



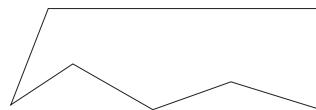
6.



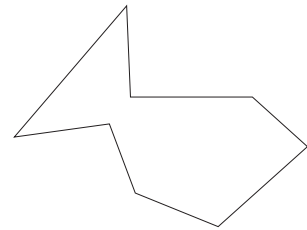
3.



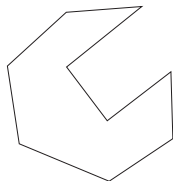
7.



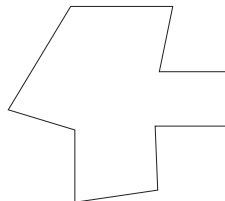
9.



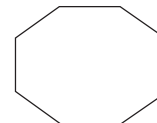
4.



8.



10.



Number of Sides	Name of Polygon
3	triangle
4	quadrilateral
5	pentagon
6	hexagon
7	heptagon
8	octagon
9	nonagon
10	decagon
12	dodecagon

Solid Figures

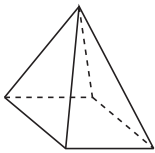
EXAMPLE

Look at the solid figure. Identify it.

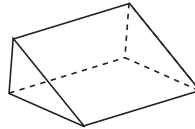
_____ cone _____

**Directions** Identify these solid figures.

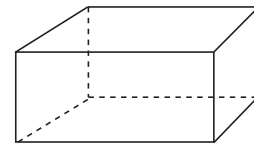
1.



5.



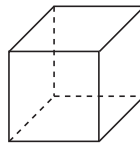
9.



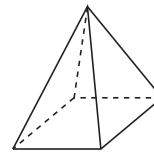
2.



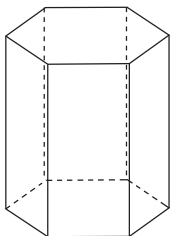
6.



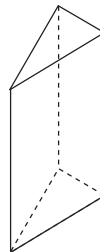
10.



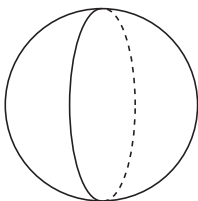
3.



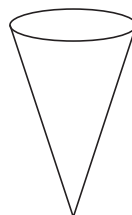
7.



4.



8.



Units of Measurement

EXAMPLE

Circle the letter of the best answer. Think about the meaning of the prefix. Convert from one unit of measurement to the other.

4 centimeters

- A** 0.004 meter
B 0.04 meter
C 0.40 meter
D 4 meter

Centi means one-hundredth. 4 centimeters is 4 one-hundredths, or 0.04, meters.

Directions Circle the letter of the best answer.

- 3 millimeters
 - 3 meters
 - 30 meters
 - 0.03 meters
 - 0.003 meters
- 7 kilometers
 - 70 meters
 - 700 meters
 - 7,000 meters
 - 0.007 meters
- 8 centimeters
 - 0.08 meters
 - 0.8 meters
 - 80 meters
 - 8 meters
- 9 dekameters
 - 9 meters
 - 90 meters
 - 0.09 meters
 - 900 meters
- 4 hectometers
 - 40 meters
 - 0.04 meters
 - 0.004 meters
 - 400 meters

Prefix	Value	Symbol	Example
kilo	one thousand	k	kilometer
hecto	one hundred	h	hectometer
deka	ten	da	dekagram
deci	one-tenth	d	decimeter
centi	one-hundredth	c	centigram
milli	one-thousandth	m	milliliter

Sometimes **deka** is spelled **deca**.

- 3 decimeters
 - 3 meters
 - 0.3 meters
 - 0.03 meters
 - 30 meters
- 7 decimeters
 - 0.7 meters
 - 0.07 meters
 - 70 meters
 - 700 meters
- 19 kilometers
 - 190 meters
 - 0.0019 meters
 - 1,900 meters
 - 19,000 meters
- 3,000 millimeters
 - 300 meters
 - 30 meters
 - 3 meters
 - 0.03 meters
- 27 centimeters
 - 2.7 meters
 - 0.27 meters
 - 0.027 meters
 - 27 meters

Using the Metric System

EXAMPLE

Use a metric ruler to measure the line to the nearest millimeter.

Give your answer in centimeters and millimeters.

7 cm 4 mm

Directions Measure these line segments using the metric system.
Measure to the nearest millimeter. Write your answers on the line.

1. _____

2. _____

3. _____

4. _____

5. _____

6. _____

7. _____

8. _____

9. _____

10. _____

11. _____

12. _____

13. _____

14. _____

15. _____

Converting Units

EXAMPLES

$$4.5 \text{ m} = \frac{450}{2 \text{ places}} \text{ cm}$$

$$\text{km } \underline{3} \text{ m } \underline{2} \text{ cm } \underline{1} \text{ mm}$$

$$6.2 \text{ cm} = \frac{0.000062}{5 \text{ places}} \text{ km}$$

$$\text{km } \underline{3} \text{ m } \underline{2} \text{ cm } \underline{1} \text{ mm}$$

The decimal has moved 5 places to the left. Also note that the arrow has moved under the 2 and the 3. $2 + 3 = 5$
Move the decimal 5 places in the direction of the arrow.

Directions Make the following conversions.

1. $5 \text{ m} = \underline{\hspace{2cm}} \text{ mm}$

2. $2 \text{ cm} = \underline{\hspace{2cm}} \text{ mm}$

3. $12 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

4. $9 \text{ cm} = \underline{\hspace{2cm}} \text{ m}$

5. $2.3 \text{ cm} = \underline{\hspace{2cm}} \text{ m}$

6. $3.44 \text{ km} = \underline{\hspace{2cm}} \text{ cm}$

7. $19 \text{ mm} = \underline{\hspace{2cm}} \text{ cm}$

8. $7.1 \text{ cm} = \underline{\hspace{2cm}} \text{ km}$

9. $2 \text{ cm} = \underline{\hspace{2cm}} \text{ m}$

10. $0.04 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

1 kilometer = 1,000 meters

1 meter = 100 centimeters

1 meter = 1,000 millimeters

1 centimeter = 10 millimeters

11. $29,000 \text{ mm} = \underline{\hspace{2cm}} \text{ m}$

12. $9,000,000 \text{ mm} = \underline{\hspace{2cm}} \text{ km}$

13. $0.0003 \text{ cm} = \underline{\hspace{2cm}} \text{ km}$

14. $0.004 \text{ cm} = \underline{\hspace{2cm}} \text{ mm}$

15. $82 \text{ mm} = \underline{\hspace{2cm}} \text{ m}$

Working with Measurements of Length

EXAMPLE

Add. Convert meters to centimeters.

$$2 \text{ m} + 350 \text{ cm}$$

$$200 \text{ m} + 350 \text{ cm} = 550 \text{ cm}$$

Directions Use the charts to help make these conversions.

km <u> 3 </u> m <u> 2 </u> cm <u> 1 </u> mm

1. $234 \text{ mm} = \underline{\hspace{2cm}}$ cm

2. $82 \text{ m} = \underline{\hspace{2cm}}$ km

3. $3.4 \text{ mm} = \underline{\hspace{2cm}}$ m

4. $5 \text{ km} = \underline{\hspace{2cm}}$ cm

5. $35 \text{ cm} = \underline{\hspace{2cm}}$ mm

6. $87 \text{ mm} = \underline{\hspace{2cm}}$ km

7. $3.2 \text{ cm} = \underline{\hspace{2cm}}$ mm

8. $0.24 \text{ km} = \underline{\hspace{2cm}}$ m

1 kilometer = 1,000 meters

1 meter = 100 centimeters

1 meter = 1,000 millimeters

1 centimeter = 10 millimeters

9. $0.7 \text{ mm} = \underline{\hspace{2cm}}$ cm

10. $0.001 \text{ km} = \underline{\hspace{2cm}}$ m

11. $15 \text{ cm} = \underline{\hspace{2cm}}$ m

12. $0.02 \text{ m} = \underline{\hspace{2cm}}$ cm

Directions Find the answers to these addition problems.

13. $34 \text{ cm} + 4.9 \text{ cm} + 7 \text{ cm} = \underline{\hspace{2cm}}$ cm

20. $1 \text{ cm} + 1 \text{ m} = \underline{\hspace{2cm}}$ m

14. $9 \text{ mm} + 22 \text{ mm} = \underline{\hspace{2cm}}$ mm

21. $9 \text{ mm} + 30 \text{ mm} + 1.1 \text{ cm} = \underline{\hspace{2cm}}$ mm

15. $66 \text{ m} + 120 \text{ cm} + 10 \text{ m} = \underline{\hspace{2cm}}$ m

22. $8 \text{ km} + 2,031 \text{ m} = \underline{\hspace{2cm}}$ km

16. $4 \text{ km} + 5 \text{ m} + 120 \text{ cm} = \underline{\hspace{2cm}}$ m

23. $30 \text{ m} + 20 \text{ cm} = \underline{\hspace{2cm}}$ km

17. $3.4 \text{ cm} + 12 \text{ mm} + 4 \text{ mm} = \underline{\hspace{2cm}}$ mm

24. $0.003 \text{ km} + 2 \text{ m} = \underline{\hspace{2cm}}$ cm

18. $2 \text{ km} + 23 \text{ m} + 300 \text{ cm} = \underline{\hspace{2cm}}$ m

25. $4 \text{ mm} + 30 \text{ cm} = \underline{\hspace{2cm}}$ mm

19. $4 \text{ m} + 34 \text{ m} + 0.005 \text{ km} = \underline{\hspace{2cm}}$ m



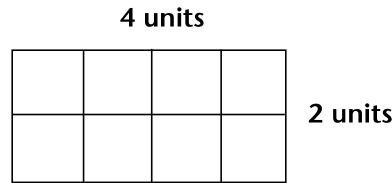
Computing Area of a Rectangle

EXAMPLE

$$\text{Area} = \text{length} \times \text{width}$$

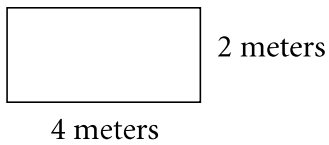
$$\text{Area} = 4 \text{ units} \times 2 \text{ units}$$

$$\text{Area} = 8 \text{ square units}$$

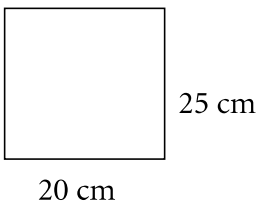


Directions Solve for the area of these rectangles.

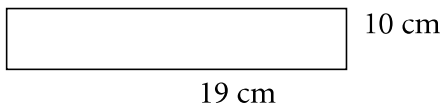
1.



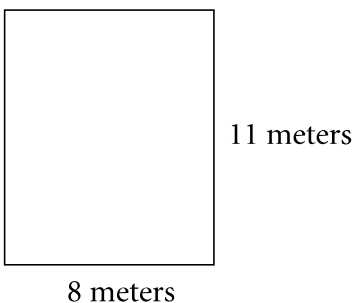
2.



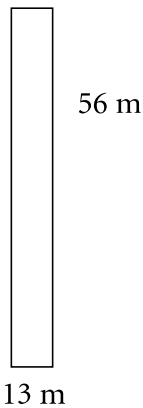
3.



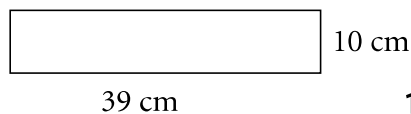
4.



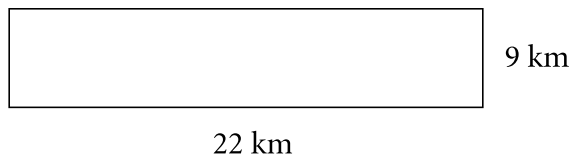
5.



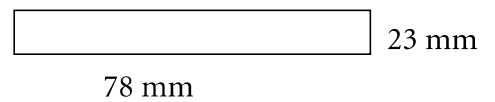
6.



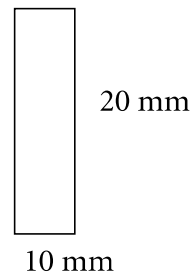
7.



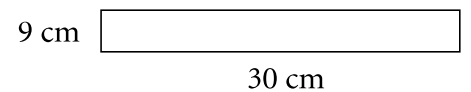
8.



9.



10.



Computing Volume

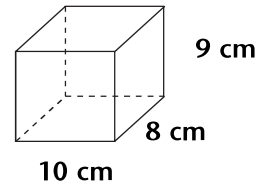
EXAMPLE

Compute the volume for this rectangular prism.

$$\text{Volume} = \text{length} \times \text{width} \times \text{height}$$

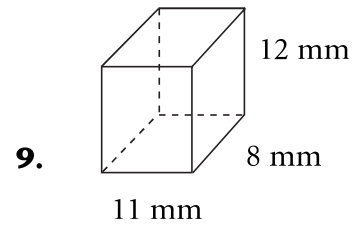
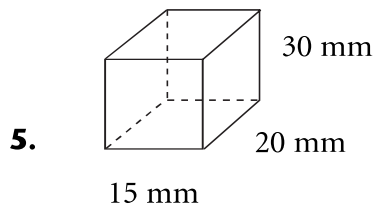
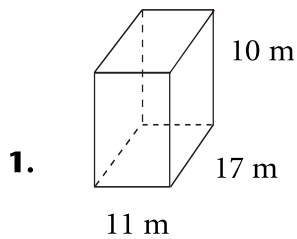
$$\text{Volume} = 10 \text{ cm} \times 8 \text{ cm} \times 9 \text{ cm}$$

$$\text{Volume} = 720 \text{ cubic cm}$$



All volume measurements are expressed in cubic units.

Directions Compute the volumes.



2. length = 1 km
width = 2 km
height = 5 km

6. length = 12 cm
width = 20 cm
height = 6 cm

10. length = 45 cm
width = 17 cm
height = 10 cm

3. length = 13 cm
width = 8 cm
height = 20 cm

7. length = 100 m
width = 100 m
height = 10 m

4. length = 22 km
width = 22 km
height = 10 km

8. length = 25 km
width = 20 km
height = 40 km

Capacity

EXAMPLE

Capacity is the amount a container will hold when full.

Liter is L. The L is always capitalized in abbreviations.

Centiliter is cL, kiloliter is kL, and milliliter is mL.

$$15 \text{ L} = \underline{\hspace{2cm}} \text{ cL}$$

$$1 \text{ L} = 100 \text{ cL, so}$$

$$15 \text{ L} = 1,500 \text{ cL}$$

$$1 \text{ kiloliter} = 1,000 \text{ liters}$$

$$1 \text{ liter} = 100 \text{ centiliters}$$

$$1 \text{ centiliter} = 10 \text{ milliliters}$$

Directions Choose the proper unit of measure for each of these examples.

1. a large container of milk

2. the amount of water in a swimming pool

3. the amount of cream in a bowl

4. milk shake in a paper cup

5. trunk space of a large car

6. automobile gas tank

7. the amount of salt needed

8. a bottle of perfume

9. a thimble full of water

10. a bathtub full of water

Directions Make these conversions using the table.

11. 2 kiloliters = _____ liters

16. 200 centiliters = _____ milliliters

12. 2,000 liters = _____ kiloliters

17. 1 kL = _____ L

13. 300 milliliters = _____ cL

18. 30 mL = _____ centiliters

14. 400 mL = _____ liters

19. 10 L = _____ cL

15. 9 kL = _____ L

20. 40 cL = _____ mL



Units of Capacity

EXAMPLE

 kL 3 L 2 cL 1 mL

$$2,200 \text{ mL} = \underline{\quad} \text{ L}$$

$$1,000 \text{ mL} = 1 \text{ L, so}$$

$$2,200 \text{ mL} = \underline{2.2} \text{ L}$$

1 kiloliter = 1,000 liters
1 liter = 100 centiliters
1 centiliter = 10 milliliters
1 liter = 1,000 milliliters

Directions Use these charts to help determine the correct conversion.

1. $4,500 \text{ mL} = \underline{\quad\quad\quad} \text{ L}$

4. $3.6 \text{ L} = \underline{\quad\quad\quad} \text{ kL}$

2. $0.00012 \text{ kL} = \underline{\quad\quad\quad} \text{ L}$

5. $0.091 \text{ mL} = \underline{\quad\quad\quad} \text{ cL}$

3. $2.3 \text{ L} = \underline{\quad\quad\quad} \text{ mL}$

6. $7 \text{ mL} = \underline{\quad\quad\quad} \text{ L}$

Directions Solve for the volumes.

7. length = 2 mm

width = 3 mm

height = 4 mm

volume = $\underline{\quad\quad\quad} \text{ mm}^3$

10. length = 1 m

width = 1 m

height = 50 cm

volume = $\underline{\quad\quad\quad} \text{ cm}^3$

13. length = 3 km

width = 10 km

height = 1 km

volume = $\underline{\quad\quad\quad} \text{ km}^3$

8. length = 8 cm

width = 5 cm

height = 9 cm

volume = $\underline{\quad\quad\quad} \text{ cm}^3$

11. length = 4 mm

width = 20 mm

height = 1 cm

volume = $\underline{\quad\quad\quad} \text{ mm}^3$

14. length = 90 cm

width = 300 cm

height = 1 m

volume = $\underline{\quad\quad\quad} \text{ cm}^3$

9. length = 12 m

width = 4 m

height = 1 m

volume = $\underline{\quad\quad\quad} \text{ m}^3$

12. length = 2.3 cm

width = 100 cm

height = 20 mm

volume = $\underline{\quad\quad\quad} \text{ cm}^3$

15. length = 45 mm

width = 2 cm

height = 20 cm

volume = $\underline{\quad\quad\quad} \text{ cm}^3$



Mass

EXAMPLE

Circle the best measurement.

a bag of flour

mg g

 kg

A bag of flour weighs more than 1,000 grams, so use kilograms to measure its mass.

Directions Choose the best measurement for each of these items.
Circle your answer.

- | | | |
|---|---|---|
| 1. a pencil
mg g kg | 11. a toothpick
mg g kg | 21. a large turkey
mg g kg |
| 2. a grape
mg g kg | 12. one large steak
mg g kg | 22. a ballpoint pen
mg g kg |
| 3. a sunflower seed
mg g kg | 13. a large cow
mg g kg | 23. a plate full of chicken
mg g kg |
| 4. a small child
mg g kg | 14. a small cow
mg g kg | 24. one large shoe
mg g kg |
| 5. an automobile
mg g kg | 15. a sheep
mg g kg | 25. one carrot
mg g kg |
| 6. a soup bowl
mg g kg | 16. a 17-inch TV
mg g kg | 26. an egg sandwich
mg g kg |
| 7. a textbook
mg g kg | 17. a sandwich
mg g kg | 27. a bike
mg g kg |
| 8. a tube of toothpaste
mg g kg | 18. a tomato
mg g kg | 28. one peanut
mg g kg |
| 9. a box of cereal
mg g kg | 19. a can of soup
mg g kg | 29. one grain of salt
mg g kg |
| 10. an apple
mg g kg | 20. a kitchen table
mg g kg | 30. a train
mg g kg |

Working with Units of Mass

EXAMPLE

3,400 grams _____ kilograms

 kg 3 g 2 cg 1 mg
 ←

Step 1 Draw a line from g to kg.

Step 2 The line moves to the left as it passes the 3.

 3,400 grams Move the decimal 3 places to the left.
 ←

 3,400 grams 3.4 kilograms

Directions Use the chart to help make the conversions.

1. 23 mg = _____ g

2. 31 mg = _____ g

3. 32 g = _____ kg

4. 120 cg = _____ g

5. 13 kg = _____ cg

6. 350 kg = _____ g

7. 100 mg = _____ g

8. 300 mg = _____ cg

9. 240 cg = _____ g

1 kilogram = 1,000 grams 1 gram = 100 centigrams 1 centigram = 10 milligrams 1 gram = 1,000 milligrams

10. 1 kg = _____ cg

11. 1,000 cg = _____ g

12. 300 g = _____ kg

13. 20 g = _____ cg

14. 50 mg = _____ kg

15. 1,500 g = _____ kg

Liquid Capacity

EXAMPLES

If necessary, change the units to intermediate units first.

10 quarts = _____ fluid ounces

Write this:

10 quarts = 20 pints = 320 fluid ounces

6 pints = 96 fluid ounces

Multiply. $6 \times 16 = 96$

Commonly Used Measurements

1 pint = 16 fluid ounces

1 quart = 2 pints

1 quart = 32 fluid ounces

1 gallon = 4 quarts

Directions Make these conversions. Multiply when you are converting from large to smaller units.

1. 2 quarts = _____ pints

8. 10 gallons = _____ quarts

2. 4 quarts = _____ pints

9. 20 quarts = _____ pints

3. 4 gallons = _____ quarts

10. 13 quarts = _____ pints

4. 3 pints = _____ fluid ounces

11. 20 quarts = _____ fluid ounces

5. 5 quarts = _____ pints

12. 3 gallons = _____ pints

6. 2 gallons = _____ quarts

13. 4 quarts = _____ fluid ounces

7. 5 pints = _____ fluid ounces

Directions Make these conversions. Divide when you are converting from small to larger units. If necessary express answers as mixed numbers.

14. 40 pints = _____ quarts

20. 12 pints = _____ quarts

15. 14 quarts = _____ gallons

21. 34 quarts = _____ gallons

16. 48 fluid ounces = _____ pints

22. 45 fluid ounces = _____ pints

17. 22 pints = _____ quarts

23. 80 quarts = _____ gallons

18. 32 pints = _____ quarts

24. 56 fluid ounces = _____ pints

19. 30 quarts = _____ gallons

25. 23 pints = _____ quarts



Converting Units of Weight

EXAMPLES

Multiply or divide to convert units.

$$2 \text{ tons} = \underline{\hspace{2cm}} \text{ pounds}$$

$$2 \times 2,000 = 4,000 \text{ pounds}$$

$$3,000 \text{ pounds} = \underline{\hspace{2cm}} \text{ tons}$$

$$3,000 \div 2,000 = 1 \frac{1}{2} \text{ tons}$$

Commonly Used Measurements

$$1 \text{ pound} = 16 \text{ ounces}$$

$$1 \text{ ton} = 2,000 \text{ pounds}$$

Directions Multiply to convert large units to smaller units.

1. 3 tons = _____ pounds

8. 32 pounds = _____ ounces

2. 5.5 pounds = _____ ounces

9. 5 tons = _____ ounces

3. 10 pounds = _____ ounces

10. 11 pounds = _____ ounces

4. 7 tons = _____ pounds

11. 15 tons = _____ pounds

5. 7 pounds = _____ ounces

12. 2.5 pounds = _____ ounces

6. 4.5 tons = _____ pounds

13. 1.5 pounds = _____ ounces

7. 2.5 pounds = _____ ounces

14. 1.5 tons = _____ pounds

Directions Divide to convert small units to larger units. Some remainders may be expressed as fractions.

15. 40,000 pounds = _____ tons

21. 100 ounces = _____ pounds

16. 48 ounces = _____ pounds

22. 4,500 pounds = _____ tons

17. 64,000 ounces = _____ pounds

23. 35,000 pounds = _____ tons

18. 32 ounces = _____ pounds

24. 4,600 pounds = _____ tons

19. 21,000 pounds = _____ tons

25. 8,800 pounds = _____ tons

20. 550 ounces = _____ pounds



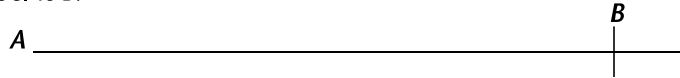
Measuring Lengths

EXAMPLE

Use a ruler to measure the length.

Draw a vertical rule. Label it B .

$$\overline{AB} = 3 \text{ inches}$$



Directions Use a ruler to mark the following measurements. Begin the measured line with point A ending with point B .

1. $\overline{AB} = 2$ inches A _____
2. $\overline{AB} = 3.5$ inches A _____
3. $\overline{AB} = 2\frac{1}{2}$ inches A _____
4. $\overline{AB} = 4$ inches A _____
5. $\overline{AB} = 2\frac{1}{8}$ inches A _____
6. $\overline{AB} = 3\frac{1}{4}$ inches A _____
7. $\overline{AB} = 3.75$ inches A _____
8. $\overline{AB} = 1\frac{1}{4}$ inches A _____
9. $\overline{AB} = 1\frac{1}{2}$ inches A _____
10. $\overline{AB} = 1\frac{7}{8}$ inches A _____
11. $\overline{AB} = 2\frac{4}{8}$ inches A _____
12. $\overline{AB} = 1\frac{15}{16}$ inches A _____
13. $\overline{AB} = 4.5$ inches A _____
14. $\overline{AB} = 2\frac{5}{8}$ inches A _____

Directions Measure the lengths of these lines to the nearest $\frac{1}{4}$ inch.

15. _____
16. _____
17. _____
18. _____
19. _____
20. _____

Length and Distances

EXAMPLES

Use the chart below to make conversions.

$$4 \text{ feet} = \underline{\hspace{2cm}} \text{ inches}$$

$$4 \times 12 = 48$$

$$\swarrow \quad \searrow$$

$$12 \text{ inches} = 1 \text{ foot}$$

$$4 \text{ feet} = \underline{48} \text{ inches}$$

$$120 \text{ inches} = \underline{\hspace{2cm}} \text{ feet}$$

$$120 \div 12 = 10$$

$$\swarrow \quad \searrow$$

$$12 \text{ inches} = 1 \text{ foot}$$

$$120 \text{ inches} = \underline{10} \text{ feet}$$

Directions Use the chart and multiply to make these conversions.

1. 5 feet = _____ inches

2. 5 yards = _____ feet

3. 2 miles = _____ feet

4. 8 feet = _____ inches

5. 4 yards = _____ inches

6. 56 yards = _____ feet

7. 9 feet = _____ inches

8. 7 miles = _____ inches

1 foot = 12 inches

1 yard = 36 inches

1 yard = 3 feet

1 mile = 5,280 feet

9. 20 feet = _____ inches

10. 7 feet = _____ inches

11. 36 yards = _____ inches

12. 10 miles = _____ feet

Directions Use the chart and divide to make these conversions.

Express any remainders as fractions.

13. 180 inches = _____ feet

14. 38 inches = _____ feet

15. 96 inches = _____ feet

16. 39 inches = _____ feet

17. 50 inches = _____ feet

18. 52 feet = _____ yards

19. 15,840 feet = _____ miles

20. 75 feet = _____ yards

21. 21,120 feet = _____ miles

22. 300 feet = _____ yards

23. 6,000 feet = _____ miles

24. 192 inches = _____ feet

25. 288 inches = _____ yards



Operations with Linear Measurements

EXAMPLES

Add.

$$\begin{array}{r} 3 \text{ feet } 5 \text{ inches} \\ + 7 \text{ feet } 9 \text{ inches} \\ \hline 10 \text{ feet } 14 \text{ inches} \\ \text{or} \\ 11 \text{ feet } 2 \text{ inches} \end{array}$$

Subtract.

$$\begin{array}{r} \\ 8 \text{ feet } 8 \text{ inches} \\ - 2 \text{ feet } 9 \text{ inches} \\ \hline 3 \text{ feet } 8 \text{ inches} \end{array}$$

Multiply.

$$\begin{array}{r} 2 \text{ feet } 3 \text{ inches} \\ \times 6 \\ \hline 12 \text{ feet } 18 \text{ inches} \\ \text{or} \\ 13 \text{ feet } 6 \text{ inches} \end{array}$$

Divide.

$$12 \text{ yards } 6 \text{ feet } 10 \text{ inches} \div 2 =$$

$$\frac{12 \text{ yards}}{2} \quad \frac{6 \text{ feet}}{2} \quad \frac{10 \text{ inches}}{2} =$$

$$6 \text{ yards } 3 \text{ feet } 5 \text{ inches}$$

Directions Add these units of measure and simplify answers.

1. $4 \text{ yards } 3 \text{ feet}$
 $+ 2 \text{ yards } 4 \text{ feet}$

2. $8 \text{ feet } 11 \text{ inches}$
 $+ 2 \text{ feet } 5 \text{ inches}$

3. $5 \text{ feet } 6 \text{ inches} + 6 \text{ feet } 2 \text{ inches}$

4. $7 \text{ yards } 6 \text{ feet} + 4 \text{ yards } 6 \text{ feet}$

5. $6 \text{ yards } 11 \text{ inches} + 5 \text{ yards } 9 \text{ inches}$

Directions Subtract these units of measure. Simplify the answers.

6. $12 \text{ yards } 2 \text{ feet}$
 $- 3 \text{ yards } 3 \text{ feet}$

7. $9 \text{ feet } 11 \text{ inches}$
 $- 2 \text{ feet } 9 \text{ inches}$

8. $2 \text{ yards } 2 \text{ feet} - 4 \text{ feet} =$ _____

9. $8 \text{ feet } 6 \text{ inches} - 3 \text{ feet } 9 \text{ inches} =$ _____

10. $1 \text{ foot } 4 \text{ inches} - 9 \text{ inches} =$ _____

Directions Multiply these measurements.

11. $4 \text{ yards } 1 \text{ foot } 3 \text{ inches}$
 \times _____ 4 _____

12. $10 \text{ feet } 5 \text{ inches}$
 \times _____ 3 _____

13. $2 \times (3 \text{ feet } 2 \text{ inches}) =$ _____

14. $3 \times (3 \text{ yards } 2 \text{ feet } 7 \text{ inches}) =$ _____

15. $8 \times (7 \text{ yards } 3 \text{ feet}) =$ _____

Directions Divide these measurements.

16. $(18 \text{ yards } 24 \text{ feet } 9 \text{ inches}) \div 3 =$ _____

19. $(24 \text{ yards } 8 \text{ feet } 16 \text{ inches}) \div 8 =$ _____

17. $(4 \text{ yards } 2 \text{ feet } 8 \text{ inches}) \div 2 =$ _____

20. $(25 \text{ yards } 15 \text{ feet } 5 \text{ inches}) \div 5 =$ _____

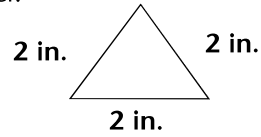
18. $(66 \text{ yards } 33 \text{ feet } 11 \text{ inches}) \div 11 =$ _____

Perimeter

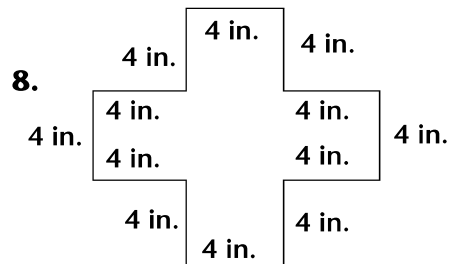
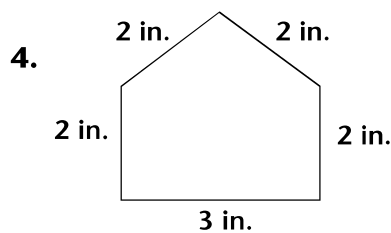
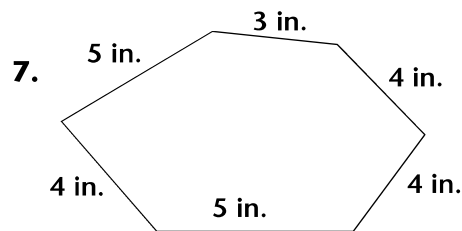
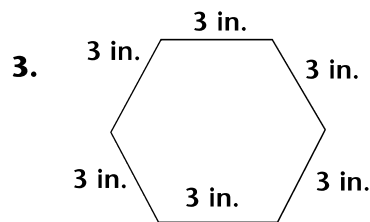
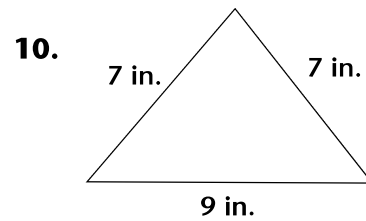
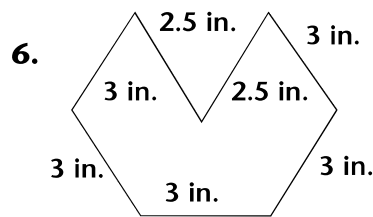
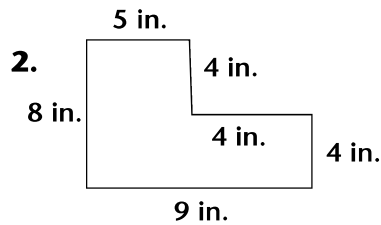
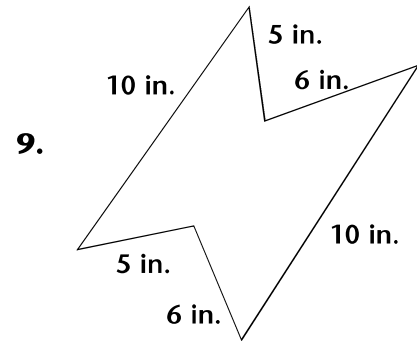
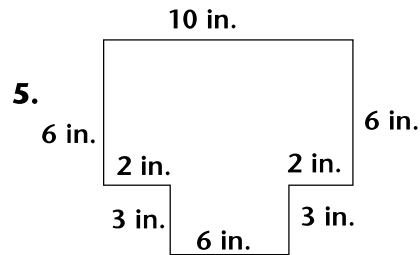
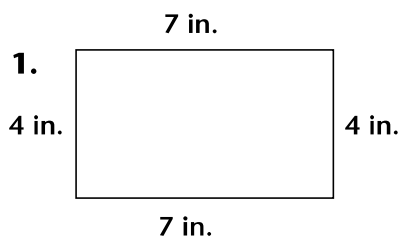
EXAMPLE

Add the lengths of all sides to get perimeter.

$$2 + 2 + 2 = 6 \text{ in.}$$



Directions Find the perimeter of each shape.

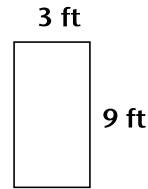
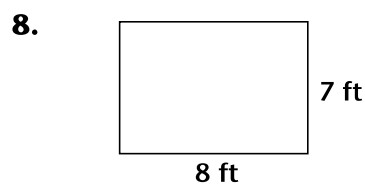
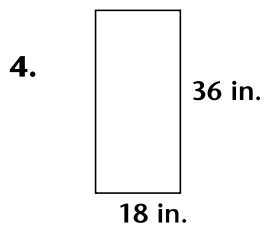
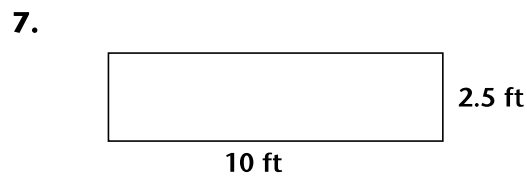
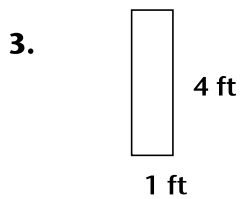
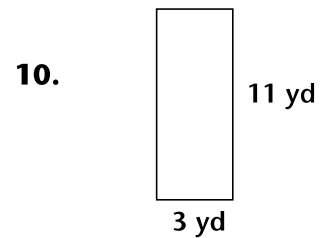
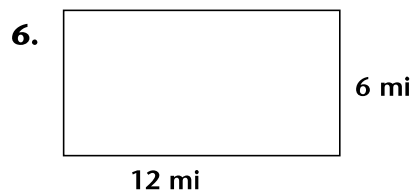
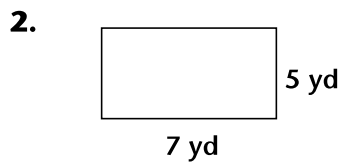
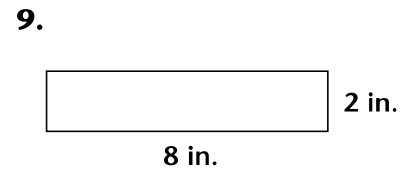
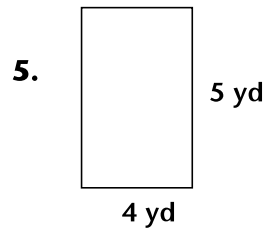
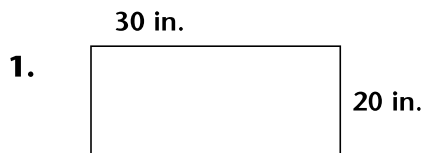


Area

EXAMPLE

Multiply length by width to find the area.

$$\begin{aligned}L \times W &= A \\9 \times 3 &= A \\27 \text{ square feet} &= A\end{aligned}$$

**Directions** Find the area of each rectangle.

Area of Triangles

EXAMPLE

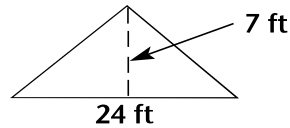
Find the area of a triangle whose base is 24 feet and height is 7 feet.

$$\text{Area} = \frac{1}{2} \text{ base} \times \text{height}$$

$$A = \frac{1}{2} (24) \times 7$$

$$A = 12 \times 7$$

$$A = 84 \text{ square feet}$$



Directions Find the area of each triangle described below.

- | | |
|---|---|
| 1. base = 16 feet
height = 6 feet _____ | 11. base = 6 inches
height = 17 inches _____ |
| 2. base = 41 feet
height = 32 feet _____ | 12. base = 3 yards
height = 20 yards _____ |
| 3. base = 40 feet
height = 10 feet _____ | 13. base = $\frac{2}{3}$ inch
height = 12 inches _____ |
| 4. base = 50 feet
height = 12 feet _____ | 14. base = $\frac{3}{4}$ foot
height = 16 feet _____ |
| 5. base = 12 feet
height = 10 feet _____ | 15. base = $1\frac{1}{8}$ inches
height = 6 inches _____ |
| 6. base = 5 feet
height = 4 feet _____ | 16. base = 10 yards
height = $4\frac{1}{2}$ yards _____ |
| 7. base = 20 inches
height = 10 inches _____ | 17. base = 20 yards
height = 5 yards _____ |
| 8. base = 33 inches
height = 50 inches _____ | 18. base = 10 feet
height = 2 feet _____ |
| 9. base = 9 yards
height = 18 yards _____ | 19. base = $\frac{1}{2}$ inch
height = $\frac{1}{16}$ inch _____ |
| 10. base = 10 yards
height = 15 yards _____ | 20. base = $1\frac{1}{16}$ inches
height = 6 inches _____ |

Area of Parallelograms

EXAMPLE

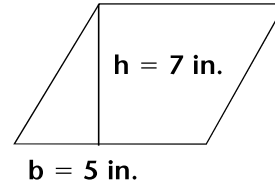
To find area of a parallelogram, multiply base by height.

$$\text{Area} = \text{base} \times \text{height}$$

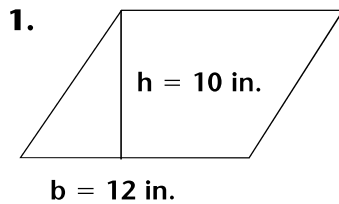
$$A = bh \quad b = 5 \text{ in.} \quad h = 7 \text{ in.}$$

$$A = 5 \times 7$$

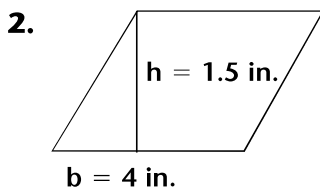
$$A = 35 \text{ square inches}$$



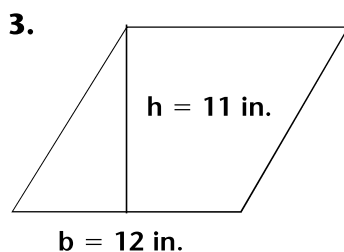
Directions Find the area of each parallelogram.



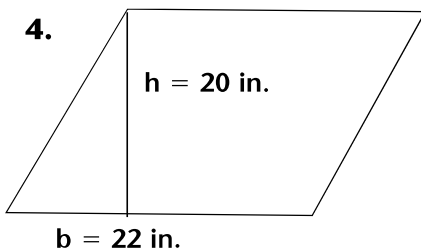
$$\text{Area} = \underline{\hspace{2cm}}$$



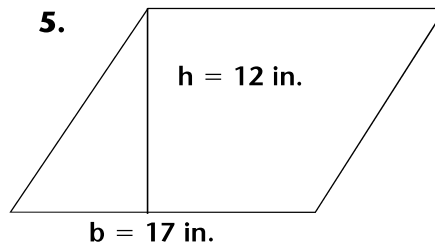
$$\text{Area} = \underline{\hspace{2cm}}$$



$$\text{Area} = \underline{\hspace{2cm}}$$



$$\text{Area} = \underline{\hspace{2cm}}$$



$$\text{Area} = \underline{\hspace{2cm}}$$

6. base = 20 feet
height = 30 feet

$$\text{Area} = \underline{\hspace{2cm}}$$

7. base = 34 yards
height = 10 yards

$$\text{Area} = \underline{\hspace{2cm}}$$

8. base = 4 inches
height = 14 inches

$$\text{Area} = \underline{\hspace{2cm}}$$

9. base = 12 feet
height = 6 feet

$$\text{Area} = \underline{\hspace{2cm}}$$

10. base = 21 miles
height = 2 miles

$$\text{Area} = \underline{\hspace{2cm}}$$

11. base = 1 foot
height = 1 foot

$$\text{Area} = \underline{\hspace{2cm}}$$

12. base = 14 inches
height = 1 foot

$$\text{Area} = \underline{\hspace{2cm}}$$

13. base = 4.5 inches
height = 4 inches

$$\text{Area} = \underline{\hspace{2cm}}$$

14. base = 5 inches
height = 1 foot

$$\text{Area} = \underline{\hspace{2cm}}$$

15. base = 3 yards
height = 4 feet

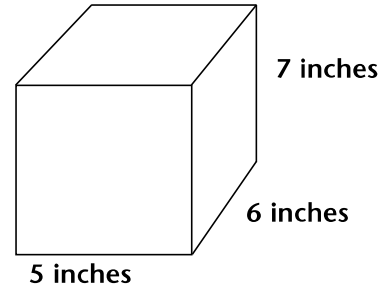
$$\text{Area} = \underline{\hspace{2cm}}$$

Volume of Rectangular Prisms

EXAMPLE

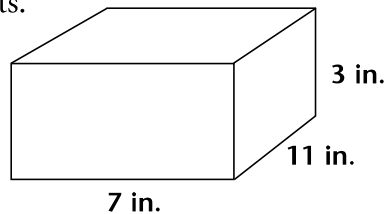
Multiply length by width by height to find volume.

$$\begin{aligned} \text{Volume} &= \text{area of base} \times \text{height} \\ &= \text{length} \times \text{width} \times \text{height} \\ &= 5 \text{ in.} \times 6 \text{ in.} \times 7 \text{ in.} \\ &= 30 \text{ square inches} \times 7 \text{ in.} \\ &= 210 \text{ cubic inches} \end{aligned}$$



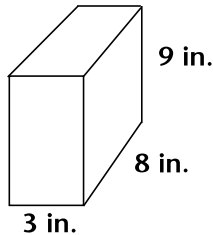
Directions Compute the volume for these prisms. Express your answers in cubic units.

1.



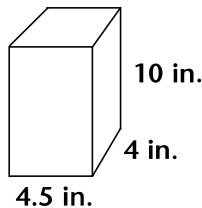
Volume = _____

2.



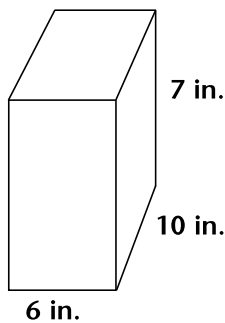
Volume = _____

3.



Volume = _____

4.



Volume = _____

5. length = 20 yards
width = 7 yards
height = 4 yards

Volume = _____

6. length = 2 feet
width = 5 feet
height = 10 feet

Volume = _____

7. length = 15 feet
width = 7 feet
height = 5 feet

Volume = _____

8. length = 13 feet
width = 5 feet
height = 2 feet

Volume = _____

9. length = 6 in.
width = 14 in.
height = 4 in.

Volume = _____

10. length = 10 in.
width = 12 in.
height = 9 in.

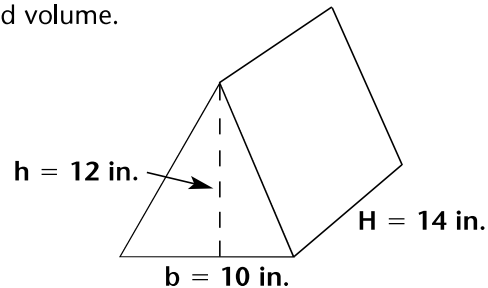
Volume = _____

Volume of Triangular Prisms

EXAMPLE

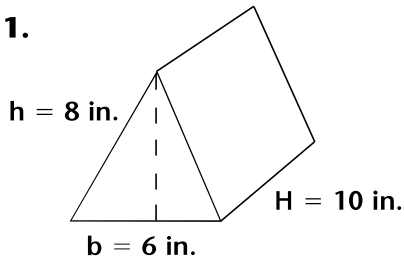
Multiply $\frac{1}{2}$ area of base by height to find volume.

$$\begin{aligned} \text{Volume} &= \frac{1}{2} (\text{base} \times \text{height}) \text{ Height} \\ &= \frac{1}{2} (10 \times 12) \times 14 \\ &= \frac{1}{2} (120) \times 14 \\ &= 60 \times 14 \\ &= 840 \text{ cubic inches} \end{aligned}$$



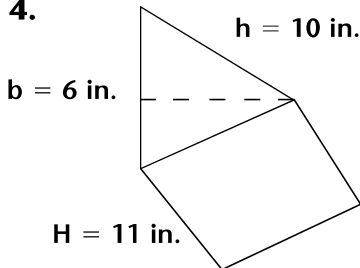
Directions Find the volume of these triangular prisms.

1.



Volume = _____

4.

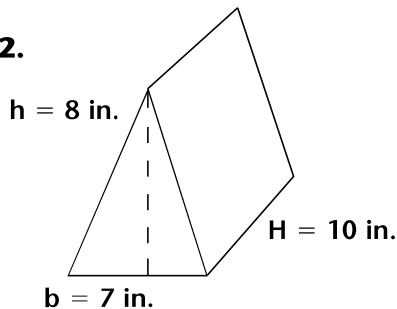


Volume = _____

7. base = 30 inches
height = 10 inches
Height = 15 inches

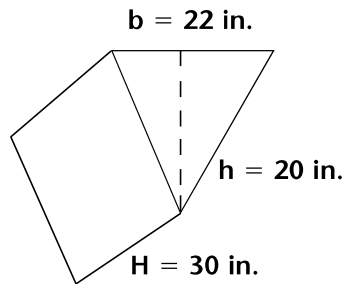
Volume = _____

2.



Volume = _____

5.



Volume = _____

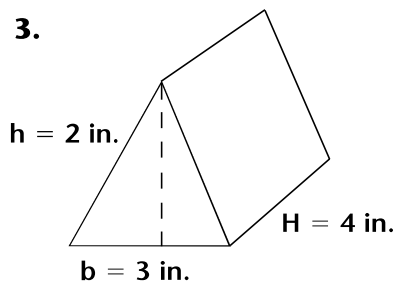
8. base = 40 inches
height = 10 inches
Height = 20 inches

Volume = _____

9. base = 16 inches
height = 12 inches
Height = 22 inches

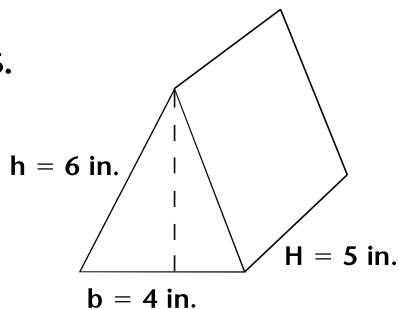
Volume = _____

3.



Volume = _____

6.



Volume = _____

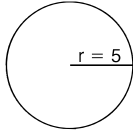
10. base = 20 inches
height = 15 inches
Height = 17 inches

Volume = _____

Finding Circumference

EXAMPLE

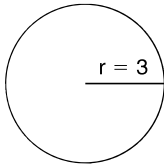
Find the circumference of a circle with a radius of 5 inches.


 Circumference = $\pi \times d$ where $\pi = 3.14$
 $C = 3.14 \times 10$ because diameter = $2 \times$ radius

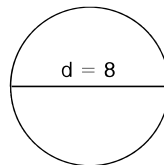
 $C = 31.4$ inches

 Remember to multiply the radius by 2 to get the diameter for the formula. $C = \pi \times d$
Directions Find the circumference of these circles.

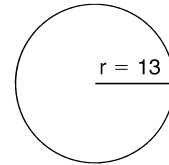
1.


 $C = \underline{\hspace{2cm}}$

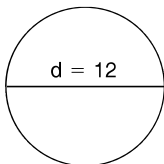
3.


 $C = \underline{\hspace{2cm}}$

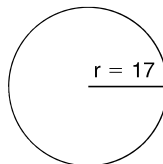
5.


 $C = \underline{\hspace{2cm}}$

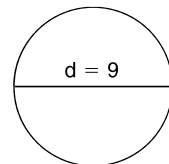
2.


 $C = \underline{\hspace{2cm}}$

4.


 $C = \underline{\hspace{2cm}}$

6.


 $C = \underline{\hspace{2cm}}$

7. diameter = 22

Circumference = _____

9. radius = 16

Circumference = _____

8. diameter = 25

Circumference = _____

10. radius = 20

Circumference = _____

Area and Circumference of Circles

EXAMPLES

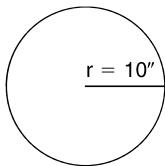
Find the area and circumference of a circle with a radius of 5 inches.

$$\begin{aligned} \text{Area} &= \pi r^2 \\ &= 3.14 \times 5^2 \\ &= 3.14 \times 25 \\ &= 78.50 \text{ square inches} \end{aligned}$$

$$\begin{aligned} \text{Circumference} &= 2 \pi r \\ &= 2 \times 3.14 \times 5 \\ &= 31.4 \text{ inches} \end{aligned}$$

Directions Solve for the area and circumference for each circle.
Use 3.14 for π . The abbreviation for circumference is C.

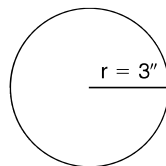
1.



Area = _____

C = _____

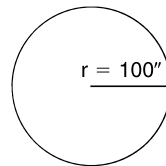
5.



Area = _____

C = _____

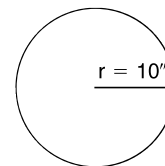
9.



Area = _____

C = _____

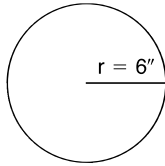
13.



Area = _____

C = _____

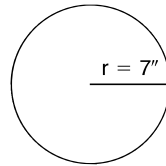
2.



Area = _____

C = _____

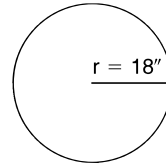
6.



Area = _____

C = _____

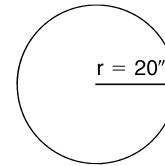
10.



Area = _____

C = _____

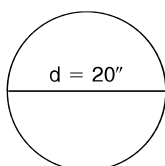
14.



Area = _____

C = _____

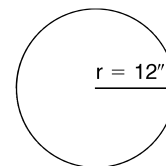
3.



Area = _____

C = _____

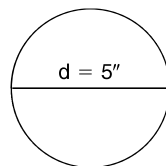
7.



Area = _____

C = _____

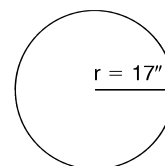
11.



Area = _____

C = _____

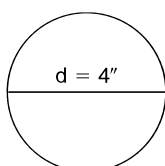
15.



Area = _____

C = _____

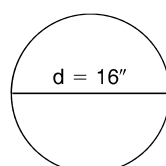
4.



Area = _____

C = _____

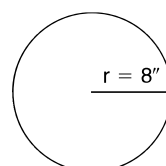
8.



Area = _____

C = _____

12.



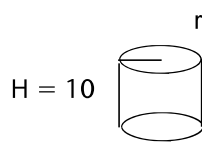
Area = _____

C = _____

Volume of a Cylinder

EXAMPLE

$$\text{Volume} = \pi r^2 H$$



$$\begin{aligned} \text{Volume} &= \pi \times 3^2 \times 10 \\ &= 3.14 \times 9 \times 10 \\ &= 3.14 \times 90 \\ &= 282.6 \text{ cubic units} \end{aligned}$$

Remember volume is expressed as cubic units.

Directions Find the volume for each cylinder.

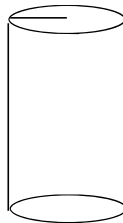
1.



$r = 11$
 $H = 20$

$$V = \underline{\hspace{2cm}}$$

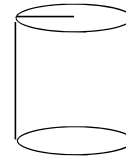
3.



$r = 12$
 $H = 30$

$$V = \underline{\hspace{2cm}}$$

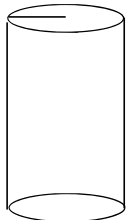
5.



$r = 1$
 $H = 10$

$$V = \underline{\hspace{2cm}}$$

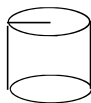
2.



$r = 3$
 $H = 20$

$$V = \underline{\hspace{2cm}}$$

4.



$r = 9$
 $H = 2$

$$V = \underline{\hspace{2cm}}$$

6.



$r = 11$
 $H = 2$

$$V = \underline{\hspace{2cm}}$$

7. radius = 11

height = 10

Volume = _____

9. radius = 20

height = 22

Volume = _____

8. radius = 10

height = 15

Volume = _____

10. radius = 8

height = 18

Volume = _____

Units of Time

EXAMPLE

Add.

$$\begin{array}{r}
 5 \text{ weeks } 3 \text{ days} \\
 + \quad \quad \quad 4 \text{ days} \\
 \hline
 5 \text{ weeks } 7 \text{ days} = 6 \text{ weeks}
 \end{array}$$

Directions Perform the indicated operations. Simplify the answers.

1.
$$\begin{array}{r}
 6 \text{ weeks } 4 \text{ days} \\
 + \quad \quad \quad 4 \text{ days} \\
 \hline
 \end{array}$$

8.
$$\begin{array}{r}
 10 \text{ years } 2 \text{ weeks } 1 \text{ day} \\
 - 8 \text{ years } 5 \text{ weeks } 4 \text{ days} \\
 \hline
 \end{array}$$

2.
$$\begin{array}{r}
 3 \text{ years } 2 \text{ weeks } 6 \text{ days} \\
 + 2 \text{ years } 6 \text{ weeks } 3 \text{ days} \\
 \hline
 \end{array}$$

9.
$$\begin{array}{r}
 3 \text{ days } 12 \text{ hours } 10 \text{ min} \\
 + 3 \text{ days } 7 \text{ hours } 56 \text{ min} \\
 \hline
 \end{array}$$

3.
$$\begin{array}{r}
 7 \text{ weeks } 4 \text{ days} \\
 + 2 \text{ weeks } 5 \text{ days} \\
 \hline
 \end{array}$$

10.
$$\begin{array}{r}
 5 \text{ hours } 10 \text{ min } 5 \text{ sec} \\
 + 8 \text{ hours } 50 \text{ min } 58 \text{ sec} \\
 \hline
 \end{array}$$

4.
$$\begin{array}{r}
 9 \text{ weeks } 5 \text{ days} \\
 - 7 \text{ weeks } 6 \text{ days} \\
 \hline
 \end{array}$$

11.
$$\begin{array}{r}
 2 \text{ hours } 20 \text{ min } 4 \text{ sec} \\
 - 1 \text{ hour } 10 \text{ min } 7 \text{ sec} \\
 \hline
 \end{array}$$

5.
$$\begin{array}{r}
 8 \text{ years } 6 \text{ weeks } 3 \text{ days} \\
 - 3 \text{ years } 5 \text{ weeks } 6 \text{ days} \\
 \hline
 \end{array}$$

12.
$$\begin{array}{r}
 4 \text{ hours } 10 \text{ min } 5 \text{ sec} \\
 - 3 \text{ hours } 9 \text{ min } 5 \text{ sec} \\
 \hline
 \end{array}$$

6.
$$\begin{array}{r}
 5 \text{ weeks } 3 \text{ days} \\
 - \quad \quad \quad 6 \text{ days} \\
 \hline
 \end{array}$$

13.
$$\begin{array}{r}
 3 \text{ hours } 2 \text{ min} \\
 - 2 \text{ hours } 8 \text{ min} \\
 \hline
 \end{array}$$

7.
$$\begin{array}{r}
 15 \text{ years } 9 \text{ weeks} \\
 - 7 \text{ years } 7 \text{ weeks} \\
 \hline
 \end{array}$$

14.
$$\begin{array}{r}
 7 \text{ hours } \quad \quad \quad 8 \text{ sec} \\
 - 6 \text{ hours } 10 \text{ min} \\
 \hline
 \end{array}$$

15. 3 days = _____ hours

17. 3 years = _____ weeks

16. 18 minutes = _____ seconds

18. 180 seconds = _____ minutes

19. 5 weeks 3 days - 3 weeks 5 days 3 hours = _____

20. 8 years 8 weeks 2 days + 2 years 9 weeks 5 days = _____

21. 4 hours 3 min 34 sec - 2 hours 7 min 50 sec = _____

22. 5 min 45 sec + 5 hours 4 min 49 sec = _____

23. 35 hours 24 sec - 9 hours 28 min = _____

24. 55 min 19 sec + 1 hour 20 min 4 sec = _____

25. 36 hours - 3 hours 5 min 6 sec = _____

Time Problems

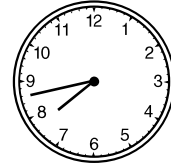
You can solve word problems involving elapsed time by adding or subtracting time. You may need to rename in some problems. Remember that there are 60 minutes in one hour.

EXAMPLE

Mr. Winkle went to sleep at 11:25 last night. He looked at the clock when he woke up. How long did he sleep?

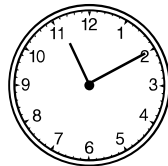
$$\begin{array}{r} 7:43 \\ - 11:25 \\ \hline \end{array} = \begin{array}{r} 19:43 \\ - 11:25 \\ \hline 8:18 \end{array}$$

Mr. Winkle slept 8 hours and 18 minutes.

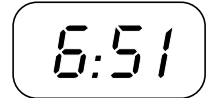


Directions Solve each word problem. Use the clock shown with each problem to help you.

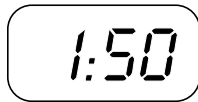
1. Tanya started to play tennis at 9:30. How long has she been playing?



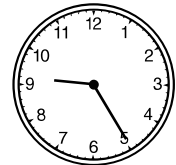
6. Carmine's favorite program comes on at 8:30. How long until it starts?



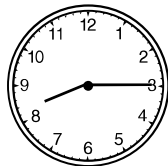
2. Emily left for the ocean at 7:45. She saw a clock when she arrived. How long was the trip?



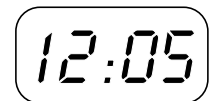
7. Niki arrived at the doctor's office at 8:45. She glanced at the clock when her name was called. How long did she wait?



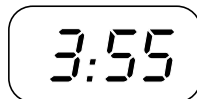
3. A video lasts 117 minutes. At what time will it be finished?



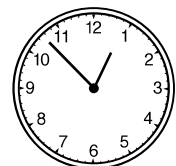
8. Jared started the meeting at 10:15. Afterward, he looked at the clock. How long was the meeting?



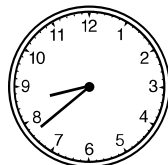
4. The roast is to cook for 2 hours and 15 minutes. At what time will it be finished cooking?



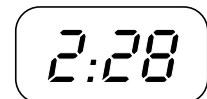
9. The bus from Duluth will arrive at 3:23. How long until it arrives?



5. We can play for another half of an hour. At what time must we come in?



10. Carlos put money in the parking meter for $1\frac{1}{2}$ hours. When must he return?



Reading Pictographs

EXAMPLE

Look at the pictograph below.

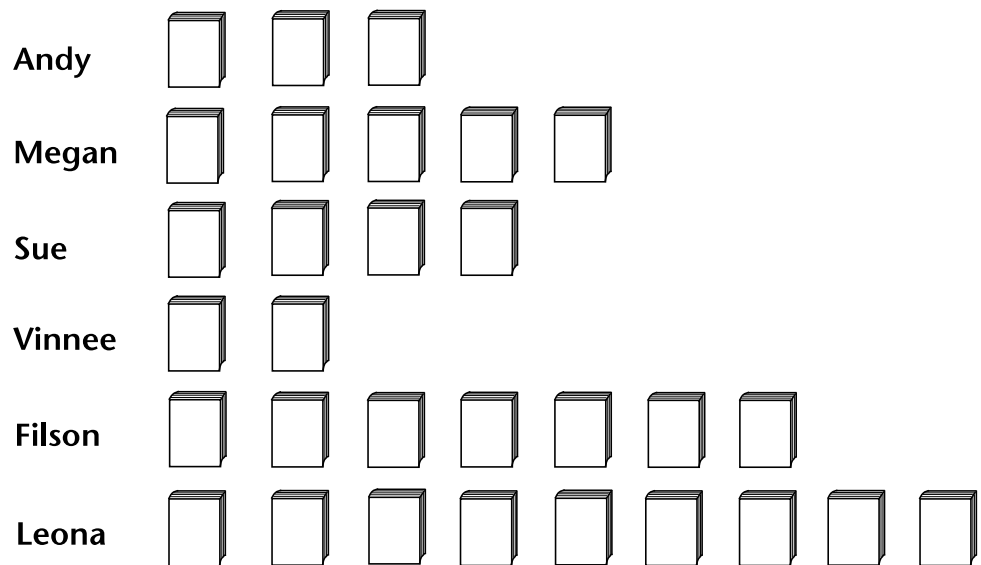
One book is equal to 4 books read.
 How many books did Andy read?
 3 whole books are pictured.
 $3 \times 4 = 12$

Andy read 12 books.

Summer Book Reading Club



= 4 books read



Directions Use the pictograph to answer the questions.

1. How many books did Megan read for the summer? _____
2. How many books did Sue read? _____
3. How many books did Filson read? Did he read more than Andy? _____
4. How many books did Vinnee read? _____
5. How many books did Sue and Andy read? _____
6. What was the total number of books read by the club? _____
7. What is the title of this graph? _____
8. How many books would Megan need to read to match Filson's total? _____
9. How many books did Leona read? _____
10. How many did both Leona and Megan read? _____

Constructing Bar Graphs

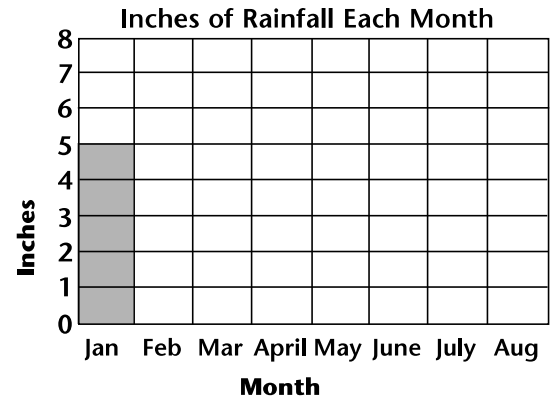
EXAMPLE

January = 5 inches

Find January on the horizontal line.

Find 5 on the vertical line.

Shade the bar from the horizontal line to 5.



Directions Shade the data for each bar of the graphs.

Jan = 3 inches

Feb = 5 inches

March = 4 inches

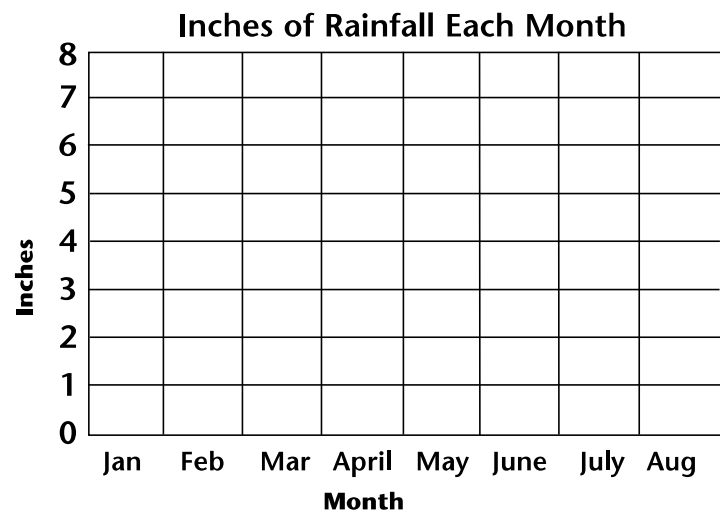
April = 2 inches

May = 6 inches

June = 5 inches

July = 8 inches

Aug = 5 inches



Jan = 6 inches

Feb = 3 inches

March = 7 inches

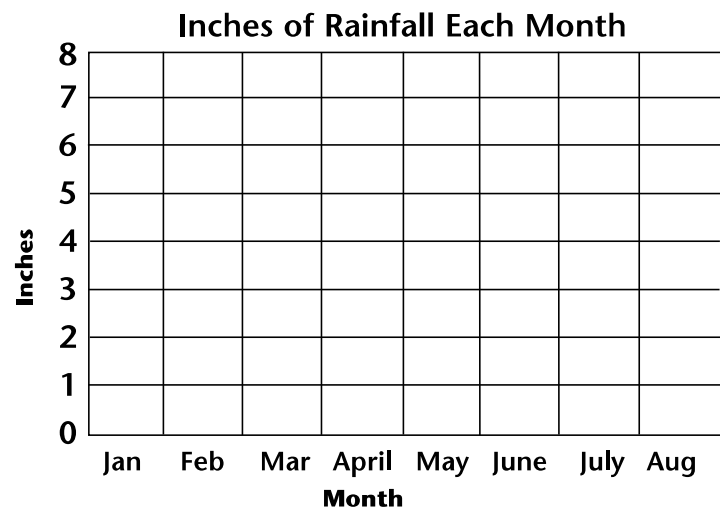
April = 1 inches

May = 4.5 inches

June = 8 inches

July = 3.5 inches

Aug = 1.5 inches



Reading Divided Bar Graphs

EXAMPLE

How many trucks are in Lot F?

Find F on the graph.

Determine the scale.

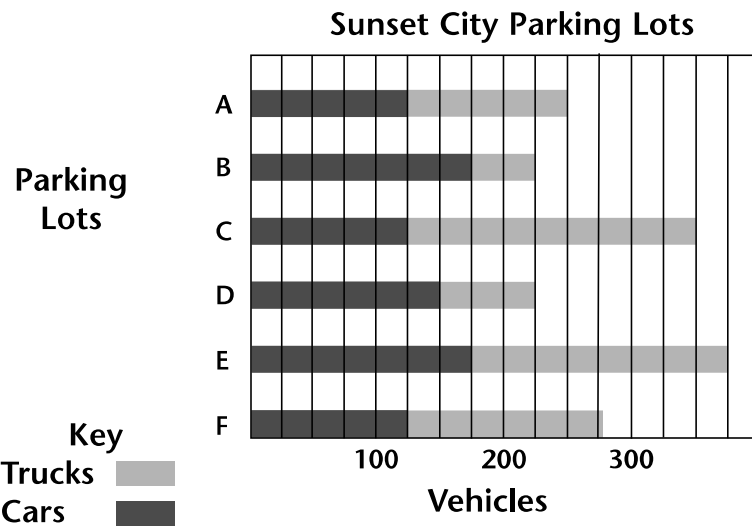
Read the key.

The scale in each section equals 25 vehicles.

Trucks make up 6 sections.

$25 \times 6 = 150$ 150 trucks are in Lot F.

Directions Use the divided bar graph to answer the questions.



1. How many trucks are parked in Lot D? _____
2. How many cars are located in Lot B? _____
3. How many vehicles are in Lot F? _____
4. How many trucks are in Lot A? _____
5. How many vehicles are in Lot C? _____
6. How many vehicles are in Lot D? _____
7. How many cars are parked in Lot E? _____
8. How many vehicles are shown for Lots D and E together? _____
9. How many vehicles are shown for Lots A and B together? _____
10. How many vehicles are parked in Sunset City parking lots? _____

Constructing Divided Bar Graphs

EXAMPLE

How many points did Mattie score on the first test?

Find Mattie on the graph.

Determine the scale.

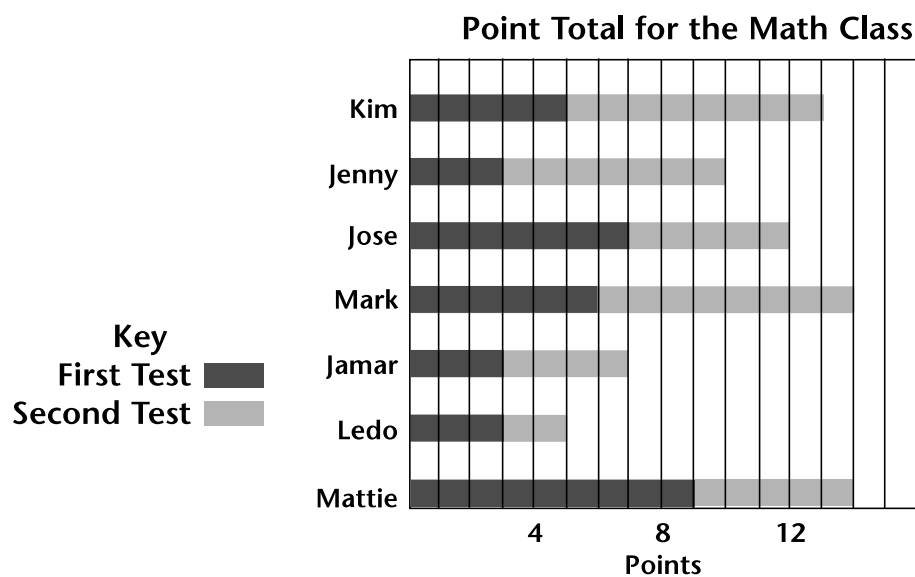
Read the key.

The scale is 1 section equals 1 point.

Mattie's first test shows 9 sections.

Mattie scored 9 points.

Directions Use the divided bar graph to answer the questions.



1. Did Jamar score more total points than Jenny? _____
2. How many total points did Jose score? _____
3. How many points did Ledo score on the first test? _____
4. How many points did Kim score on the second test? _____
5. What are the total points accumulated for Mark and Kim? _____
6. What are the total points accumulated for all the students? _____
7. What are the total points for Jenny and Mark on the second test? _____
8. What are the total points scored on the first test? _____
9. What is the difference between the first and second test totals? _____
10. What was Ledo's total point accumulation? _____

Reading Line Graphs

EXAMPLE

How many tickets were sold in January?

Find January (Jan) on the graph.

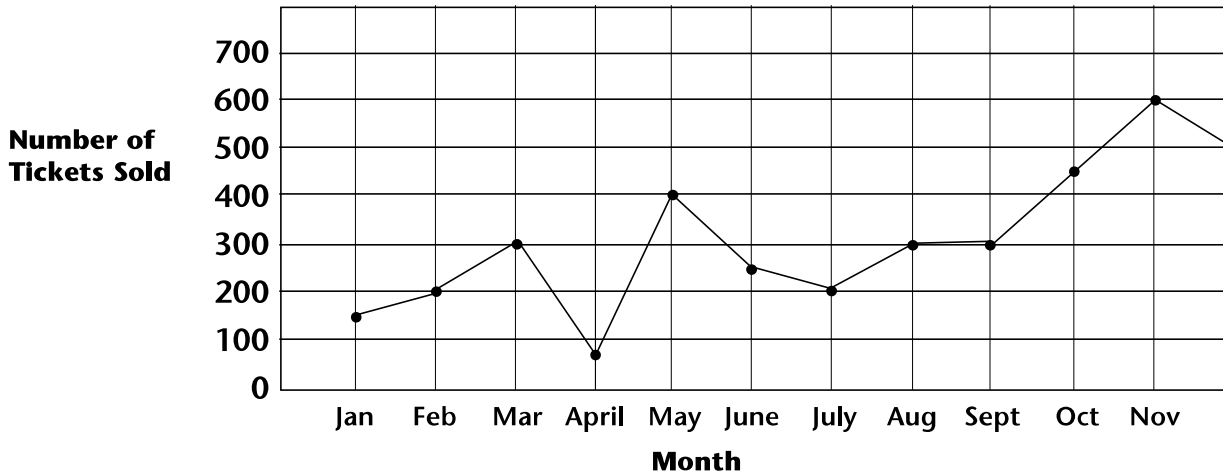
Use a straightedge to align the point for January with the vertical line.

Read the number.

150 tickets were sold in January.

Directions Use the line graph to answer the questions about the school's raffle ticket sale.

School Raffle Ticket Sales



- Were there more tickets sold in May than October? _____
- How many tickets were sold in May? _____
October? _____
- How many tickets were sold in March? _____
- How many tickets were sold in the summer months of June and July? _____
- What month had the highest sales? _____
- What month had the lowest sales? _____
- How many more tickets were sold in May than July? _____
- How many tickets were sold in February? _____
- How many tickets were sold in June? _____
- What was the total number of tickets sold? _____

Circle Graphs

EXAMPLE

The Davises have an annual income of \$24,000.00.
How much do they spend on food?

Find the section labeled food and identify its percent of the budget.

Multiply. $\$24,000.00 \times 30\% =$
 $\$24,000.00 \times 0.30 = \$7,200.00$

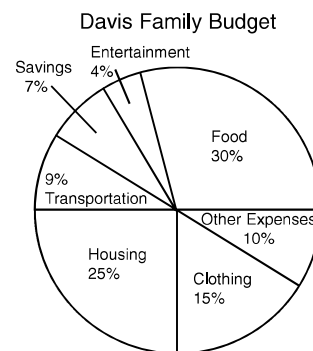
Directions Answer the following questions about this graph.

Use an annual income of \$24,000 for problems 2–4.

1. What do the members of the Davis family spend most of their money on? _____
2. How much do they spend for clothing? _____
3. How much do they save each year? _____
4. What do they spend for entertainment? _____
5. How much do the Davises spend for each category in their budget if their annual income is \$48,400.00?

Food _____ Clothing _____ Transportation _____

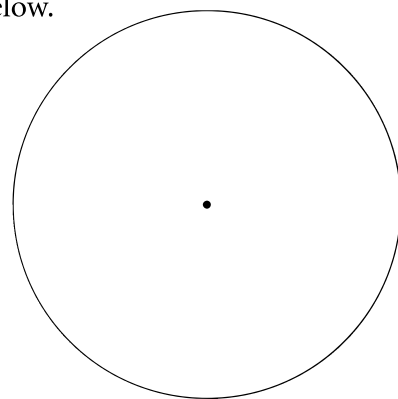
Housing _____ Savings _____ Entertainment _____



Directions Make a circle graph to show the information in the table below.

Follow these six steps:

- Step 1** Draw a large circle. Mark the center of the circle with a dot.
- Step 2** Draw a radius.
- Step 3** Find out how many degrees are in each sector.
To find the degrees, multiply the percent or fraction by the 360° in a circle. (Example: $360^\circ \times 10\% = 36^\circ$)
- Step 4** Use a protractor to measure and draw each sector.
Use the center of the circle as the vertex of each angle.
- Step 5** Label each sector and mark the appropriate percent or fraction.
- Step 6** Give the graph a title.



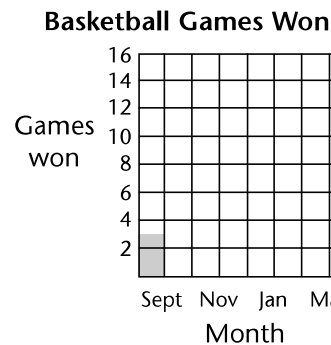
The Thomas Family Budget	
Category	Percent Allowed
Food	25%
Housing	30%
Clothing	20%
Car	10%
Savings	5%
Other	10%

Graphs That Mislead

EXAMPLE

Draw a bar showing 3 games won in September on each graph.

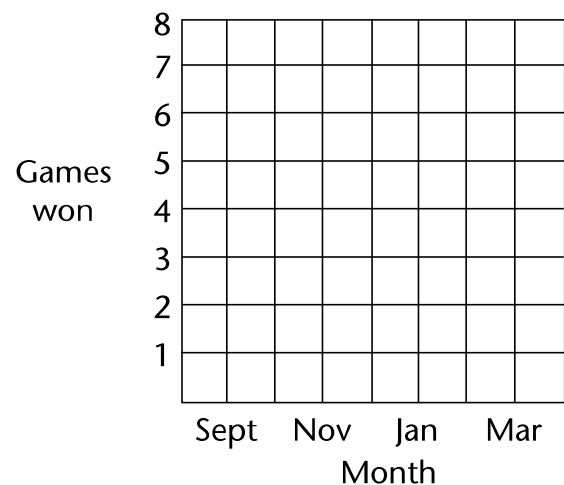
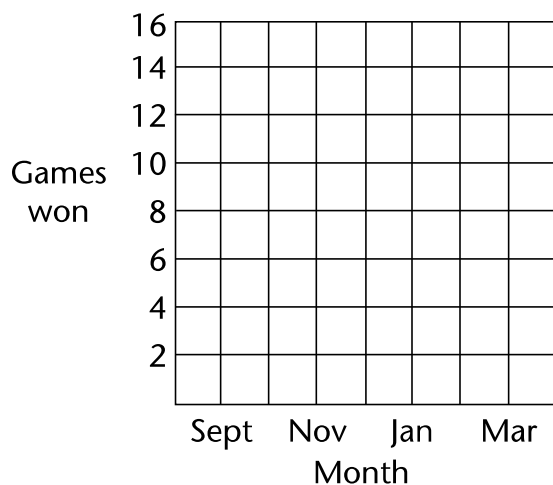
Find September on the graphs.
Give a title for the graphs.
Shade sections to show 3 games in each graph.



Directions Make the bar graphs below. Then answer the questions on your own paper.

Walbrook High School basketball stats for the current school year	
Month	Games won
September	2 games
October	3 games
November	4 games
December	5 games
January	6 games
February	8 games
March	7 games

- Construct 2 bar graphs for the data. Use the templates given below.
- Give a title for each graph.
- How do the graphs differ?
- Why does graph 2 look better than graph 1?
- Does one graph represent the data better than the other? Explain.



Scale Models

EXAMPLE

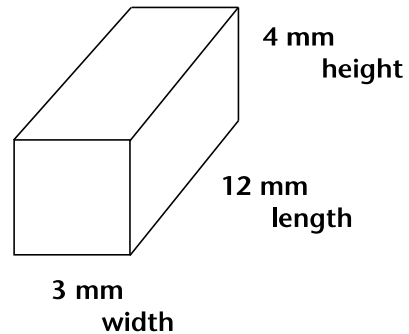
The building block shown below is a scale model of a much bigger block using 1:50 scale. How long is the actual block?

$$\frac{1}{50} = \frac{12}{n}$$

$$50 \times 12 = n$$

$$600 \text{ mm} = n \quad 600 \text{ mm is the length of the actual building block.}$$

Directions Use the model to solve each problem.



1. The ratio is changed to 1:25.

a. Solve for the actual length. _____

b. Solve for the actual width. _____

c. Solve for the actual height. _____

2. Solve for all three components if the ratio is 1:75.

3. Solve for all three components if the ratio is 1:200.

4. Solve for all three components if the ratio is 1:100.

5. Solve for all three components if the ratio is 1:80.

Scale Drawings

EXAMPLE

The wagon below measures $\frac{1}{2}$ inch high and $2\frac{1}{2}$ inches long.

The scale ratio is 1:50. How long is the actual wagon?

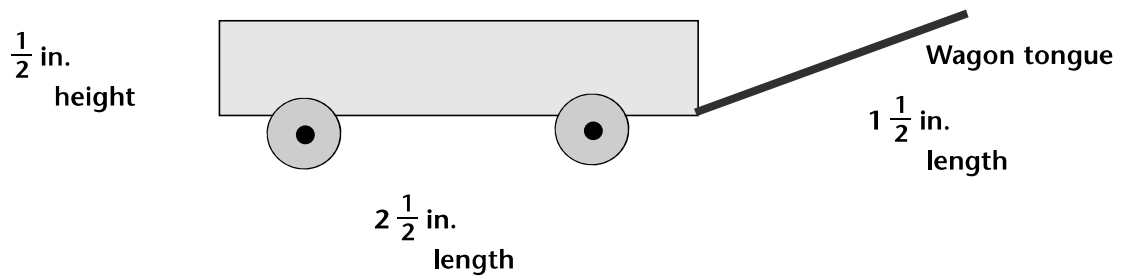
$$\frac{1}{50} = \frac{2\frac{1}{2}}{n}$$

$$2\frac{1}{2} \times 50 = n$$

$$\frac{5}{2} \times 50 = \frac{250}{2} = 125$$

125 inches = n The actual wagon is 125 inches long.

Directions Use the model to solve each problem.



1. Solve for the actual height of the wagon if the scale is 1:50. _____
2. Solve for the actual height of the wagon if the scale is 1:25. _____
3. Solve for the actual length of the wagon with a scale of 1:100. _____
4. How long is the wagon tongue if the scale is 1:50? _____
5. How long is the wagon tongue if the scale is 1:25? _____

Floor Plans

EXAMPLE

The scale is 1 inch for each 8 feet. Find the actual dimensions of this drawing in feet.

Find the length.

Set up a proportion.

$$\frac{1}{8} = \frac{6}{n}$$

$$8 \times 6 = n$$

$$48 \text{ feet} = n \quad \text{Actual length is 48 feet.}$$

Find the width.

Set up a proportion.

$$\frac{1}{8} = \frac{3}{n}$$

$$8 \times 3 = n$$

$$24 \text{ feet} = n \quad \text{Actual width is 24 feet.}$$

Scale
1 inch = 8 feet



width = 3 inches

length = 6 inches

Directions Use proportions to solve each problem.

1. Find the actual measurements in feet of a room drawing that measures 4 inches by 5 inches with a scale of 1 inch = 3 feet.

length _____ width _____

2. Find the actual measurements in feet of a room drawing that measures 3 inches by 4 inches with a scale of 1 inch = 4 feet.

length _____ width _____

3. Scale of 1 inch = 5 feet

length = 4 inches

width = 3 inches

actual length = _____

actual width = _____

4. Scale of 1 inch = 4 feet

length = 7 inches

width = 6 inches

actual length = _____

actual width = _____

5. Scale of 1 inch = 6 feet

length = 5 inches

width = 3 inches

actual length = _____

actual width = _____



Map Distances

EXAMPLE

Use a scale of 1 inch = 500 miles.

Solve for the actual distance between two cities if they measure $3\frac{1}{2}$ inches apart.

$$3\frac{1}{2} \times 500 = \text{actual distance}$$

$$\frac{7}{2} \times 500 = \text{actual distance}$$

$$\frac{3,500}{2} = \text{actual distance}$$

1,750 miles

The actual distance is 1,750 miles.

Directions Use the information to solve each problem.

1. scale of 1 inch = 600 miles
measured distance of $2\frac{1}{2}$ inches
actual distance = _____

2. scale of 1 inch = 500 miles
measured distance of $3\frac{1}{2}$ inches
actual distance = _____

3. scale of 1 inch = 400 miles
measured distance of 5 inches
actual distance = _____

4. scale of 1 inch = 14 miles
measured distance of 6 inches
actual distance = _____

5. scale of 1 inch = 13 miles
measured distance of $4\frac{1}{2}$ inches
actual distance = _____

6. scale of 1 inch = 35 miles
measured distance of $4\frac{1}{2}$ inches
actual distance = _____

7. scale of 1 inch = 40 miles
measured distance of 7 inches
actual distance = _____

8. scale of 1 inch = $12\frac{1}{2}$ miles
measured distance of 6 inches
actual distance = _____

9. scale of 1 inch = 100 miles
measured distance of 3 inches
actual distance = _____

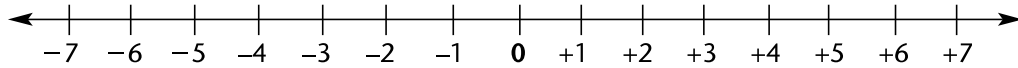
10. scale of 1 inch = 200 miles
measured distance of $1\frac{1}{2}$ inches
actual distance = _____



Integers

EXAMPLES

Compare the numbers using $<$ and $>$.



1 5 $<$ means less than. Read 1 is less than 5. $1 < 5$

6 2 $>$ means more than. Read 6 is more than 2. $6 > 2$

Directions Use the number line to help you compare the integers in each pair using $<$ or $>$.

- | | | | |
|----------------------|-----------------------|------------------------|-------------------------|
| 1. -1 8 | 6. -9 -5 | 11. -11 -1 | 16. -5 0 |
| 2. -1 -2 | 7. +1 -3 | 12. -1 0 | 17. -3 -5 |
| 3. 3 -3 | 8. 0 -9 | 13. 0 -19 | 18. +7 -1 |
| 4. +4 -5 | 9. -4 +2 | 14. -1 +1 | 19. -34 +32 |
| 5. +5 +9 | 10. -4 -5 | 15. -8 +1 | 20. +19 -1 |

Directions Find the sum of these integers.

- | | | |
|------------------------------|---------------------------|---------------------------|
| 21. $0 + 3$ _____ | 24. $-3 + 3$ _____ | 27. $-9 + 0$ _____ |
| 22. $-8 + 8$ _____ | 25. $-1 + 1$ _____ | 28. $-1 + 0$ _____ |
| 23. $+9 + (-9)$ _____ | 26. $-2 + 2$ _____ | |

Directions Name the opposite of each integer.

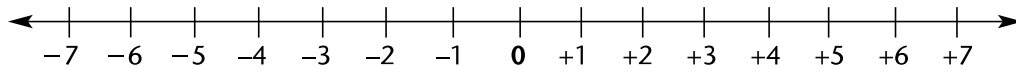
- | | | | |
|---------------------------|---------------------------|----------------------------|----------------------------|
| 29. -23 _____ | 32. 0 _____ | 35. -29 _____ | 38. -201 _____ |
| 30. +54 _____ | 33. +33 _____ | 36. -211 _____ | 39. -101 _____ |
| 31. -1 _____ | 34. +1 _____ | 37. +22 _____ | 40. +46 _____ |

Adding Positive and Negative Integers

EXAMPLE

Find the sum of 2 and (-8) .

Begin at 2 on the number line. Move 8 places left.



$$2 + (-8) = -6$$

Directions Use a number line to help find each sum.

- | | | |
|----------------------|-------------------------|-------------------------|
| 1. $+3 + (-7)$ _____ | 8. $-9 + (+1)$ _____ | 15. $-1 + 0$ _____ |
| 2. $-3 + (+2)$ _____ | 9. $-3 + (+9)$ _____ | 16. $-13 + (-12)$ _____ |
| 3. $-3 + (+8)$ _____ | 10. $+2 + (+4)$ _____ | 17. $+11 + (-21)$ _____ |
| 4. $-9 + (-1)$ _____ | 11. $+8 + (-1)$ _____ | 18. $-19 + (+10)$ _____ |
| 5. $-3 + (-1)$ _____ | 12. $+2 + (-2)$ _____ | 19. $+12 + (-16)$ _____ |
| 6. $-7 + (+1)$ _____ | 13. $-11 + (-12)$ _____ | 20. $-14 + (+1)$ _____ |
| 7. $-1 + (-1)$ _____ | 14. $-10 + (-10)$ _____ | |

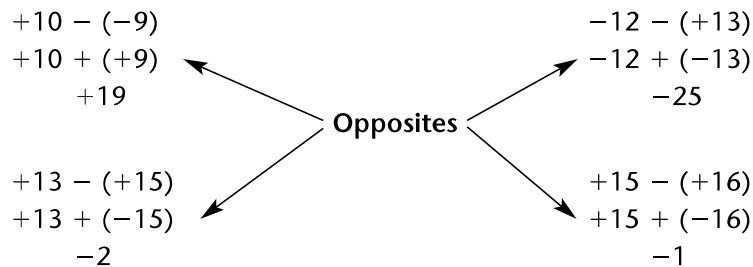
Directions Give the absolute value for each number.

- | | | |
|-------------------|--------------------|--------------------|
| 21. $ -3 $ _____ | 28. $ -99 $ _____ | 35. $ +102 $ _____ |
| 22. $ +12 $ _____ | 29. $ +22 $ _____ | 36. $ +38 $ _____ |
| 23. $ -1 $ _____ | 30. $ -202 $ _____ | 37. $ +51 $ _____ |
| 24. $ -11 $ _____ | 31. $ -33 $ _____ | 38. $ -18 $ _____ |
| 25. $ -6 $ _____ | 32. $ +17 $ _____ | 39. $ -111 $ _____ |
| 26. $ -77 $ _____ | 33. $ +21 $ _____ | 40. $ -90 $ _____ |
| 27. $ +8 $ _____ | 34. $ -28 $ _____ | |

Subtracting Positive and Negative Integers

EXAMPLES

Change subtraction problems to addition of the opposite.



Directions Solve these subtraction problems by changing to adding the opposite.

- | | |
|---|--|
| <p>1. $+1 - (-12)$ _____</p> <p>2. $+22 - (-12)$ _____</p> <p>3. $+10 - (-12)$ _____</p> <p>4. $+20 - (-12)$ _____</p> <p>5. $-9 - (+11)$ _____</p> <p>6. $-31 - (+20)$ _____</p> <p>7. $+21 - (-20)$ _____</p> <p>8. $+3 - (+3)$ _____</p> <p>9. $-29 - (+23)$ _____</p> <p>10. $-21 - (+21)$ _____</p> <p>11. $+34 - (-23)$ _____</p> <p>12. $+56 - (-40)$ _____</p> <p>13. $-31 - (-13)$ _____</p> <p>14. $-90 - (+41)$ _____</p> <p>15. $+26 - (-50)$ _____</p> | <p>16. $-11 - (-51)$ _____</p> <p>17. $-14 - (-33)$ _____</p> <p>18. $-10 - (-22)$ _____</p> <p>19. $-28 - (+1)$ _____</p> <p>20. $-10 - (-40)$ _____</p> <p>21. $+20 - (-50)$ _____</p> <p>22. $-18 - (+7)$ _____</p> <p>23. $-21 - (-22)$ _____</p> <p>24. $-20 - (+20)$ _____</p> <p>25. $+2 - (-1) - (-2) - (+11)$ _____</p> <p>26. $+1 - (-3) - (+3) - (-10)$ _____</p> <p>27. $-10 - (-11) - (+12) - (-12)$ _____</p> <p>28. $-1 - (+1) - (+2) - (-3)$ _____</p> <p>29. $+12 - (-10) - (-11) - (+20)$ _____</p> <p>30. $+11 - (-10) - (-1) - (+2)$ _____</p> |
|---|--|

Word Problems

EXAMPLE

Subtract by adding the opposite.

$$-19 - (+10) + (-15)$$

$$-19 + (-10) + (-15) = -44$$

Directions Find these sums and differences.

- | | | | |
|---------------------------------|-------|------------------------------|-------|
| 1. $-2 - (+4) + (-7) - (+8)$ | _____ | 6. $+15 - (+16) + (+10)$ | _____ |
| 2. $-1 + (+33) + (-10) - (-10)$ | _____ | 7. $+11 - (-11) + (+10)$ | _____ |
| 3. $-10 + (-12) + (+19) - (-2)$ | _____ | 8. $-19 - (-19) + (+8)$ | _____ |
| 4. $+3 - (+4) - (+5) - (-7)$ | _____ | 9. $+2 - (-1) - (+7) - (+8)$ | _____ |
| 5. $-4 - (-7) + (+10) + (-8)$ | _____ | 10. $+11 + (-10) - (+13)$ | _____ |

Directions Write an addition sentence for each problem in the space provided and solve.

11. Marline's saving account had \$750.00 and she withdrew \$20.00 on Monday. She deposited \$100.00 on Tuesday. Wednesday she wrote a check for \$12.90. Thursday she deposited her paycheck of \$175.50. Friday she deposited \$100.00. How much was her final balance on Friday?
- _____
12. Starting at 70 degrees, if the temperature goes up 20 degrees, then drops 10 degrees, then goes up 14 degrees, what is the new temperature?
- _____
13. Milo spent \$30.00 for food and \$13.75 for camping supplies. He was paid \$12.00 for the trip. How much does he have?
- _____
14. Dante had the following expenses for his Lawn Care Service: \$2.75, \$5.00, \$10.00, \$8.00. He was paid \$22.00, \$25.00, \$15.00, and \$18.00. How much did he make after expenses?
- _____
15. Teresa spent \$5.95 at one store, \$6.32 at another, and \$15.98 at a third store. If she had \$35.00 before shopping, how much does she have left?
- _____

Multiplying Positive and Negative Integers

EXAMPLES

The product of two numbers with like signs will be positive.

$$-3(-4) = +12 \quad +2(+4) = +8$$

The product of two numbers with unlike signs will be negative.

$$-3(+7) = -21 \quad +4(-10) = -40$$

Directions Write the factor to make a correct sentence.

1. $-4(\quad) = -16$

6. $(+8) = -64$

11. $+9(\quad) = -27$

2. $+5(\quad) = +20$

7. $+19(\quad) = -38$

12. $(+4) = -48$

3. $(-6) = -18$

8. $(-22) = +66$

13. $-2(\quad)(-5) = -30$

4. $-7(\quad) = -14$

9. $-1(\quad) = -1$

14. $(-3)(+5) = +45$

5. $-6(\quad) = +24$

10. $+12(\quad) = -36$

15. $+5(+2)(\quad) = -20$

Directions Solve for the product.

16. $-5(-6) = \underline{\hspace{2cm}}$

24. $+9(-3)(-1) = \underline{\hspace{2cm}}$

17. $-4(+5) = \underline{\hspace{2cm}}$

25. $+5(-5)(-5) = \underline{\hspace{2cm}}$

18. $+7(-5) = \underline{\hspace{2cm}}$

26. $-1(-1)(-1)(-1) = \underline{\hspace{2cm}}$

19. $-23(+2) = \underline{\hspace{2cm}}$

27. $+2(-8)(-2)(-1) = \underline{\hspace{2cm}}$

20. $-2(-3)(-4) = \underline{\hspace{2cm}}$

28. $-4(+8)(-2) = \underline{\hspace{2cm}}$

21. $+3(-6)(-1) = \underline{\hspace{2cm}}$

29. $-3(+3)(-1)(-1) = \underline{\hspace{2cm}}$

22. $-9(+2)(-2) = \underline{\hspace{2cm}}$

30. $-7(+3)(+2) = \underline{\hspace{2cm}}$

23. $-7(-7)(+2) = \underline{\hspace{2cm}}$

Properties of Addition and Multiplication

EXAMPLES

Commutative Property of Addition and Multiplication

$$7 + 8 = 8 + 7$$

$$15 = 15 \quad \text{Both sums equal 15.}$$

$$-3 \times (-4) = -4 \times (-3)$$

$$+12 = +12 \quad \text{Both products equal +12.}$$

Associative Property of Addition and Multiplication

$$(6 + 2) + 8 = 6 + (2 + 8)$$

$$8 + 8 = 6 + 10$$

$$16 = 16$$

$$(5 \times 6) \times 2 = 5 \times (6 \times 2)$$

$$30 \times 2 = 5 \times 12$$

$$60 = 60$$

Distributive Property of Multiplication with Respect to Addition and Subtraction

$$3 \times (2 + 5) = 3 \times 2 + 3 \times 5$$

$$3 \times 7 = 6 + 15$$

$$21 = 21$$

$$4 \times (10 - 3) = 4 \times 10 - 4 \times 3$$

$$4 \times 7 = 40 - 12$$

$$28 = 28$$

Directions Write the property used for each expression.

1. $-2(-4) = -4(-2)$ _____

2. $(2 \times 4) \times 5 = 2 \times (4 \times 5)$ _____

3. $2 \times (15 - 3) = 2 \times 15 - 2 \times 3$ _____

4. $7 + (5 + 4) = (7 + 5) + 4$ _____

5. $11 + 16 = 16 + 11$ _____

6. $+8(+3) = +3(+8)$ _____

7. $(3 + 7) + 8 = 3 + (7 + 8)$ _____

Directions Solve these expressions.

8. $-9 \times (+8) =$

11. $23 + (45 + 20) =$

14. $-15(-10) =$

9. $-6(-8) =$

12. $(7 + 19) + 12 =$

15. $-3(-8) =$

10. $4 \times (12 - 7) =$

13. $(12 + 4) + 3 =$

Dividing Positive and Negative Integers

EXAMPLES

The quotient of two numbers with like signs will be positive.

$$-12 \div (-4) = +3 \text{ and } +20 \div (+5) = +4$$

Both answers are positive.

The quotient of two numbers with unlike signs will be negative.

$$+24 \div (-2) = -12 \qquad \frac{-16}{+2} = -8$$

Directions Solve for the quotients.

1. $-12 \div (+2) =$ _____

2. $-16 \div (+2) =$ _____

3. $+24 \div (+3) =$ _____

4. $-25 \div (-5) =$ _____

5. $+45 \div (-5) =$ _____

6. $+22 \div (-1) =$ _____

7. $+34 \div (-17) =$ _____

8. $+23 \div (+1) =$ _____

9. $-54 \div (-9) =$ _____

10. $+18 \div (-2) =$ _____

11. $-48 \div (+6) =$ _____

12. $-35 \div (-5) =$ _____

13. $+90 \div (-2) =$ _____

14. $+21 \div (-7) =$ _____

15. $+49 \div (-7) =$ _____

16. $-26 \div (-13) =$ _____

17. $-36 \div (+9) =$ _____

18. $-28 \div (+2) =$ _____

19. $\frac{-12}{-2} =$ _____

20. $\frac{+35}{-7} =$ _____

21. $\frac{+60}{-5} =$ _____

22. $\frac{-8}{-8} =$ _____

23. $\frac{+28}{-4} =$ _____

24. $\frac{-40}{+4} =$ _____

25. $\frac{+88}{-11} =$ _____

26. $\frac{+50}{+5} =$ _____

27. $\frac{+44}{-4} =$ _____

28. $\frac{-80}{+4} =$ _____

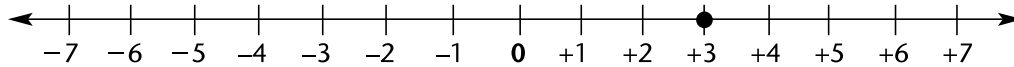
29. $\frac{+110}{-11} =$ _____

30. $\frac{+24}{+8} =$ _____

Variables and the Number Line

EXAMPLE

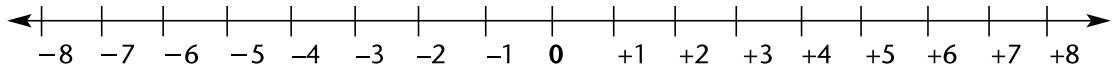
Find the number on the number line. Draw a dot there.



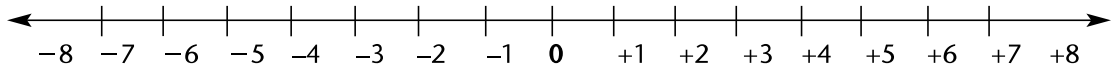
$x = 3$

Directions Graph these values of x on the number lines.

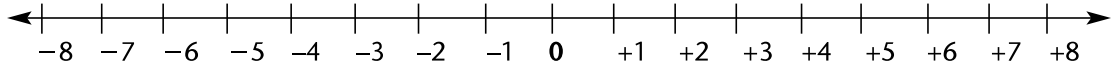
1. $x = 7$



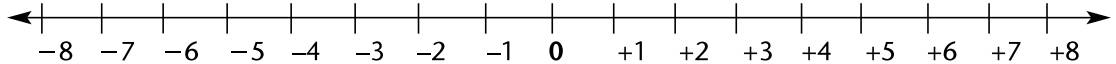
2. $x = -4$



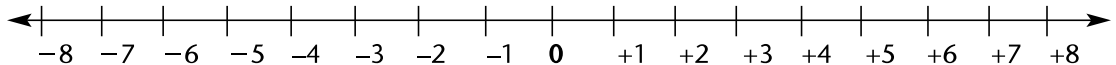
3. $x = -2$



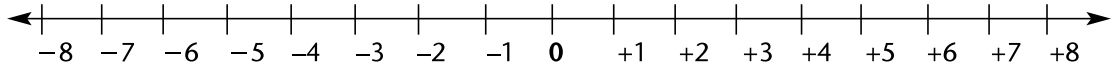
4. $x = +5$



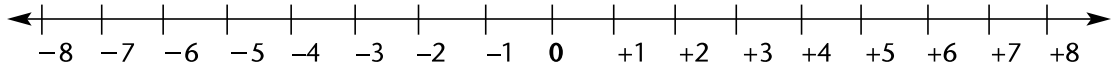
5. $x = -6$



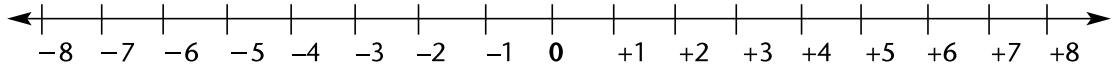
6. $x = -1$



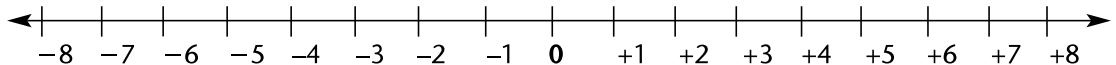
7. $x = -7$



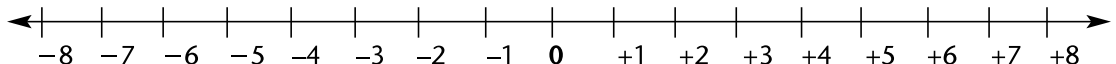
8. $x = -8$



9. $x = 0$



10. $x = 6$



Graphing Coordinates

EXAMPLE

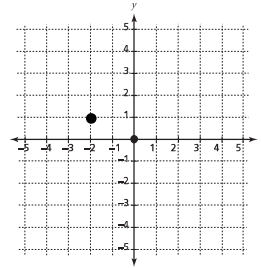
Number the x and y axes and graph the ordered pairs.

Plot $(-2, 1)$.

Find -2 on x on the graph.

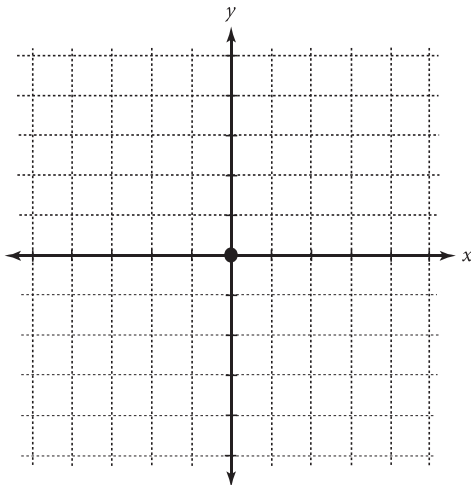
Find 1 on y on the graph.

Plot the point where they meet.

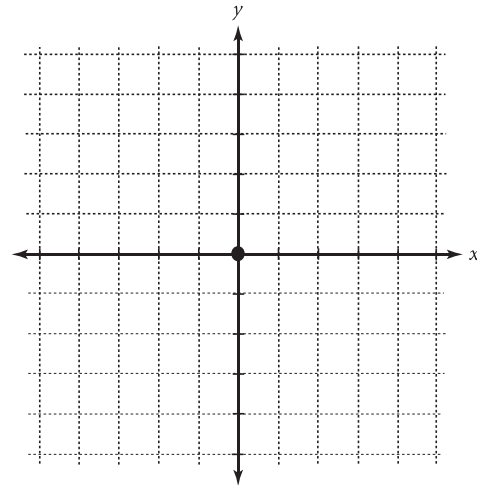


Directions Number the x and y axes and graph the ordered pairs.

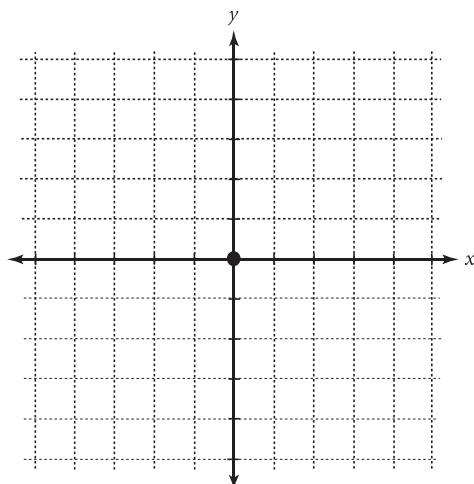
1. $(-3, 4)$ $(-5, -5)$ $(1, 4)$ $(0, -3)$ $(4, 0)$



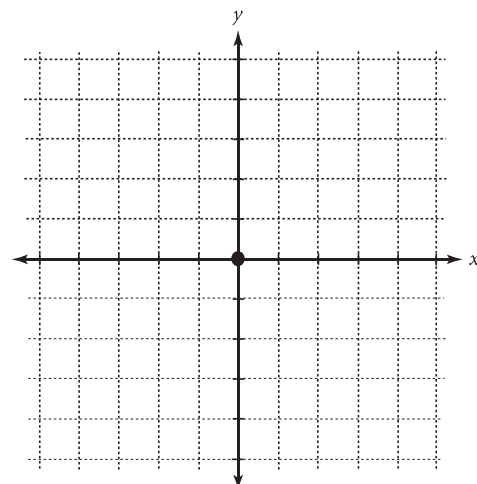
3. $(2, -5)$ $(-1, -1)$ $(-2, 4)$ $(5, -3)$ $(-4, -2)$



2. $(2, 1)$ $(3, -1)$ $(-2, 5)$ $(-4, 4)$ $(-3, -4)$



4. $(0, -1)$ $(0, 4)$ $(-4, 0)$ $(-1, 3)$ $(-4, 1)$



Solving Equations by Adding and Subtracting

EXAMPLESolve the equation. $x - 19 = +2$

$$x - 19 = +2$$

$$\underline{+19 = +19}$$

$$x + 0 = +21$$

$$x = +21$$

Directions Solve for the variable. Show steps.

1. $x - 2 = 10$

7. $x + 2 = -11$

13. $y + 1 = -12$

2. $x + 2 = 12$

8. $-3 + x = -9$

14. $8 = x - 11$

3. $x - 10 = 12$

9. $4 + x = -13$

15. $h - 13 = -23$

4. $x - 10 = -19$

10. $y - 12 = -3$

5. $x + 8 = -2$

11. $-9 + y = -23$

6. $x - 10 = 20$

12. $11 = x - 10$

Solving Equations by Multiplying and Dividing

EXAMPLESolve the equation. $-2x = 38$

$$-2x = 38$$

$$\frac{-2x}{-2} = \frac{38}{-2}$$

$$x = -19$$

Directions Solve for the variable. Show your work.

1. $4x = 20$

9. $\frac{x}{5} = 8$

17. $-2x = -46$

2. $5x = 25$

10. $\frac{y}{3} = 9$

18. $\frac{x}{4} = 23$

3. $7x = 56$

11. $\frac{k}{8} = 12$

19. $\frac{y}{-9} = 42$

4. $9x = 81$

12. $\frac{y}{10} = 14$

20. $-3k = 30$

5. $8y = 72$

13. $-7x = 42$

6. $8f = 96$

14. $\frac{k}{9} = 17$

7. $12x = 144$

15. $\frac{x}{-8} = 20$

8. $6x = 66$

16. $-7x = 35$

Two-Step Equations

EXAMPLE

Solve for the variable. Subtract 3 from both sides. Then divide each side by 2.

$$\begin{array}{r} 2x + 3 = 13 \\ -3 = -3 \\ \hline 2x = 10 \\ \frac{2x}{2} = \frac{10}{2} \\ x = 5 \end{array}$$

Directions Solve for the variables. Leave fractional answers as improper fractions. Show your work.

1. $3x + 4 = 14$

$x = \underline{\hspace{2cm}}$

2. $3y - 2 = 19$

$y = \underline{\hspace{2cm}}$

3. $3y - 8 = 16$

$y = \underline{\hspace{2cm}}$

4. $2y - 5 = -37$

$y = \underline{\hspace{2cm}}$

5. $6x + 1 = 27$

$x = \underline{\hspace{2cm}}$

6. $8k - 2 = 70$

$k = \underline{\hspace{2cm}}$

7. $6a - 1 = 22$

$a = \underline{\hspace{2cm}}$

8. $9a + 1 = 82$

$a = \underline{\hspace{2cm}}$

9. $7z - 2 = 22$

$z = \underline{\hspace{2cm}}$

10. $3a - 2 = 42$

$a = \underline{\hspace{2cm}}$

11. $4a + 1 = 35$

$a = \underline{\hspace{2cm}}$

12. $-2z - 2 = 33$

$z = \underline{\hspace{2cm}}$

13. $4x - 5 = 32$

$x = \underline{\hspace{2cm}}$

14. $7w + 1 = 29$

$w = \underline{\hspace{2cm}}$

15. $-5k - 7 = 76$

$k = \underline{\hspace{2cm}}$



Combining Like Terms

EXAMPLECombine like terms. Add the two terms. $-2a - 4a$

$$-2a$$

$$\underline{-4a}$$

$$-6a$$

$$\text{so } -2a - 4a = -6a$$

Directions Combine like terms.

1. $-7a - 6a$

8. $+7x + 2x - 10x$

15. $23c - 8c + c$

22. $+7 + 12a - 7a$

2. $+4a - 5a$

9. $-10y + 31y - y$

16. $9 - 17c + 5c$

23. $3 - x - x - 2x$

3. $-2c - 3c - 4c$

10. $-30f - 11f + 1$

17. $+a + a + 8$

24. $13x - 18x + 1$

4. $-4v - 3v$

11. $-17y + 20y - 2$

18. $-18y + 17y + 1$

25. $1 - 3f + 2f + 3$

5. $7x + 3x - x$

12. $4 - 8a - 3a$

19. $-2a - 3a + 5a$

6. $-x - 4x + 9x$

13. $-x - x + 4$

20. $12 + 12a - 24$

7. $-2x + 8x - x$

14. $+4c - 7c - c$

21. $-22 + 20y - y$

